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# Revealing decision-making strategies of Americans in taking COVID-19 vaccination

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**Efficient coverage for newly developed vaccines requires knowing which groups of individuals will accept the vaccine immediately and which will take longer to accept or never accept. Of those who may eventually accept the vaccine, there are two main types: success-based learners, basing their decisions on others' satisfaction, and myopic rationalists, attending to their own immediate perceived benefit. We used COVID-19 vaccination data to fit a mechanistic model capturing the distinct effects of the two types on the vaccination progress. We estimated that 47% of Americans behaved as myopic rationalists with a high variation across the jurisdictions, from 31% in Mississippi to 76% in Vermont. The proportion was correlated with the vaccination coverage, proportion of votes in favor of Democrats in 2020 presidential election, and education score.**

## 1 Introduction

Vaccination is a primary measure to reduce morbidity and mortality of new infectious diseases (1), especially in areas that admit high coverage (2). High vaccination coverage requires high vaccine acceptance—a collective outcome of individual-level decision-making processes (3). Particularly, when facing a new vaccine, people need to decide between the promised immunity followed by potential side-effects associated with accepting the vaccine versus the mortality risk and governmental restrictions of refusing the vaccine. Individuals, however, vary in their decision-making strategies (4–6), and different strategy compositions can result in different collective outcomes (7), including different vaccination rates and coverage (8, 9). Effec-

24 tive promotion of vaccination benefits from identifying the different types of decision-makers  
25 and deploying tailored communication methods.

26 In various contexts, people are known to be mainly one of the following two decision-  
27 making types (6, 7, 10, 11): (i) those who learn from others' success, particularly, those who  
28 take the action of others with a higher payoff, known as *success-based learners* (12), or *imita-*  
29 *tors* (13), and (ii) those who base their decisions on their own perceptions of the environment,  
30 often aiming to maximize their instant perceived payoff (5, 6), named *myopic rationalists*, or  
31 *best-responders* (14). Exclusive populations of myopic rationalists who perceive the social con-  
32 text similarly are likely to reach satisfactory decisions (15) whereas exclusive populations of  
33 success-based learners may undergo perpetual changes of decisions (12, 16, 17). Mixed popula-  
34 tions of the two may exhibit a wide range of behaviors depending on the proportions (8, 18, 19).  
35 Understanding the collective outcome of mixed populations, hence, requires knowing the pro-  
36 portions of success-based learners and myopic rationalists.

37 The two types of decision makers also differ in the type of information they attend to (12).  
38 Myopic rationalists seek information that shapes their payoffs, whereas success-based learners  
39 focus on the satisfaction achieved by others. Hence, in addition to providing insights to the  
40 vaccination dynamics, knowing the proportions of the two types inform health management  
41 and media.

42 The proportion, however, is unknown and needs to be estimated from data – a yet unaccom-  
43 plished challenging task. The challenge is mainly because the proportions of decision-makers  
44 are unobserved. A natural approach to tackle this problem is to build a mechanistic model  
45 with the proportion of decision-makers as a parameter and estimate it by fitting the equations  
46 to existing data on measured quantities such as vaccine uptake. However, for this approach to  
47 be successful, it must be first shown that such a parameter is identifiable. Several other chal-  
48 lenges exist. There may be insufficient detail in data from previous seasonal or relatively old  
49 diseases, where decisions were made typically once a year (20, 21) or lifetime (22). Baseline  
50 trust regarding a vaccines' effectiveness and safety may change as an initially distrustful public  
51 gradually becomes accustomed to it (23). The resulting hesitancy followed by the desire for  
52 immunity results in frequent decision revisions, e.g., on a bi-weekly basis (23). Finally, not all  
53 the population may be concerned about the vaccine as can be seen in some previously recorded  
54 vaccination programs (24).

55 The recorded data on COVID-19 in the US provides a unique opportunity to tackle each  
56 of these challenges. Although the proportion is unobservable, the two decision-making groups  
57 have different vaccination paces and differently shape the vaccination progress curve, which  
58 is observable. Indeed, we prove that the proportion of myopic rationalists is an identifiable  
59 parameter. Hence, by fitting the collective decision-making dynamics of the two types to vacci-  
60 nation data, we can estimate the proportion and use bootstrapping methods to obtain confidence  
61 intervals. Owing to the importance of timely vaccination and thanks to the advancement of tech-  
62 nology, the vaccination data are available on a daily basis (25). The changes in baseline attitude  
63 toward the vaccine's side effects were captured through longitudinal surveys (26). Moreover,  
64 almost every resident had to decide on vaccination (27).

65 Our objective was to estimate the proportions of myopic rationalists and success-based  
66 learners in each of the 50 states of the US and the District of Columbia (D.C.) separately, in de-  
67 ciding whether to take first dose of COVID-19 vaccination. We excluded later doses as they are  
68 influenced by the experience in the first dose (28). We developed a mechanistic model to cap-  
69 ture the behavior of the two types of interacting individuals augmented by a third group *vaccine*  
70 *refusers*, those *a priori* known to refuse the vaccine based on surveys (29). A fixed parameter  
71 ( $\alpha$ ) was used as the proportion of myopic rationalists in the population in each jurisdiction. The  
72 perceived excess payoff of vaccination is shaped by the epidemiological conditions represented  
73 by weekly cases and deaths, the risk of vaccine side effects, and the social and governmental  
74 pressure on unvaccinated individuals.

## 75 **2 Materials and Methods**

76 In this section, we describe the data collection procedure and the model developed to capture  
77 the vaccination progress among myopic rationalists and success-based learners. Additionally,  
78 we describe the utilized parameter estimation and inference approaches.

### 79 **2.1 Data Collection**

80 To calculate the cumulative number of available COVID-19 vaccine doses for administering the  
81 first shot, we used the temporal data on the number of delivered doses to each jurisdiction’s  
82 provider locations. The data were available on the website of Centers for Disease Control and  
83 Prevention (CDC) (30) and captured the last part of the vaccine distribution process (31). To  
84 estimate the number of allocated doses for the first shot, the number of individuals completing  
85 the primary series of a two-dose vaccine, as well as the numbers of those receiving the first and  
86 the second booster doses were subtracted from the data. In majority of the US jurisdictions,  
87 the decision whether to vaccinate children under the age of 12 was left up to their guardians  
88 (32). Hence, we narrowed the population to those of 12 years and older. As the emergency  
89 authorization of vaccinating children of age 5 through 11 was issued on late October, 2021, we  
90 set October 31, 2021 as the last day of the dataset (33).

91 December 14, 2020 was selected as the starting date. Daily data on the total number of  
92 individuals who received their first dose, the number of individuals who completed the primary  
93 course of vaccination, and the number of individuals who received their first and second booster  
94 doses were collected from (34). State-level data on daily new COVID-19 cases and deaths were  
95 obtained from (35). We converted the temporal scale from daily to weekly.

96 The estimated percentage of strongly hesitant adults, available on “state\_hesitancy\_estimates”  
97 sheet of the Excel file “Predicted Vaccine Hesitancy by State, PUMA, and County” (29), was  
98 expressed as proportion and then used as the state-wide estimated proportion of COVID-19 vac-  
99 cine refusers. To estimate the trend of the reduction in the perceived risk of vaccine side-effects,  
100 we used the data collected by the US Census Bureau (26). To determine the start date at which

101 containment, closure or health policies differentiated based on individuals' vaccination status,  
 102 we used the US sub-national data available in (25). The data on the state-level population by  
 103 age was obtained from (36).

104 We additionally explored a number of variables that could possibly relate to the propor-  
 105 tions of success-based learners and rationalists. We collected data on votes in favor of each  
 106 political party from (37), income per capita and the proportion of people below the poverty line  
 107 from (38), and the state-level education score from (39). The data on education score were origi-  
 108 nally in the interval of  $[0, 100]$  and we scaled them to  $[0, 1]$ . Data on the number of potential  
 109 vaccination facilities per 10K residents and the proportion of population with driving distance  
 110 greater than 10 miles to the closest potential vaccination facility were obtained from (40). The  
 111 methodology was elaborated in (41). The data on age, sex distribution, education level distri-  
 112 bution, number of intensive care unit beds, ventilator capacity, percent insured residents, meat  
 113 plants, religious congregation ratio, and immigrant student ratio were obtained from (42).

## 114 2.2 Model Formulation

115 We modeled the vaccination progress as the collective outcome of the vaccination behaviour of  
 116 two decision-making types: myopic rationalists and success-based learners. In this regard, for  
 117 each jurisdiction, a large, fixed population of  $N$  interacting individuals aged 12 and above is  
 118 considered. An unknown fixed portion  $\alpha$  are myopic rationalists, a known fixed portion (see  
 119 Section 2.1) are COVID-19 vaccine refusers, and the remainder are success-based learners.

120 It is assumed that non vaccine refusers, i.e., myopic rationalists and success-based learn-  
 121 ers decide based on the perceived excess payoff for receiving a dose of a COVID-19 vaccine,  
 122 denoted by  $\Delta\pi(t)$ . Myopic rationalists go for vaccination if their perceived payoff for vaccina-  
 123 tion is larger than that of remaining unvaccinated, that is,  $\Delta\pi > 0$ , while success-based learners  
 124 base their decisions on their interactions with others in the population: Upon an interaction, an  
 125 unvaccinated success-based learner compares their own payoff with those of others, who may  
 126 be vaccinated or unvaccinated. Unvaccinated others conceive the same payoff as the unvacci-  
 127 nated success-based learner, resulting in no learning. If vaccinated others have a higher payoff,  
 128 the success-based learners consider receiving vaccination with a probability proportional to the  
 129 perceived excess payoff for vaccination  $\Delta\pi$ . We hence consider a two-state differential equa-  
 130 tion, where one state models the evolution of vaccination progress among myopic rationalists  
 131 and the other one captures that of success-based learners.

The myopic rationalists follow the *best-response dynamics* (43), that is, unvaccinated my-  
 opic rationalists compare the payoff for vaccination with that of remaining unvaccinated and  
 become vaccine seekers if the excess payoff is positive, i.e.,

$$\begin{array}{c} \text{number of} \\ \text{vaccine-seeker myopic} \\ \text{rationalists} \end{array} \underbrace{M_s(t)} = \underbrace{\begin{array}{c} \text{number of} \\ \text{unvaccinated} \\ \text{myopic rationalists} \end{array}}_{(\alpha_1 N_n - M_v(t))} \underbrace{\begin{array}{c} \text{sign indicator of} \\ \text{excess payoff} \end{array}}_{H(\Delta\pi(t))}, \quad (1)$$

132 where  $M_s(t)$  denotes the number of vaccine-seeker myopic rationalists at time  $t$ ,  $\alpha_1$  denotes the

133 proportion of myopic rationalists in the total number of myopic rationalists and success-based  
 134 learners,  $N_n$ ,  $M_v(t)$  denotes the number of vaccinated myopic rationalists until time  $t$ , and  $H(\cdot)$   
 135 equals one for a positive argument and zero otherwise.

136 At it mentioned earlier, the success-based learners learn via interaction with others. When an  
 137 unvaccinated success-based learner meets vaccinated individuals, if those vaccinated individu-  
 138 als have a higher payoff, the success-based learner becomes a vaccine-seeker with a probability  
 139 proportional to the excess payoff. The number of vaccine-seeker success-based learners at time  
 140  $t$  is then

$$\underbrace{L_s(t)}_{\text{number of vaccine-seeker success-based learners}} = \underbrace{((1 - \alpha_1)N_n - L_v(t))}_{\text{number of unvaccinated success-based learners}} \underbrace{\frac{L_v(t) + M_v(t)}{N}}_{\text{proportion of vaccinated individuals}} \underbrace{\sigma[\Delta\pi(t)]_+}_{\text{dimensionless excess payoff}}, \quad (2)$$

141 where  $L_s(t)$  is the number of vaccine-seeker success-based learners at time  $t$ ,  $L_v(t)$  is the num-  
 142 ber of vaccinated success-based learners until time  $t$ ,  $\sigma$  is the constant of proportionality (44),  
 143 and  $[x]_+$  equals  $x$  if  $x > 0$  and equals zero otherwise. We focused on the first dose, indicating  
 144 that vaccinated individuals never changed their strategies.

145 Providing there are sufficient vaccine doses, each vaccine seeker can get vaccinated. In the  
 146 presence of vaccine limitations, however, not all vaccine seekers can be inoculated at once. In  
 147 this case, it is assumed that the available doses are assigned randomly to the vaccine seekers  
 148 of each group of decision-making types. The per capita available vaccine doses for vaccine  
 149 seekers can be formulated as  $v(t)/(L_s(t) + M_s(t))$  where  $v(t)$  denotes the number of available  
 150 doses at time  $t$  for the first shot and  $L_s(t) + M_s(t)$  represents the total demand for vaccination  
 151 at time  $t$ . Having  $v(t)/(L_s(t) + M_s(t)) > 1$  simply means that given the available doses, each  
 152 vaccine seeker has the opportunity to receive the vaccine. The rate of change of vaccinated  
 153 myopic rationalists can be written as

$$\underbrace{\dot{M}_v(t)}_{\text{rate of change of vaccinated myopic rationalists}} = \underbrace{\kappa}_{\text{max rate of vaccination}} \underbrace{M_s(t) \min\left\{1, \frac{v(t)}{L_s(t) + M_s(t)}\right\}}_{\text{number of vaccine-seeker myopic rationalists who can get a vaccine}}, \quad (3)$$

154 where  $\kappa$  represents the maximum vaccination rate. Similarly, for the rate of change of  
 155 vaccinated success-based learners, we have

$$\underbrace{\dot{L}_v(t)}_{\text{rate of change of vaccinated success based learners}} = \underbrace{\kappa}_{\text{max rate of vaccination}} \underbrace{L_s(t) \min\left\{1, \frac{v(t)}{L_s(t) + M_s(t)}\right\}}_{\text{number of vaccine-seeker success-based learners who can get a vaccine}}. \quad (4)$$

156 The difference between the rate of change of vaccinated success-based learners and that  
 157 of myopic rationalists stems from their respective number of vaccine seekers. Once the excess  
 158 payoff for vaccination is positive, all unvaccinated myopic rationalists become a vaccine seeker,  
 159 irrespective of the vaccination coverage. However, the number of vaccine-seeker success-based  
 160 learners is affected by the value of the excess payoff and the vaccination coverage–(2). For  
 161 example, at day zero, when no one is vaccinated, no success-based learner is vaccine seeker,  
 162 whereas all myopic rationalists are vaccine seekers if the excess payoff is positive. Conse-  
 163 quently, the vaccination progress at the beginning of the vaccine roll-out is mainly shaped by  
 164 the myopic rationalists.

It is assumed that both types of decision-makers conceive the same excess payoff for receiving a dose of COVID-19 vaccine which is defined by

$$\Delta\pi(t) = \underbrace{c_{\bar{v}} - c_{v_0}(t - t_0 + 1)^\lambda}_{C_v(t)} + C_d \frac{D(t)}{N} + C_i \frac{I(t)}{N}, \quad (5)$$

165 where  $N$  is the total population including children,  $I(t)$  is the weekly number of confirmed  
 166 COVID-19 cases, and  $D(t)$  is the weekly number of confirmed deaths from COVID-19 as a  
 167 function of time. The conceived excess payoff for vaccination comprises of three terms: First,  
 168 the quantity  $C_s(t)$  is the perceived benefit of vaccination in the absence of confirmed cases or  
 169 deaths and is equal to the perceived risk of remaining unvaccinated in a disease-free situation,  
 170  $c_{\bar{v}}$  minus the perceived risk of vaccine associated side-effects,  $C_v(t)$ , i.e.,  $C_s(t) = c_{\bar{v}} - C_v(t)$ .  
 171 Second, the perceived vaccine-induced risk reduction of dying from COVID-19,  $C_d$ , that is  
 172 the perceived normalized value of an actual life times the perceived effectiveness of the first  
 173 dose, multiplied by  $D(t)/N$ , which is the perceived chance of death from COVID-19. Third,  
 174 the perceived vaccine-induced risk reduction of COVID-19 infection is defined similarly as  
 175  $C_i I(t)/N$ . According to Household Pulse survey, a longitudinal survey conducted by Census  
 176 Bureau, the perceived risk of vaccine associated side-effects declines over time (23). Our fitting  
 177 result indicates that this decreasing trend can be best described by a power law function of the  
 178 form  $(t - t_0 + 1)^\lambda$ ,  $\lambda < 0$  (see SI). Hence,  $C_v(t)$  is replaced with  $c_{v_0}(t - t_0 + 1)^\lambda$  where  $c_{v_0}$   
 179 is a free parameter (see SI). The perceived risk of remaining unvaccinated in the absence of  
 180 confirmed deaths or cases is modeled by a free parameter,  $c_{\bar{v}}$ .

### 181 2.3 Parameter Estimation

182 The parameters  $\{\alpha_1, c_{v_0}, c_{\bar{v}}, C_i, \sigma, \kappa\}$  were estimated by fitting the derived equations to time  
 183 series data. For each jurisdiction, the valid interval for  $C_i$  was capped at  $\min_t D(t)/I(t)$  for a  
 184 nonzero  $D(t)$  to limit the impact of morbidity on the excess payoff by that of mortality. The  
 185 valid intervals for  $c_{v_0}$  and  $c_{\bar{v}}$  were capped at 1. The valid interval for  $\kappa$  was set to  $[0, 10]$ . The  
 186 constant of proportionality  $\sigma$  was bounded at 1.

187 A time-varying  $c_{\bar{v}}$  was also considered to capture the possible impacts of differentiating  
 188 policies based on the vaccination status on the perceived excess payoff for vaccination. In this

189 regard,  $c_{\bar{v}}$  is allowed to be varying over the time following a piece-wise-linear function—Fig  
190 S1. A time-varying  $c_{\bar{v}}$  was captured by three additional parameters, i.e.,  $s_f$ ,  $\eta$ , and  $s_u$ . More  
191 specifically, as of the announcement date of the differentiating policies, a linear increment in  
192 the perceived cost of remaining unvaccinated is introduced with a start value,  $c_{\bar{v}_0}$ , inclination,  
193  $s_u$ , and the peak value,  $\eta c_{\bar{v}_0}$ , as free parameters. The increment was then followed by a linear  
194 reduction whose inclination was a free parameter denoted by  $s_f$ .

195 The initial conditions,  $L_v(0)$ ,  $M_v(0)$  were set to zero. For each US state and D.C., the  
196 power law exponent  $\lambda$  was estimated using the available data on the Americans’ concern about  
197 vaccine side-effects (see SI). We fit the model to the reported number of weekly vaccinated  
198 individuals, i.e.,  $n_v[k] = N_v[k] - N_v[k - 1]$  with  $n_v[0] = N_v[0]$ . The error function was chosen  
199 to be the residual sum of squares, i.e.,  $\sum_k ||n_v[k] - \hat{n}_v[k]||^2$ , where  $\hat{n}_v[k]$  denotes the estimated  
200 number of those who received their first dose of COVID-19 vaccine at time  $k$ . The error was  
201 minimized using the dual annealing optimization algorithm (45) and its Python implementation  
202 (46). The control parameters *initial\_temp* and *maxiter* were set to 50000 and 1000, respectively.  
203 The algorithm was executed with five distinct seeds—2023, 2024, 2025, 2026, 2027—for each  
204 jurisdiction. For each jurisdiction, the set of parameters corresponding to the least sum of  
205 squared residuals was selected from the five obtained sets.

206 We obtained the 95% confidence intervals of the estimated parameters using both parametric  
207 and non-parametric bootstrapping approaches. Following (47) 500 bootstrapped datasets were  
208 synthesized. For implementing the parametric bootstrap, for each time  $k$ , we assumed a Poisson  
209 error structure whose mean was the estimated number of newly vaccinated individuals at  $k$ . For  
210 each bootstrapped dataset, the number of newly vaccinated individuals at time  $k$  was drawn  
211 from the constructed Poisson distribution for week  $k$  (48). To synthesize the datasets based  
212 on the non-parametric approach, due to serial correlation between residual data points, an auto-  
213 regressive model was constructed and out of the resultant uncorrelated residuals, 500 time-series  
214 were drawn with replacements (49); see SI for more details. The 95% confidence interval was  
215 then calculated using the percentile approach (50).

216 After inferring the parameters of the excess payoff function with a time-varying  $c_{\bar{v}}$ , it turned  
217 out that the a time-varying  $c_{\bar{v}}$  imposes high variability in the estimated parameters (Tables S17-  
218 S24). We, hence, modeled  $c_{\bar{v}}$  as a constant free parameter. In addition, it turned out that  
219 although  $\sigma$  was identifiable (Subsection 3.1), its point estimate was not reliable (Table S16).  
220 Hence, it was set to one. Fixing the constant of proportionality to one, did not, however, impact  
221 the estimated value of our parameter of interest, i.e.,  $\alpha_1$ . More specifically, the percentage of  
222 variations in the estimated  $\alpha_1$  was less than 10% for all jurisdictions. Therefore, the fitting  
223 results of the model, where  $\sigma$  was set to one and  $c_{\bar{v}_0}$  was treated as a time-invariant parameter,  
224 were reported in Subsection Fitting Results.

## 225 2.4 Correlation with Explanatory Variables

226 The linear correlations between a variety of variables—including socio-economic factors, vacci-  
227 nation coverage, and voting behaviour—and the estimated proportion of people who behaved like

228 myopic rationalists in taking the first dose of COVID-19 vaccine  $\alpha$  were investigated. There was  
 229 insufficient data available for the D.C. across most potential explanatory variables. Additionally,  
 230 the distribution of the proportion of myopic rationalists did not follow a normal distribution, as  
 231 indicated by the Shapiro test. The distribution, however, became normal by excluding the D.C.  
 232 and the state of Vermont. Consequently, these two jurisdictions were excluded from the linear  
 233 regression analysis.

234 As for the linear correlation analysis, we used Pearson-r coefficient and the simple linear  
 235 regression was performed using the Python implementation of Ordinary Least Squares (51). To  
 236 check whether the assumptions of simple linear regressions were satisfied, we utilized Shapiro-  
 237 Wilk test, which is a test of normality (52), and also Breusch-Pagan test to test the presence of  
 238 heteroscedasticity in a regression model (53).

### 239 3 Main Results

240 In this section, we provide the identifiability analysis of the developed model and report the  
 241 fitting results.

#### 242 3.1 Identifiability Analysis

243 In this section, we investigate the identifiability of the parameters  $\alpha_1, \kappa, c_{v_0}, \sigma, C_i,$  and  $c_{\bar{v}}$ , that  
 244 is whether theoretically it is possible to uniquely determine these parameters by observing the  
 245 accumulated number of vaccinated individuals over time. There are a variety of definitions of  
 246 parameter/model identifiability (54). We consider the following definition.

247 **Definition 1** Consider the following dynamical system

$$\Sigma^\theta = \begin{cases} \dot{\mathbf{x}}(t) = \mathbf{f}(\mathbf{x}(t), \mathbf{u}(t), \boldsymbol{\theta}), & \mathbf{x}_0 = \mathbf{x}(0), \\ \mathbf{y}(t, \boldsymbol{\theta}) = \mathbf{h}(\mathbf{x}(t), \boldsymbol{\theta}), \\ t \in \mathbb{R}_{\geq 0}, \\ \mathbf{x} \in \mathcal{X} \subseteq \mathbb{R}^x, \mathbf{u} \in \mathcal{U} \subseteq \mathbb{R}^u, \mathbf{y} \in \mathcal{Y} \subseteq \mathbb{R}^y, \boldsymbol{\theta} \in \Theta \subseteq \mathbb{R}^\theta. \end{cases} \quad (6)$$

Parameter  $\theta_i$  of (6) is said to be uniquely identifiable if for almost every  $\boldsymbol{\theta}' \in \Theta$ , every input  $\mathbf{u}$  in  $\mathcal{U}$ , and the given initial condition  $\mathbf{x}_0$ , the following holds:

$$\forall t \geq 0 \quad y(t, \boldsymbol{\theta}) = y(t, \boldsymbol{\theta}') \implies \theta_i = \theta'_i.$$

248 For the sake of readability, the multiplication of the excess payoff  $\Delta\pi(t)$  and the constant of  
 249 proportionality  $\sigma$  is represented as  $\sum_{i=0}^{i=3} c_i u_i(t)$ . The coefficients  $c_i$ s are as follows:  $c_0 = \sigma c_{v_0}$ ,  
 250  $c_1 = \sigma c_{\bar{v}}$ ,  $c_2 = \sigma C_i$ , and  $c_3 = C_d \sigma$ . The actual effectiveness of the first dose in death prevention  
 251 was estimated to be 85% (55). Its perceived effectiveness is set equal to 100%, and the perceived  
 252 normalized value of life is chosen to be 1 (the highest possible value), resulting in  $C_d = 1$  and in

253 turn  $c_3 = \sigma$ . The inputs  $u_i$ s,  $i = 0, \dots, 3$ , are  $u_0(t) = -(t - t_0 + 1)^\lambda$ ,  $u_1(t) = 1$ ,  $u_2(t) = I(t)/N$ ,  
 254 and  $u_3(t) = D(t)/N$ , where  $N$  is the total population and assumed to be fixed and known.

255 In the following, the cumulative number of vaccinated success-based learners  $L_v(t)$  and the  
 256 cumulative number of vaccinated myopic rationalists  $M_v(t)$  are denoted by  $x_1(t)$  and  $x_2(t)$ ,  
 257 respectively. The success-based learner and myopic rationalist dynamics are then rewritten as

$$\begin{aligned}
 M_s(t) &= (\alpha_1 N_n - x_2(t))H(\Delta\pi(t)), \\
 L_s(t) &= ((1 - \alpha_1)N_n - x_1(t))\frac{x_1(t) + x_2(t)}{N}\sigma[\Delta\pi(t)]_+, \\
 \dot{x}_1(t) &= \kappa L_s(t) \min\left\{1, \frac{u_4(t) - x_1(t) - x_2(t)}{L_s(t) + M_s(t)}\right\}, \\
 \dot{x}_2(t) &= \kappa M_s(t) \min\left\{1, \frac{u_4(t) - x_1(t) - x_2(t)}{L_s(t) + M_s(t)}\right\}, \\
 y(t) &= x_1(t) + x_2(t),
 \end{aligned} \tag{7}$$

258 where the accumulated number of COVID-19 vaccine doses distributed for the first shot up to  
 259 time  $t$  is denoted by  $u_4(t)$ . The accumulated number of vaccinated people  $x_1(t) + x_2(t)$  is the  
 260 measured output denoted by  $y(t)$ .

261 A negative perceived excess payoff  $\Delta\pi(t)$  means that no one will get vaccinated and in turn  
 262  $\dot{y}(t)$  will be equal to zero. However, during the course of COVID-19 vaccination, the number of  
 263 weekly vaccinated individuals was always greater than zero (34). Hence, we make the following  
 264 assumption.

265 **Assumption 1** *There exists some  $T > 0$  such that for all  $t \in [0, T)$ , the excess payoff  $\Delta\pi(t)$  is*  
 266 *positive. The time interval  $T$  is sufficiently large for the identification purpose.*

267 Inputs  $u_0$  and  $u_1$  are differentiable. In the following assumption, we further assume that  
 268 the number of confirmed cases, deaths, and the accumulated number of distributed COVID-19  
 269 vaccine doses are differentiable.

270 **Assumption 2** *The inputs  $u_i$ ,  $i = 2, \dots, 4$ , are differentiable.*

271 During the first months of COVID-19 vaccine roll-out, there was vaccine supply limitation, and  
 272 then the shortage was relaxed. This observation motivates the following assumption.

273 **Assumption 3** *There exists some  $t_1 \in (0, T)$  such that*

$$\begin{cases} u_4(t) - x_1(t) - x_2(t) < L_s(t) + M_s(t) & \text{if } t < t_1, \\ u_4(t) - x_1(t) - x_2(t) > L_s(t) + M_s(t) & \text{otherwise.} \end{cases} \tag{8}$$

274 *In words, the vaccination demand was higher than the available vaccine doses for  $t < t_1$ , and*  
 275 *for  $t > t_1$  the limitation was eased.*

276 In view of eq. (7),  $\sigma y(t)\Delta\pi(t)/N$  is indeed the proportion of vaccine-seeker success-based  
 277 learners, and therefore, it does not exceed one.

278 **Assumption 4** For all  $t \in [0, T)$ , where  $T$  was defined in Assumption 1,  $\sigma y(t)\frac{\Delta\pi(t)}{N} < 1 - \epsilon$  for  
 279 an arbitrary positive constant  $\epsilon$ .

280 In this paper, the population of individuals aged 12 and above, the total population, and the  
 281 population of non vaccine refusers are obtained from the available sources (29,36). This justifies  
 282 the next assumption.

283 **Assumption 5** The population of individuals of age 12 and above  $N$ , the total population  $N$ ,  
 284 and the population of non vaccine refusers  $N_n$  are known and fixed.

285 In our model  $\mathcal{U}$  is the set of inputs satisfying Assumptions 1-4, and  $\Theta$  is defined as  $\{\theta \in$   
 286  $\mathbb{R}^6 | \theta_1, \theta_3, \theta_4 \geq 0 \text{ and } 0 \leq \theta_2 \leq 1\}$ , where  $\theta_1 = \kappa, \theta_2 = \alpha_1, \theta_3 = \sigma, \theta_4 = C_i, \theta_5 = c_{\bar{v}}, \theta_6 = c_{v_0}$ .

287 **Proposition 1** Consider the dynamical system (7) with the single output  $y(t)$  and five inputs,  
 288  $u_i, i = 0, \dots, 4$ . Provided that Assumptions 1-5 hold, the parameters  $\kappa, \alpha_1, \sigma, C_i, c_{\bar{v}}$ , and  $c_{v_0}$   
 289 are uniquely identifiable.

**Proof.** Assume that we are given two systems  $S$  and  $S'$  described by (7) with parameter sets  
 $(\kappa, \alpha_1, \sigma, C_i, c_{\bar{v}}, c_{v_0})$  and  $(\kappa', \alpha'_1, \sigma', C'_i, c'_{\bar{v}}, c'_{v_0})$ , respectively. Moreover, assume that these sys-  
 tems have the same initial conditions, outputs, and inputs. To show the identifiability of the  
 parameters, we need to conclude that

$$(\kappa, \alpha_1, \sigma, C_i, c_{\bar{v}}, c_{v_0}) = (\kappa', \alpha'_1, \sigma', C'_i, c'_{\bar{v}}, c'_{v_0}). \quad (9)$$

For the time interval  $t \in (t_1, T)$ , where there is no dose limitation, we construct a generalized  
 input-output equation (for more information on the notion of generalized input-output equa-  
 tions, please refer to (56)). In this regard, a differential polynomial based on (7) should be  
 calculated which does not contain  $x_1, x_2$ , or their derivatives. In view of (7) and Assumptions 1  
 and 4,

$$\begin{aligned} x_1(t) &= y(t) - x_2(t), \\ \dot{y}(t) &= \kappa((1 - \alpha_1)N_n - y(t) + x_2(t))\frac{y(t)}{N}\sigma\Delta\pi(t) + \kappa(\alpha_1N_n - x_2(t)). \end{aligned}$$

Considering Assumptions 2 and 3, we will have

$$\begin{aligned}
& \left(1 - \frac{y(t)\sigma\Delta\pi(t)}{N}\right) \frac{\dot{y}(t)}{\kappa} = \left(\kappa\left(1 - \frac{y(t)\sigma\Delta\pi(t)}{N}\right) + y(t)\frac{\sigma\dot{\Delta}\pi(t)}{N} + \dot{y}(t)\frac{\sigma\Delta\pi(t)}{N}\right) \times \\
& \left(-\frac{\dot{y}(t)}{\kappa} - \frac{y^2(t)\sigma\Delta\pi(t)}{N} + \alpha_1 N_n + (1 - \alpha_1)N_n \frac{y(t)}{N} \sigma\Delta\pi(t)\right) \\
& - \kappa\alpha_1 N_n \left(1 - \frac{y(t)\sigma\Delta\pi(t)}{N}\right)^2 + (1 - \alpha_1)N_n \frac{\dot{y}(t)}{N} \sigma\Delta\pi(t) \left(1 - \frac{y(t)\sigma\Delta\pi(t)}{N}\right) + \\
& (1 - \alpha_1)N_n \frac{y(t)}{N} \sigma\dot{\Delta}\pi(t) \left(1 - \frac{y(t)\sigma\Delta\pi(t)}{N}\right) - 2y(t)\dot{y}(t) \frac{\sigma\Delta\pi(t)}{N} \left(1 - \frac{y(t)\sigma\Delta\pi(t)}{N}\right) \\
& - \frac{y^2(t)}{N} \sigma\dot{\Delta}\pi(t) \left(1 - \frac{y(t)\sigma\Delta\pi(t)}{N}\right), \tag{10}
\end{aligned}$$

which results in

$$\begin{aligned}
& \frac{\ddot{y}(t)y(t)}{N\kappa} \sum_{i=0}^{i=3} c_i u_i(t) - \frac{1}{\kappa} \ddot{y}(t) - \dot{y}(t) - \frac{y(t)\dot{y}(t)}{N} \sum_{i=0}^{i=3} c_i u_i(t) + \\
& \frac{\dot{y}(t)y^2(t)}{N^2} \left(\sum_{i=0}^{i=3} c_i u_i(t)\right)^2 - \frac{\dot{y}^2(t)}{\kappa N} \sum_{i=0}^{i=3} c_i u_i(t) - \frac{\kappa}{N} y^2(t) \sum_{i=0}^{i=3} c_i u_i(t) + \frac{\kappa}{N^2} y^3(t) \left(\sum_{i=0}^{i=3} c_i u_i(t)\right)^2 + \\
& \frac{\kappa}{N} N_n y(t) \sum_{i=0}^{i=3} c_i u_i(t) - \frac{\kappa}{N^2} N_n y^2(t) \left(\sum_{i=0}^{i=3} c_i u_i(t)\right)^2 + \\
& \frac{N_n \dot{y}(t)}{N} \left(\sum_{i=0}^{i=3} c_i u_i(t)\right) + \left(-\frac{y^2(t)}{N} - \frac{y(t)\dot{y}(t)}{\kappa N} + \frac{y(t)N_n}{N}\right) \sum_{i=0}^{i=3} c_i \dot{u}_i(t) = 0. \tag{11}
\end{aligned}$$

According to (56), for single-output systems, the coefficients of a generalized input-output equation are identifiable. The following coefficients of the monomials can hence be uniquely identified for system  $S^1$  :

$$\frac{N}{c_3}, \quad \frac{N\kappa}{c_3}, \quad \frac{c_0}{c_3}, \quad \frac{c_1}{c_3}, \quad \frac{c_2}{c_3}. \tag{12}$$

Similarly, the following coefficients can be uniquely identified for system  $S'$

$$\frac{N}{c'_3}, \quad \frac{N\kappa'}{c'_3}, \quad \frac{c'_0}{c'_3}, \quad \frac{c'_1}{c'_3}, \quad \frac{c'_2}{c'_3}. \tag{13}$$

290 In view of equations (12) and (13) and the fact that population of people aged 12 and above  $N$   
291 is assumed to be fixed and a *a priori* known parameter, it is readily concluded that  $c_3 = c'_3$ . By  
292 equating  $\frac{N\kappa'}{c'_3} = \frac{N\kappa}{c_3}$ , it is concluded that  $\kappa' = \kappa$ . In a similar manner, we will have  $c_0 = c'_0$ ,  $c_1 =$   
293  $c'_1$ , and  $c_2 = c'_2$ .

<sup>1</sup>Here we assume the following ranking system  $y < \dot{y} < \ddot{y}$  and  $\{u_0, u_1, u_2, u_4\} < u_3$ .

To show  $\alpha_1 = \alpha'_1$ , let us define  $\beta(t) = x_2(t) - \alpha_1 N_n$ . In view of the identifiability of  $c_0, c_1, c_2, c_3$ , and  $\kappa$ , by equating  $\dot{y}(t) = \dot{y}'(t)$ , we obtain the following equation

$$\beta(t) = \beta'(t), \quad \forall t \in (t_1, T). \quad (14)$$

294 We prove  $\alpha_1 = \alpha'_1$  by contradiction. Without loss of generality, let us assume that  $\alpha_1 > \alpha'_1$ .  
 295 Consider the time interval  $[0, t_1)$ , where the demand exceeds the supply. Based on Definition 1,  
 296 the initial condition is specified, i.e.,  $x_2(0) = x'_2(0)$ , and consequently  $\beta(0) < \beta'(0)$ . Let us  
 297 assume that at time  $t'$  we have  $\beta(t') = \beta'(t')$ , i.e.,  $x_2(t') - x'_2(t') = N_n(\alpha_1 - \alpha'_1)$ . In what  
 298 follows we show that  $t' \not\leq t_1$ .

Let us assume that  $t' < t_1$ . Now, consider the following differential equation

$$\dot{\beta}(t) - \dot{\beta}'(t) = -f(t)(\beta(t) - \beta'(t)), \quad (15)$$

where

$$f = \frac{k(u_4 - y)(N_n - y)\frac{y\sigma\Delta\pi}{N}}{\frac{y\sigma\Delta\pi}{N}(N_n - y)(\beta + \beta')(\frac{y\sigma\Delta\pi}{N} - 1) + \beta\beta'(1 + \frac{y^2\sigma^2\Delta\pi^2}{N^2}) - 2\beta\beta'\frac{y\sigma\Delta\pi}{N} + (N_n - y)^2y^2\frac{\sigma^2\Delta\pi^2}{N^2}}. \quad (16)$$

For the time interval  $t \in [0, t_1)$ , we have

$$\begin{aligned} u_4(t) - y(t) &< -\beta(t) + \beta\frac{y(t)\sigma\Delta\pi(t)}{N} + (Nu_4 - y(t))\frac{y(t)\sigma\Delta\pi(t)}{N} \\ &< \alpha_1 N_n + 0 + N_n \\ &\leq 2N_n. \end{aligned} \quad (17)$$

299 In addition, for all  $t$ ,  $(N_n - y(t)) < N_n$  and  $\frac{y(t)\sigma\Delta\pi(t)}{N} < 1$ . On the other hand, for  $t < t_1$  the  
 300 first inequality of (8) holds, i.e.,  $u_4(t) - y(t) < 2N_n$ . Therefore, for  $t < t_1$  the nominator of  
 301  $f(t)$  is upper bounded by  $2kN_n^2$ .

The absolute values of  $\beta(t)$  and  $\beta'(t)$  are decreasing over time, suggesting that for all  $t \in [0, t_1)$  the denominator of  $f(t)$  satisfies

$$\underbrace{\frac{y\sigma\Delta\pi}{N}(N_n - y)(\beta + \beta')(\frac{y\sigma\Delta\pi}{N} - 1)}_{>0} + \underbrace{\beta\beta'(1 + \frac{y^2\sigma\Delta\pi^2}{N^2}) - 2\beta\beta'\frac{y\sigma\Delta\pi}{N}}_{\beta\beta'(1 - \frac{y\sigma\Delta\pi}{N})^2}_{>\beta(t_1)\beta'(t_1)(1 - \frac{y(t_1)\sigma\Delta\pi^{\max}}{N})^2} + \underbrace{(N_n - y)^2y^2\frac{\sigma\Delta\pi^2}{N^2}}_{>0} \quad (18)$$

where  $\Delta\pi^{\max} = \max_{t \leq t_1} \Delta\pi(t)$ . Note that for  $t < t_1$ , the demand was higher than supply (Assumption 3), resulting in  $\beta(t_1) = x_2(t_1) - \alpha_1 N_n < 0$ . In overall, for all  $t \in (0, t_1)$ , we have

$$f(t) \leq \frac{2kN_n^2}{\beta(t_1)\beta'(t_1)(1 - \frac{y(t_1)\sigma\Delta\pi^{\max}}{N})^2}. \quad (19)$$

In view of the fact that for  $t \in (0, t')$ , we have  $\beta(t) - \beta'(t) < 0$ , the following holds:

$$\dot{\beta}(t) - \dot{\beta}'(t) \leq -\frac{2kN_n^2}{\beta(t_1)\beta'(t_1)\left(1 - \frac{y(t_1)\sigma\Delta\pi^{\max}}{N}\right)^2}(\beta(t) - \beta'(t)). \quad (20)$$

Now consider the following differential equation

$$\dot{z}(t) = -\frac{2kN_n^2}{\beta(t_1)\beta'(t_1)\left(1 - \frac{y(t_1)\sigma\Delta\pi^{\max}}{N}\right)^2}z(t), \quad z(0) = \beta(0) - \beta'(0), \quad t \in [0, \infty). \quad (21)$$

302 According to Grownwall's Inequality, we know that for  $t \in [0, t_1)$ ,  $\beta(t) - \beta'(t) < z(t)$ . The  
 303 solution of this system is  $z(t) \leq z(0) \exp\left(-\frac{2kN_n^2}{\beta(t_1)\beta'(t_1)\left(1 - \frac{y(t_1)\sigma\Delta\pi^{\max}}{N}\right)^2}t\right)$  which suggests that for  
 304 all finite time  $z(t) < 0$ . Therefore  $\beta(t) - \beta'(t) < 0$ , for all  $t < t_1$ . This contradicts our  
 305 assumption that  $t' < t_1$ . On the other hand, in view of eq. (14),  $\beta(t) = \beta'(t)$ , for all  $t \in (t_1, T]$ .  
 306 The only possible case where both  $\beta(t) - \beta'(t) < 0$ , for all  $t < t_1$ , and eq. (14) are satisfied is  
 307 that  $\beta(t)$  jumps at  $t = t_1$ . This, however, cannot happen. More specifically, a jump in  $\beta(t)$  is  
 308 attributed to a jump in  $x_2(t)$ . Considering eq. (7), the first order time derivative of  $x_2(t)$ , i.e.,  
 309  $\dot{x}_2(t)$  may experience a jump. However, through integration, this possible jump vanishes, and as  
 310 a result  $x_2(t)$  cannot jump. Therefore, the assumption of  $\alpha'_1 < \alpha_1$  is contradicted. As a result,  
 311 the parameters  $\kappa, \alpha_1, \sigma, C_i, c_{\bar{v}}$ , and  $c_{v_0}$  are uniquely identifiable. This completes the proof.

312 Although it is still possible that the vaccination coverage of two populations with different  
 313  $\alpha_1$ s reaches the target level at the same time (Figs S28-S29), the identifiability of  $\alpha_1$ , under the  
 314 mentioned assumptions, implies that different proportions of decision-makers result in different  
 315 vaccination progresses over time.

## 316 3.2 Fitting Results

317 Our fitting results suggested that 47% ( $\alpha = 0.47$ ) of Americans aged 12 years and above be-  
 318 haved as myopic rationalists in receiving the first dose of COVID-19 vaccine, i.e., about 131  
 319 millions out of 279 million Americans, an equal proportion acted as success-based learners, and  
 320 the remaining 6% were COVID-19 vaccine refusers. The estimated percentage of rationalists  
 321 across the US varied from 31% in Mississippi to 76% in Vermont (Fig. 1). In fifteen states,  
 322 myopic rationalists composed more than 50% of residents.

323 To ensure that the estimations were as robust as possible, we reported the confidence in-  
 324 tervals (CIs) obtained from non-parametric bootstrapping as they resulted in larger CIs than  
 325 parametric bootstrapping (Table S1). The length of 95% CI for the proportion of myopic ra-  
 326 tionalists was 0.13 or less for all jurisdictions (Table S1). For 20 states, the upper limit of the  
 327 CI was lower than the estimated proportion across the US, i.e., 0.47, as well as the estimated  
 328 proportions of 25 other states, implying a significant difference in the proportions.

329 As of November 2021, all eligible American myopic rationalists were vaccinated. Success-  
 330 based learners had lower vaccine coverage. While in all jurisdictions more than half of the

Table 1: Linear correlation between explanatory variables and the estimated proportion of myopic rationalists.

<b>Predictor variable</b>	<b>Pearson-r</b>	<b>R-squared</b>
Vaccination coverage	0.87	0.76
Proportion of votes in favor of Democrats	0.82	0.68
Education score	0.74	0.54
Proportion of people living further than 10 miles from vaccination facilities	-0.37	0.14
Density of vaccination facilities	-0.24	0.06

imitators received at least one dose of a COVID-19 vaccine, in no jurisdiction were they all vaccinated.

The weekly number of vaccinated individuals, particularly rationalists, was greatly influenced by the vaccine doses available during the first months of vaccine roll-out which was due to vaccine supply limitations (Fig. 2A, B, E, F). The success-based learners participation in vaccination was negligible in the beginning compared to that of myopic rationalists (Fig. 2C, G). The changes in the perceived benefit of vaccination in some states were negligible compared to other states (Fig. 2D, H, Figs. S3-S27).

The proportion of myopic rationalists was correlated with the vaccination coverage, proportion of votes in favor of Democrats in the 2020 presidential election, and education score (Table 1—see Table S2 for the other explanatory variables with lower correlations). The proportion of myopic rationalists was not highly correlated with the accessibility to the vaccination facilities (Table 1—last two rows).

We evaluated the impact of each model component on the fitting results. The averaged residual sum of the squares (RSS) over all jurisdictions increased if any of the components were altered. More specifically, by assuming a fully myopically rational population ( $\alpha = 1$ ), the RSS increased by 616%, whereas a population of success-based learners ( $\alpha = 0$ ), resulted in an increase of 626%. To investigate the effect of the possible delay in delivering the vaccine doses compared to what was reported in the data, we introduced a 3-day delay based on California vaccine distribution plan (57). The estimated composition of myopic rationalists and success-based learners at the state level was fairly insensitive to the introduced delay. More specifically, the variations in the estimated proportion of myopic rationalists were less than 10% (see Table S3).

## 4 Discussion

We considered vaccination coverage as a collective outcome resulting from decisions of individuals that are known to be mainly either myopic rationalists or success-based learners. Although crucial to the vaccination dynamics, the proportion of the two types of decision makers has

358 to date been unknown and not measured directly. We tackled this problem by developing a  
359 mechanistic model capturing the evolution of vaccinated population with fixed ratios of the two  
360 types of decision-makers in the context of vaccine uptake. We additionally considered a third  
361 type of vaccine refusers who never intended to be vaccinated. By fitting the model to data on  
362 the number of first-dose COVID-19 vaccinated individuals in the US, we found that, exclud-  
363 ing the 6% vaccine refusers, about half of the Americans behaved as myopic rationalists, and  
364 half as success-based learners. The results may inform health management and guide tailored  
365 communication towards promoting vaccination uptake.

366 The main challenge in this work was how to estimate this unobserved proportion of myopic  
367 rationalists. We took the natural approach of building a mechanistic model with the propor-  
368 tion of decision-makers as a hidden parameter and then estimated it by fitting the equations to  
369 existing data on observed quantities such as vaccine uptake. However, there are two potential  
370 drawbacks with this approach. First, there could be parameter identifiability issues, resulting  
371 in a low estimation confidence. We tackled this issue by proving that the proportion of myopic  
372 rationalists is an identifiable parameter that can be uniquely estimated.

373 The fact that the proportion is identifiable implies that it can be estimated using a sufficiently  
374 rich dataset, which appeared to be the case for our study due to the sufficiently narrow confi-  
375 dence intervals. As the fitting errors did not follow a normal distribution and were temporally  
376 correlated, the confidence intervals could not be obtained based on the common assumption  
377 of independence and normally distribution. We addressed this issue by using non-parametric  
378 bootstrapping methods and applying an auto-regression to reduce the temporal correlation. Es-  
379 timating the parameters using Bayesian methods could be another plausible approach which is  
380 left for future investigation.

381 The second drawback is that even with a unique solution, there may be other possible models  
382 for the observed human behaviour. Alternative explanations of the vaccine uptake trends could  
383 be a population consisting of *(i)* multiple groups of success-based learners with different learn-  
384 ing rates, *(ii)* multiple groups of myopic rationalists with different uptake rates, *(iii)* multiple  
385 groups of both success-based learners learning at different rates and myopic rationalists with  
386 different uptake rates who are interacting, and *(iv)* multiple groups of success-based learners  
387 with different learning rates, myopic rationalists with different uptake rates, and intermediate  
388 learners who are both myopic rationalists and success-based learners to some degree (58). The  
389 first two hypotheses ignore the evidence from other studies of the existence of variations in peo-  
390 ple's reliance on social learning (59, 60). Indeed, the dichotomy of decision-making populations  
391 has been acknowledged in previous vaccination studies (8, 61) as well as other contexts, such  
392 as marketing and psychology (4, 7, 10–12, 62, 63). The last two hypotheses, however, are likely  
393 to be more realistic. Despite this, we have considered the simplest model that includes both  
394 myopic rationalists and success-based learners and the more complex models are left for future  
395 work.

396 The proportion of the two types of decision-makers has not been estimated in previous vac-  
397 cination studies; only homogeneous models have been fitted to data (64, 65). Some marketing  
398 studies estimated the relative proportion of the two types in adopting several products using the

399 Bass model (7, 66, 67). Our work complements these studies in that (i) rather than estimating  
400 the proportion among the final adopters, we estimated the proportion in the whole population,  
401 including unvaccinated individuals, (ii) we considered the influence of time-varying variables  
402 including epidemiological indices, and the perceived risk associated with vaccine side effects,  
403 (iii) we incorporated supply limitation in the model, and (iv) we showed that the proportions of  
404 these decision-makers are identifiable.

405 We found that myopic rationalists greatly determined the evolution of the number of weekly  
406 vaccinated individuals (vaccination speed) during the first months of the vaccine roll-out – a  
407 crucial factor in the success of vaccination programs (68–70). In later months, the vaccina-  
408 tion speed was mainly determined by success-based learners. Considering the excess payoff  
409 formulation, the only factor capable of inducing a negative excess payoff is the perceived risk  
410 associated with side effects. This factor, however, according to a longitudinal survey, declines  
411 over time (23). This suggests that once vaccination has a higher payoff than remaining unvac-  
412 cinated, which was the case during the first months, all myopic rationalists tended to take the  
413 vaccine—the only limiting factor being vaccine availability. Although success-based learners  
414 also tended to take the vaccine once the excess payoff is positive, they based their decisions on  
415 others’ success, determined by the magnitude of the excess payoff and the number of vaccinated  
416 individuals. Hence, they tend to delay vaccination during the first months of the vaccine roll-out  
417 but exhibit a higher vaccination speed when many are vaccinated and available to imitate.

418 Myopic rationalists also greatly determined the vaccination coverage – another key factor in  
419 the success of vaccination programs (71). Our findings suggest that as of November 2021, all  
420 American rationalists have received their first dose of vaccine and consequently, excluding the  
421 vaccine refusers, those who remained unvaccinated were success-based learners.

422 The results suggest the proportion of success-based learners as a factor behind the collective  
423 vaccination behavior and contributing to the success of mass vaccination programs. The begin-  
424 ning of vaccination programs may mainly address access issues to expedite vaccination among  
425 myopic rationalists. Later on, vaccine-promoting interventions should be tailored to success-  
426 based learners to increase their perceived benefit of vaccination. The initiation of this second  
427 phase depends on the composition of the decision-makers, i.e., the more success-based learners  
428 in the population, the sooner the second phase should be initiated.

429 We observed high variations in the estimated proportion of myopic rationalists across the  
430 US jurisdiction, ranging from 0.31 to 0.76. The result is in line with studies highlighting the  
431 variation of different indices throughout the states (72, 73). The delivered doses in the first  
432 months shaped the number of vaccinated rationalists. However, the variation may not be at-  
433 tributed to vaccine supply disparity, because the doses were distributed proportionally to the  
434 state populations (74).

435 There are candidate factors to explain the inter-state differences in the ratio of myopic ra-  
436 tionalists and success-based learners. The proportion of myopic rationalists was positively cor-  
437 related with the vaccination coverage (Pearson-r = 0.87). The proportion of myopic rationalists  
438 was also positively correlated with the proportion of votes in favor of Democrats in 2020 presi-  
439 dential election (Pearson-r = 0.82). These findings are then consistent with the known relation

440 between vaccination coverage and 2020 presidential election outcome (75). The ratio of my-  
441 opic rationalists was also positively associated with education score. In view of the correlation  
442 between the ratio of myopic rationalists and vaccination coverage, this is indirectly corrobo-  
443 rated by studies suggesting American adults with less education being less likely to receive the  
444 vaccine (23, 76).

445 Our model shows how interactions between myopic rationalist and success-based learner  
446 groups have determined the course of the vaccination for COVID-19 in the United States. Ad-  
447 mittedly, true population could have additional heterogeneities, where different age, gender, or  
448 socio-economic status groups have different perception of the payoff (77–79). The extension  
449 of the model to capture this heterogeneity is subject to future work. Another limitation of this  
450 work comes from assuming a well-mixed population rather than the more realistic structured  
451 population as supported by Twitter echo-chambers (80). This assumption may not greatly affect  
452 myopic rationalists as important information about the excess payoff is often obtained from and  
453 shared by all reputable and publicly accessible news agencies. In the same way, online influ-  
454 encers – usually perceived as the most successful – make the interactions of success-based learn-  
455 ers more well-mixed than structured (81). Overall, while acknowledging the aforementioned  
456 limitations, the results of this study provide strong evidence that the COVID-19 vaccine up-  
457 take dynamics were determined by interactions between myopic rationalists and success-based  
458 learners and about half of the Americans relied on the success of others in taking COVID-19  
459 vaccine.

460

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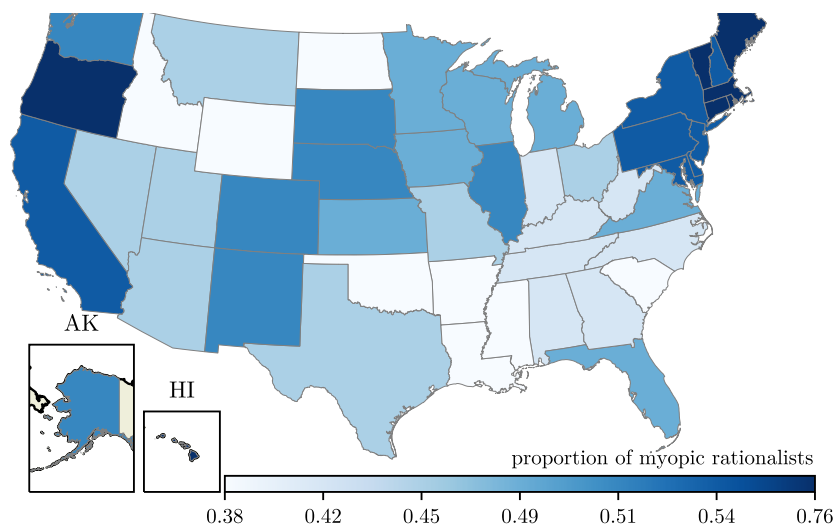


Figure 1: **Estimated proportion of myopic rationalists in taking the first dose of COVID-19 vaccination across the 50 states and the D.C. in the US.** Darker colors show a higher proportion of myopic rationalists. For each jurisdiction, the proportion of myopic rationalists aged 12 years and above was estimated by fitting the developed mechanistic model to the data on weekly newly vaccinated individuals starting from Dec 2020 to Nov 2021. The vaccine supply limitations during the first months of vaccine roll-out were captured by using the data on delivered doses to each jurisdiction over time. The national wide estimated proportion of myopic rationalists was 0.47. There was a high degree of variation across the 51 jurisdictions, i.e., 0.31 for Mississippi to 0.76 for Vermont. About 52% of the residents of the states located in the Northeast region behaved as myopic rationalists in taking COVID-19 vaccination, while in southern states, this proportion was about 43%. The estimated proportion of myopic rationalists in West and Midwest regions was respectively 0.49 and 0.46.

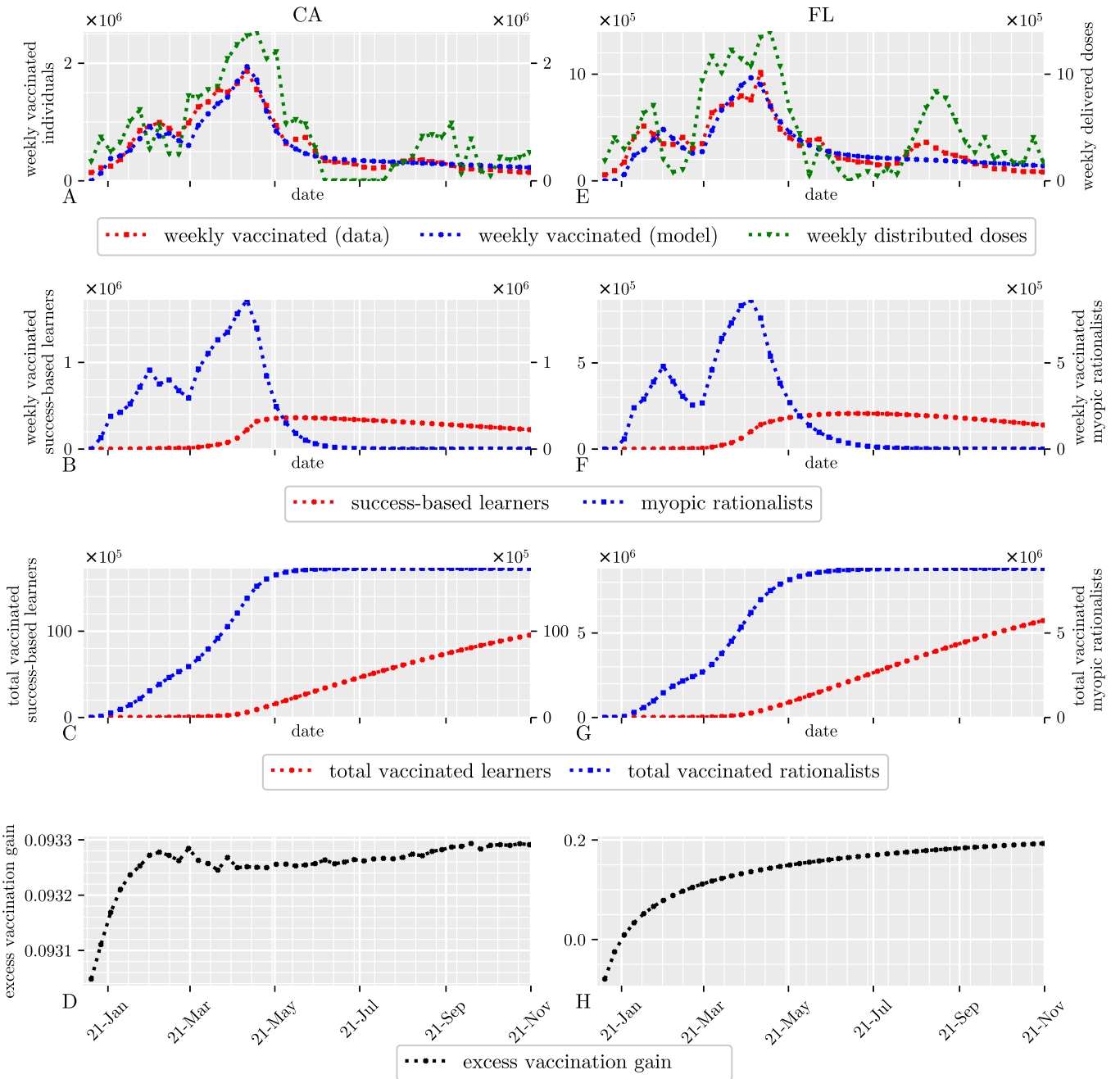


Figure 2: **Number of weekly vaccinated individuals, myopic rationalists, success-based learners, and the excess payoff over time for states of California and Florida, Dec 2020-Nov 2021**). Left panels depict the results and data for California and the right ones are for Florida. Panels A and E depict the weekly number of vaccinated residents in red, its estimation in blue, and weekly number of delivered doses in green. Panels B and F depict the estimated weekly number of vaccinated myopic rationalists and success-based learners in blue and red, respectively. Panels C and G depict the estimated total number of vaccinated myopic rationalists and success-based learners over time in blue and red, respectively. The panels in the last row depict the evolution of the benefit of vaccination (excess payoff). The number of weekly vaccinated individuals is shaped by the vaccine doses available particularly during the first months of vaccine roll-out (Panels A and E). Almost all myopic rationalists receive the vaccine by July, 2021 (the blue curves in Panels C and G). The vaccination progress is many due to myopic rationalists in the first months. As vaccination progresses, success-based learners are persuaded to receive a vaccine (Panels B and F), and then shape the vaccination progress curve (Panel C and G). Over the studied time interval, the perceived benefit of vaccination among Californians changes slightly compared to that of Floridians (Panels D and H).

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