

Performance Analysis of Hybrid Optical Wireless and Radio Frequency  
Communication Systems

by

Tamer Rakia

B.Sc., Military Technical College, 2002

M.Sc., Military Technical College, 2011

A Dissertation Submitted in Partial Fulfillment of the  
Requirements for the Degree of

DOCTOR OF PHILOSOPHY

in the Department of Electrical and Computer Engineering

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## ABSTRACT

In this thesis, we analyze the performance of heterogeneous wireless communication systems that are composed of Optical Wireless Communication (OWC) and Radio Frequency (RF) systems. OWC systems further include long range outdoor Free Space Optical (FSO) systems and short range indoor Visible Light Communication (VLC) systems.

Hybrid FSO/RF systems have emerged as a promising solution for high data rate wireless transmissions. Various transmission schemes including switch-over and soft-switching had been presented for hybrid FSO/RF systems. To overcome the drawbacks of existing schemes, we present a new transmission strategy for hybrid FSO/RF systems exploring an adaptive combining technology. This new strategy shows an improved outage performance. Typically, when the transmitter and the receiver are provided with channel state information, the transmission schemes can be adaptively designed allowing the channel to be used more efficiently. We present two new joint adaptive transmission schemes for hybrid FSO/RF systems. The first

one is joint adaptive modulation and adaptive combining scheme which improves the spectral efficiency of hybrid FSO/RF systems. The other one is joint power adaptation and adaptive combining scheme which improves the throughput and the outage performance of hybrid FSO/RF systems. We accurately evaluate the performance of both schemes. FSO technology can be used effectively in multiuser scenarios to support Point-to-Multi-Point (P2MP) networks. In P2MP networks, FSO links are used for data transmission from a central location to multiple users. In this thesis, we present a new P2MP network based on hybrid FSO/RF transmission system. A common backup RF link is used by the central station for data transmission to any user in case of the failure of its corresponding FSO link. Based on a Markov Chain formulation, we study the performance of the resulting system. P2MP Hybrid FSO/RF network achieves considerable performance improvement over the P2MP FSO-only network.

In VLC, Light Emitting Diode (LED) is used for the purpose of simultaneous illumination and data communication at high data rate. However, the light originating from a LED source is naturally confined to a small area and is susceptible to blockages. Hybrid VLC/RF systems have been emerged as a promising solution to provide enhanced communication coverage. We introduce a new dual-hop VLC/RF system with energy harvesting relay to extend the coverage of indoor wireless system based on VLC. The second-hop RF transmission uses the harvested energy over the first-hop VLC transmission. In this thesis, we propose two different approaches for energy harvesting at the relay terminal. In the first approach, the relay harvests light energy from different artificial light sources and sunlight entering the room. In this approach, we propose a novel statistical model for the harvested electrical power and analyze the probability of data packet loss. In the second approach, the relay harvests energy from the VLC link by extracting the direct current component of the received optical signal. In this approach, we investigate the optimal design of the hybrid VLC/RF system in terms of data rate maximization. In both cases, we present extensive numerical examples to define important design guide lines for VLC/RF systems.

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# List of Abbreviations

AP	Access Point
AWGN	Additive White Gaussian Noise
BER	Bit Error Rate
CSI	Channel State Information
CDF	Cumulative Distribution Function
CM	Coherent Modulation
DC	Direct Current
DD	Direct Detection
FSO	Free Space Optical
HD	Heterodyne Detection
IM	Intensity Modulation
IR	Infra Red
LED	Light Emitting Diode
Li-Fi	Light-Fidelity
LO	Local Oscillator
MMW	Milli-Meter Wavelength
MRC	Maximal Ratio Combining
OWC	Optical Wireless Communication
P2MP	Point-to-Multi-Point
PAT	Pointing, Acquisition and Tracking

PDF	Probability Density Function
PPL	Phase Locked Loop
PSK	Phase Shift Keying
QAM	Quadrature Amplitude Modulation
QoS	Quality of Service
RF	Radio Frequency
TCI	Truncated Channel Inversion
SIM	Subcarrier Intensity Modulation
SNR	Signal-to-Noise Ratio
UV	Ultra Violet
VLC	Visible Light Communication
WISP	Wireless Internet Service Provider

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DEDICATION

*To my parents*

*for their continuous guidance and dedication*

*To my lovely wife*

*for her love and support*

## PREFACE

This thesis is based on the publications listed below.

### Journal Publications

- J1.** T. Rakia, H.-C. Yang, M.-S. Alouini, and F. Gebali, “Outage Analysis of Practical FSO/RF Hybrid System with Adaptive Combining”, *IEEE Communication Letters*, vol. 19, no. 8, pp. 1366–1369, August 2015.
- J2.** T. Rakia, H.-C. Yang, M.-S. Alouini, and F. Gebali, “Power Adaptation Based on Truncated Channel Inversion for Hybrid FSO/RF Transmission with Adaptive Combining”, *IEEE Photonics Journal*, vol. 7, no. 4, pp. 1–12, August 2015.

### Conference Publications

- C1.** T. Rakia, H.-C. Yang, F. Gebali, and M.-S. Alouini, “Joint Adaptive Modulation and Combining for Hybrid FSO/RF Systems”, *15th IEEE International Conference on Ubiquitous Wireless Broadband, ICUWB’2015*, Montreal, Canada, 2015.
- C2.** T. Rakia, H.-C. Yang, F. Gebali, and M.-S. Alouini, “Outage Performance of Hybrid FSO/RF System with Low-Complexity Power Adaptation”, *IEEE Global Communications Conference, Globecom’2015*, San Deigo, USA, 2015.

### Journal Publications (accepted)

- AJ1.** T. Rakia, H.-C. Yang, F. Gebali, and M.-S. Alouini, “Optimal Design of Dual-Hop VLC/RF Communication System with Energy Harvesting”, *IEEE Communication Letters*, accepted for publication.

### Journal Publications (submitted)

- SJ1.** T. Rakia, F. Gebali, H.-C. Yang, and M.-S. Alouini, “Cross Layer Analysis of Point-to-Multi-Point Hybrid FSO/RF Network”, *Journal of Optical Communications and Networking*, submitted for publication.

### Conference Publications (submitted)

**SC1. T. Rakia**, H.-C. Yang, F. Gebali, and M.-S. Alouini, “Dual-Hop VLC/RF Transmission System with Energy Harvesting Relay under Delay Constraint”, *IEEE Global Communications Conference (Globecom’2016) Workshops*, submitted for publication.

# Chapter 1

## Introduction

### 1.1 Background

Optical Wireless Communication (OWC) refers to data transmission in unguided propagation media through the use of an optical carrier. OWC are categorized into three main types, which are Free-Space Optical (FSO) communications, Visible Light Communications (VLC), and Ultra-Violet (UV) Communications. FSO communications and UV Communications use the Infra-Red (IR) band (750 nm - 1600 nm) and the UV band (200 nm - 280 nm), respectively, to allow for outdoor long and short ranges data transmission [1, 2]. On the other hand, VLC - also known as Li-Fi for Light-Fidelity - uses the visible light band (380 nm - 780 nm) to allow for indoor short range data transmission [3].

### 1.2 Literature Review and Motivation

#### 1.2.1 Free-Space Optical Communications

FSO technology has gained an increasing interest in implementing point-to-point data transmission links, owing to its high data rate, high transmission security, large unregulated spectrum, compared to Radio Frequency (RF) technology, and fast and cheap deployment, compared to fiber optics [4]. Point-to-point FSO links had found their way in many terrestrial and satellite applications. FSO links can be used to connect one Local Area Network (LAN) to another LAN and connect them to Backbone networks, typically implemented with optical fibers as shown in Fig. 1.1 [5], where the black arrows are FSO links. FSO links can be used also as a robust outdoor backhaul

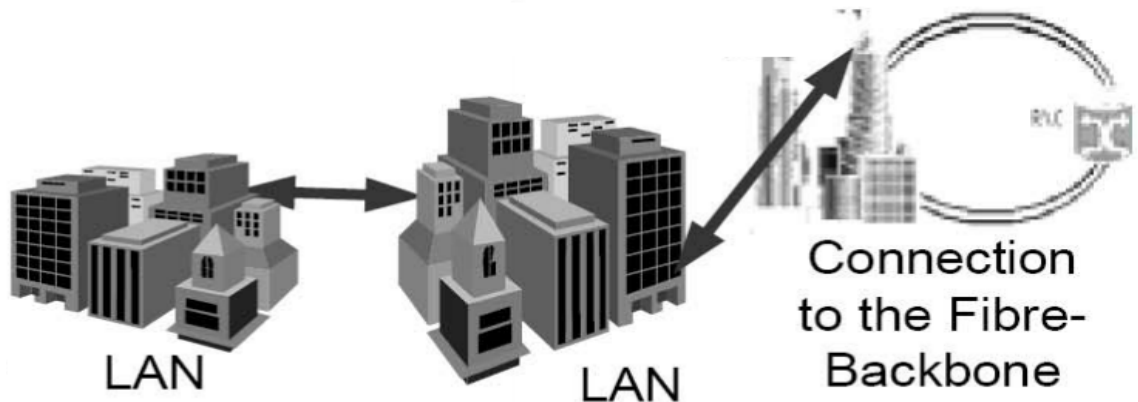


Figure 1.1: LAN-to-LAN FSO connectivity © 2005 IEEE

solution for small radio cells, such as WiFi, LTE and 5G as shown in Fig. 1.2 [6], where the red arrows are FSO links. Other terrestrial applications of FSO include

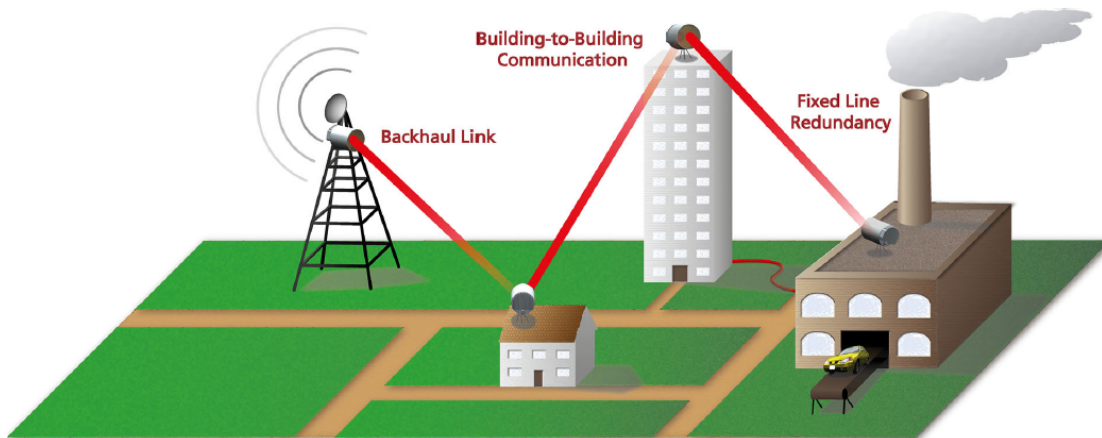


Figure 1.2: Point-to-point backhaul FSO link © 2016 IEEE

last-mile applications to connect end users to a broadband network backbone [7], recovery links for a network which is partially disconnected due to natural disasters [8] and wireless video surveillance and monitoring [9]. Satellite applications of FSO include inter-satellite communications [10] and data transmission between the satellite and the ground stations [11]. We focus on terrestrial applications in this thesis.

An FSO transmission system consists of an optical transmitter and an optical receiver which uses the atmosphere as the transmission media for the optical signal (specifically, a laser beam) as shown in Fig. 1.3. FSO systems are categorized according to the type of detection into Intensity Modulation/Direct Detection (IM/DD)

FSO systems [12] and Coherent Modulation/Heterodyne Detection (CM/HD) FSO systems [13].

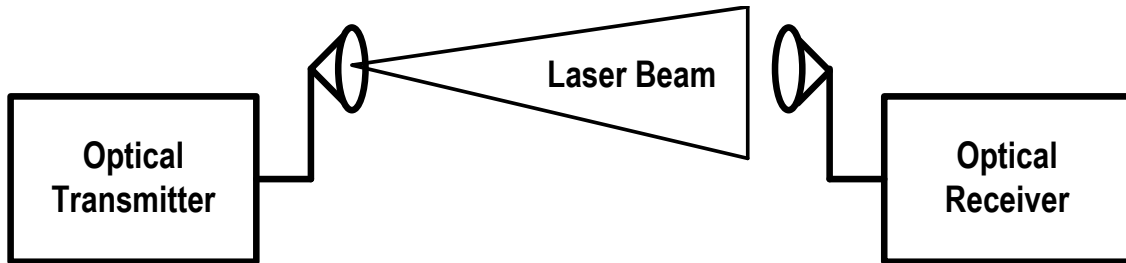


Figure 1.3: FSO system block diagram

The optical signal transmitting through the atmosphere is greatly affected by fading due to atmospheric turbulences and pointing errors [14–18] as shown in Fig. 1.4 [19]. Turbulence-induced fading, known as scintillation, causes irradiance fluctuations in the received optical signal as a result of variations in the atmospheric refractive index [20]. Dynamic wind loads and weak earthquakes can cause vibrations of the transmitted optical beam, which also causes random irradiance fluctuations in the received optical signal. Moreover, the optical power is attenuated as the distance between the transmitter and the receiver increases due to a constant atmospheric loss [17].

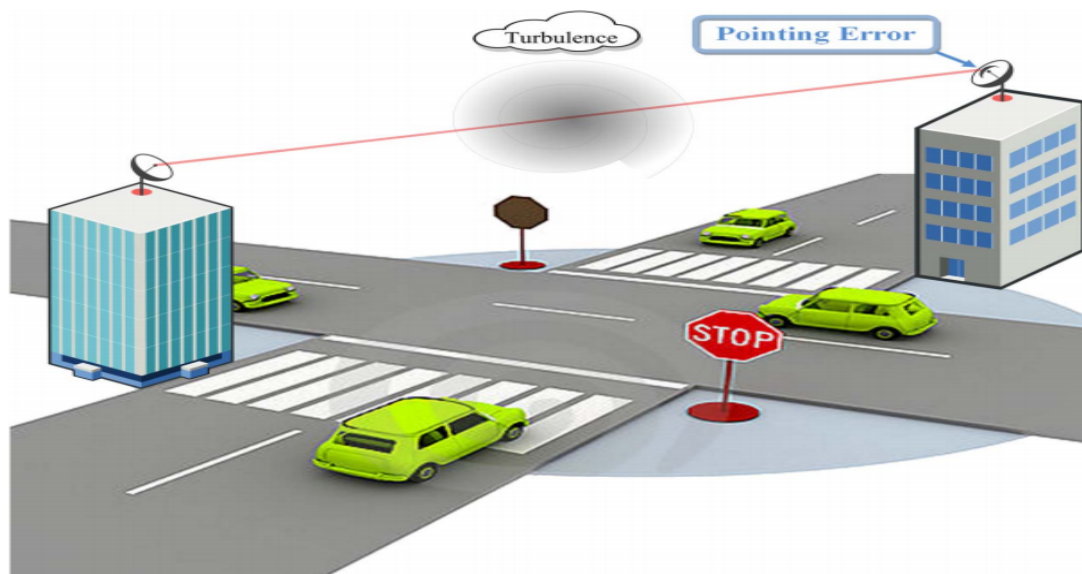


Figure 1.4: Atmospheric turbulence and pointing error in FSO system © 2014 IEEE

## Hybrid FSO/RF Implementation

Integrating the FSO link with a Milli-Meter wavelength (MMW) RF link, to form what is known as hybrid FSO/RF system, improves the performance of FSO links. This is owed to the fact that FSO and RF links are affected quite differently by atmospheric and weather effects. FSO links suffer from extremely high attenuation in the presence of fog but are less affected by rain. In contrast, fog has practically no effect on MMW RF links but rain significantly increases link attenuation. Similarly, while atmospheric turbulence is the main cause of small-scale fading in FSO links [20], RF links are impaired by fading due to multipath propagation [21]. Besides the high data rates comparable to FSO links, MMW RF links offer other similar advantages to FSO links of deployment flexibility, license free operation, and inherent security due to high link attenuation.

This complementary nature of FSO and MMW RF links has led to various approaches in implementing hybrid FSO/RF data transmission systems. Two main approaches had been presented in implementing hybrid FSO/RF systems. One approach is the switch-over hybrid FSO/RF scheme, which applies hardware switching between FSO and MMW RF links [22]. However, this approach will lead to frequent hardware switching between the FSO and RF links [23]. Another approach is to use both FSO and RF links for data transmission all the time. One way in this approach, is to transmit identical data simultaneously on both links and apply diversity combining techniques to received signals from both links [24, 25]. In this way, the system's data rate is limited to the lower rate of RF link. Another way, is to divide the coded data stream between the two links, which may have a significant improvement on total system capacity [26]. In general, this soft-switching approach requires FSO and RF links to be active continuously, even when FSO link has very good quality and can support the required bit-error rate by itself. In this scenario, RF transmission power is wasted and system generates unnecessary RF interference to the environment.

These drawbacks of previously presented hybrid FSO/RF systems had motivated us to develop a new scheme for hybrid FSO/RF transmission. This scheme is called hybrid FSO/RF transmission with adaptive combining [27]. In this scheme, FSO link is used alone for data transmission as long as its quality is acceptable and the RF link is put on standby mode. When FSO link's quality becomes unacceptable, the system activates the RF link and applies Maximal Ratio Combining (MRC) scheme on signals received from both FSO and RF links. When the quality of the FSO link

alone becomes acceptable again, the RF link is put on standby mode again to save power and spectrum utilization. Thus, the proposed adaptive combining scheme for hybrid FSO/RF systems: 1) improves communication system's reliability, without suffering from switch-over schemes problems, 2) prevents generation of unnecessary RF interference to the environment, 3) conserves RF power, and 4) benefits from FSO higher data rate most of the time.

### **Adaptive Transmission**

Since both FSO and MMW RF channels typically experience slow-fading [17, 28], the transmitter and the receiver of the hybrid FSO/RF system can adapt to the Channel State Information (CSI), allowing the channel to be used more efficiently over time varying channel conditions. Previously, hybrid FSO/RF systems with link adaptation were introduced in [29] and [30]. In [29], transmitted data frame is divided between the FSO and RF links, where both links are simultaneously active. In this case different symbol rates and modulation schemes are used adaptively in a jointly manner according to each link condition. Although, this link adaptation scheme provides good throughput, transmitting different data on both links does not allow the RF link to support the FSO link when its quality is poor. Moreover, using different symbol rates and modulation schemes for both links add extra hardware complexity to both transmitter and receiver terminals. In [30], switch-over hybrid FSO/RF system with adaptive modulation transmission scheme is introduced, where different sets of modulation schemes are used over FSO and RF links. In this scheme, the data rate of the FSO link is gradually reduced, and only switches to RF link in the worst scenario. When the hybrid system uses the RF link alone, transmission rate is also varied according to the RF channel states. Once more, using different modulation schemes sets with both links adds extra hardware complexity to both transmitter and receiver.

Motivated by the previous work in this field and aiming to solve some of drawbacks of the previous presented systems, we present a new joint adaptive modulation and adaptive combining scheme for hybrid FSO/RF system [31]. In this adaptive transmission scheme, the data rate on the FSO link is adjusted in discrete manner according to the FSO link's instantaneous received Signal-to-Noise Ratio (SNR), aiming to achieve the maximum spectral efficiency. If the FSO link's quality is too poor to be able to support the minimum SNR required to satisfy the target Bit-Error-Rate

(BER), the system activates the RF link along with the FSO link. When the RF link is activated, simultaneous transmission of the same modulated data takes place on both links, where the received signals from both links are combined using an MRC scheme. In this case, the data rate of the system is determined in discrete manner according to the instantaneous combined SNRs of both links to maintain the target BER value, while aiming to maximize the system spectral efficiency. When the quality of the FSO link alone becomes acceptable again, the RF link is put on standby mode. Thus, the proposed joint adaptation strategy: 1) provides a low complexity hybrid FSO/RF system with discrete-rate adaptation using the same digital modulation scheme on both links, 2) does not suffer from problems of hardware-switching between the two links [23] that exist in the switch-over scheme [30], and 3) conserves RF power and prevents generation of unnecessary RF interference to the environment by activating the RF link only when is necessary.

### **Power Adaptation**

Power adaptation offers a simple but effective solution to improve link reliability and data throughput, while conserving transmission power [32]. To further improve our hybrid FSO/RF system with adaptive combining, we present a joint power adaptation and adaptive combining scheme for hybrid FSO/RF systems [33, 34]. Previous work on hybrid FSO/RF systems with power adaptation includes [35] and [36]. Particular, [35] considers a hybrid FSO/RF system, in which the system switches to the reliable RF link if the FSO link is obscured to maintain communication, and apply water-filling power adaptation scheme only on the FSO link. In [36], power adaptation has been applied on both FSO and RF links of the hybrid FSO/RF system, assuming that both links are active all the time but transmitting with different rates. The proposed joint adaptive scheme is similar to the adaptive combining scheme [27]. However, when the RF link is activated, the transmit power over the RF link is adapted according to a modified Truncated Channel Inversion (TCI) power adaptation policy, such that the MRC combination of the RF and FSO links maintains a constant received SNR. The proposed joint adaptive combining and power adaptation scheme: 1) improves communication system's reliability by maintaining constant received SNR, while enhancing its outage performance, 2) benefits from FSO higher data rate most of the time, 3) prevents generation of unnecessary RF interference to the environment, 4) conserves RF power, and 5) increases the system outage capacity.

## Point-to-Multi-Point Transmission

The interesting and unique features of the FSO systems had motivated a wide range of interest. But most of the current literature is limited to point-to-point data transmissions with FSO technology. On the other hand, FSO can be used effectively in multiuser scenarios [37, 38] to support Point-to-Multi-Point (P2MP) topologies. P2MP topology is a common network architecture for outdoor wireless networks to connect multiple locations to one single central location. In these P2MP networks, FSO links are used for data transmission from a central location to multiple users as in Wireless Internet Service Provider (WISP) networks or the WiMAX networks [39]. In a WISP network, subscribers are connected at the edge of the network using a client device typically mounted on the roof of their houses. The central base station is mounted on a high building where it has line of sight with the client devices.

Motivated by the scarcity in the literature in this field, we present P2MP hybrid FSO/RF network as a new approach in multiuser scenarios. The proposed P2MP hybrid FSO/RF data transmission network consists of a number of remote nodes along with a central node. Each remote node in the network is connected to the central node via a separate primary FSO link. A common backup RF link is shared among all the remote nodes. Using a common RF channel will have the major advantages of: 1) sharing the scarce RF spectrum, 2) preventing the generation of unnecessary RF interference to the environment, and 3) conserving the RF transmission power.

### 1.2.2 Visible Light Communications

VLC had attracted a lot of attention as an extension for the wireless optical technology in indoor applications [40–43]. In VLC system, the optical signal from a Light Emitting Diode (LED) is used for the purpose of simultaneous illumination and data communication at high data rates [44]. However, the light originating from a LED source is naturally confined to a small area and is susceptible to blockages. Thus, data link may be unreliable when the receiving terminal goes far from the LED. As a solution for this problem, hybrid VLC/RF systems emerged in order to provide enhanced communication coverage [45, 46]. In [45], a number of VLC and RF Access Points (AP) are used to improve the coverage and the overall rate performance of the hybrid VLC/RF system. However, each single user may detect the optical intensity from multiple VLC APs which leads to inter-user interferences. These interferences may severely degrade the system performance [47, 48]. In [46], VLC is integrated with

an RF-based wireless networks to improve the achievable data rates of mobile users.

To extend the coverage of indoor wireless system based on VLC, we introduce a new approach in hybrid VLC/RF systems, which is a dual-hop VLC/RF system as shown in Fig. 1.5. In this approach, a second-hop RF channel is used to extend the coverage of the VLC system. This proposed hybrid VLC/RF system provides coverage within the entire space of the room with only one VLC system and one relay equipped with an RF system, instead of using many VLC and RF systems as introduced in [45]. The proposed system can be used in high data rate Internet access in indoor environment.

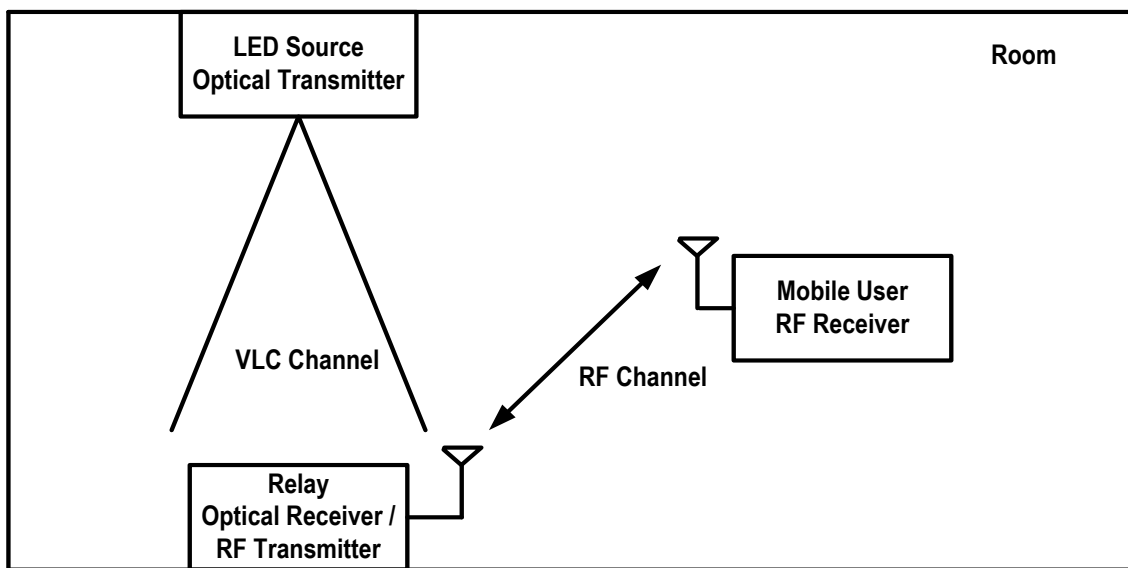


Figure 1.5: Dual-hop VLC/RF system

Recently, harvesting energy from light sources has been introduced in [49], where a solar-panel is used as a passive photo-detector for both information detection and energy harvesting. In order to reduce power consumption, the relay in our proposed dual-hop VLC/RF system is capable of harvesting optical energy and converts it into electrical energy [50,51]. The relay uses the harvested energy to retransmit the data received over the first-hop VLC link to a mobile terminal over the second-hop RF link.

### 1.3 Thesis Organization

This thesis consists of eight chapters. A summary of each remaining chapter and its contributions are presented as follows:

Chapter 2 presents and analyzes a new transmission scheme for the hybrid FSO/RF communication system based on adaptive combining. Specifically, only FSO link is active as long as the instantaneous SNR at the FSO receiver is above a certain threshold level. When it falls below this threshold level, the RF link is activated along with the FSO link and the signals from the two links are combined at the receiver using a dual-branch MRC scheme. Novel analytical expression for the Cumulative Distribution Function (CDF) of the received SNR for the proposed hybrid system is obtained. This CDF expression is used to study the system outage performance. This chapter has been included in a published journal article [J1].

In Chapter 3, we present and analyze a new transmission scheme for hybrid FSO/RF communication system based on joint adaptive modulation and adaptive combining. Specifically, the data rate on the FSO link is adjusted in discrete manner according to the FSO link's instantaneous received SNR. If the FSO link's quality is too poor to maintain the target BER, the system activates the RF link along with the FSO link. When the RF link is activated, simultaneous transmission of the same modulated data takes place on both links, where the received signals from both links are combined using MRC scheme. In this case, the data rate of the system is adjusted according to the instantaneous combined SNRs. Novel analytical expression for the CDF of the received SNR for the proposed adaptive hybrid system is obtained. This CDF expression is used to study the spectral and outage performances of the proposed adaptive hybrid FSO/RF system. This chapter has been included in a published conference article [C1].

In chapter 4, we present power adaptation strategies based on TCI for hybrid FSO/RF system employing adaptive combining. Specifically, we adaptively set the RF link transmission power when FSO link quality is unacceptable to ensure constant combined SNR at receiver. Two adaptation strategies are proposed. One strategy depends on the received RF SNR, while the other one depends on the combined SNR of both links. Analytical expressions for the outage probability of the hybrid system with and without power adaptation are obtained. This chapter has been included in a published journal article [J2] and published conference article [C2].

In chapter 5, we present and analyze a P2MP network that uses a number of FSO

links for data transmission from the central node to the different remote nodes of the network. A common backup RF link can be used by the central node for data transmission to any remote node in case of the failure of any one of the FSO links. Each remote node is assigned a transmit buffer at the central node. Considering the transmission link from the central node to a tagged remote node, we study various performance metrics. Specifically, we study the throughput from central node to the tagged node, the average transmit buffer size, the symbol queuing delay in the transmit buffer, the efficiency of the queuing system, the symbol loss probability, and the RF link utilization. We compare the performance of the proposed P2MP hybrid FSO/RF network with that of a P2MP FSO-only network. This chapter has been included in a submitted journal article [SJ1].

In chapter 6, we introduce a dual-hop VLC/RF transmission system to extend the coverage of indoor VLC systems. The relay between the two hops is able to harvest light energy from different artificial light sources and sunlight entering the room. The relay receives data packet over a VLC channel and uses the harvested energy to retransmit it to a mobile terminal over an RF channel. We propose a novel statistical model for the harvested electrical power and analyze the probability of data packet loss. This chapter has been included in a submitted conference article [SC1].

In chapter 7, we consider the same dual-hop heterogeneous VLC/RF communication system with energy harvesting relay that was introduced in chapter 6. However, we propose in this chapter a different technique for energy harvesting at the relay terminal. The relay is able to extract the Direct Current (DC) component of the received optical signal over the VLC link and uses it to retransmit the data to a mobile terminal over the second-hop RF link. We investigate the optimal design of the hybrid system in terms of data rate maximization. This chapter has been included in a revised journal article [AJ1].

Finally, we summarize the thesis in Chapter 8 and suggest some further research topics related to this thesis.

## 1.4 Research Methodology

There are in general two approaches to evaluate the performance of hybrid OWC/RF systems with different proposed transmission schemes under the effects of fading and path losses in OWC and RF links. One approach is to conduct experiments, which are typically costly and time consuming. On the other hand, analytical system perfor-

mance evaluation can be good alternative to experiments, and the obtained numerical results can be used efficiently at the beginning stage of system design. In this thesis, we will focus on efficient analytical performance evaluation of the proposed hybrid OWC/RF systems, which will provide important engineering insights into hybrid OWC/RF systems design.

## 1.5 Thesis Contributions

### 1.5.1 Contributions in FSO Communications Field

- Contributions of chapter 2:
  - Novel transmission scheme for hybrid FSO/RF communications system based on adaptive combining scheme is proposed.
  - Novel analytical expression for the cumulative distribution function of the received SNR for the proposed hybrid system is obtained.
  - The outage performance of the proposed hybrid FSO/RF system with adaptive combining is studied .
  - The proposed hybrid FSO/RF system with adaptive combining had shown superior outage performance, compared to other FSO systems.
- Contributions of chapter 3:
  - Novel transmission scheme for hybrid FSO/RF communication system based on joint adaptive modulation and adaptive combining is proposed.
  - Novel analytical expression for the CDF of the received SNR for the proposed joint adaptive hybrid system is obtained.
  - Spectral and outage performances of the proposed system are studied.
  - The proposed joint adaptive hybrid FSO/RF system had shown superior spectral and outage performances, compared to other hybrid FSO/RF systems.
- Contributions of chapter 4:
  - Novel transmission scheme for hybrid FSO/RF communication system based on joint power adaptation and adaptive combining is proposed.

- Practical power adaptation strategies are proposed.
  - The corresponding analytical expressions for the outage probability of the proposed joint adaptive hybrid system are obtained.
  - The proposed joint adaptive hybrid FSO/RF system had shown superior outage performances, compared to other hybrid FSO/RF systems.
- Contributions of chapter 5:
    - Novel P2MP hybrid FSO/RF network is proposed.
    - Cross layer Markov chain model of the proposed network is developed.
    - The main parameters affecting the performance of the proposed P2MP hybrid FSO/RF network are identified.
    - Several performance metrics are studied.

### 1.5.2 Contributions in VLC Field

- Contributions of chapter 6:
  - Novel hybrid VLC/RF transmission system setup with a light energy harvesting relay is presented.
  - Novel statistical model for the electrical power harvested from indoor light energy is presented.
  - Packet loss probability under hard delay constraint for overall system is analyzed.
  - Optimal design of energy harvesting and packet transmission duration for the second hop is done.
- Contributions of chapter 7:
  - Novel dual-hop VLC/RF transmission system setup with a relay harvesting the bias component from the received optical signal over the first hop VLC transmission is proposed.
  - Two novel strategies for optimal bias design of the proposed system are introduced.
  - The corresponding end-to-end average data rate of the system is analyzed in every case of the two strategies.

## Chapter 2

# Practical FSO/RF Hybrid System with Adaptive Combining

In this chapter, we present a new scheme for hybrid FSO/RF transmission systems. We name this scheme hybrid FSO/RF transmission system with adaptive combining. In this scheme, FSO link is used alone as long as its quality is acceptable. When FSO link's quality becomes unacceptable, the system activates the RF link, and applies MRC scheme on signals received from both FSO and RF links. When the quality of the FSO link alone becomes acceptable again, the RF link is deactivated to save power and spectrum utilization. We derive the CDF of the receiver SNR, which is then used to study the outage performance of the proposed hybrid adaptive scheme.

The remainder of the chapter is organized as follows. In section 2.1, we introduce the model of the hybrid FSO/RF transmission system with adaptive combining scheme. In section 2.2, we deduce the CDF of the receiver SNR and study the outage performance of the proposed adaptive combining scheme. Finally, section 2.3 presents some numerical examples to investigate the performance of the proposed scheme, followed by the chapter summary in section 2.4.

### 2.1 Hybrid FSO/RF System with Adaptive Combining Modeling

We consider a hybrid FSO/RF system as shown in Fig. 2.1, where only the FSO link is active as long as its instantaneous SNR at the optical receiver, denoted by  $\gamma_{FSO}$ , is above a certain threshold, defined by  $\gamma_T$ . When  $\gamma_{FSO}$  falls below the predetermined

threshold  $\gamma_T$ , the receiver sends a 1-bit feedback signal to activate the RF link along with the FSO link for simultaneous transmission of the same data. In this case, the data received from both links are combined using an MRC scheme. The receiver SNR, denoted by  $\gamma_c$ , will equal to  $\gamma_{FSO}$  when  $\gamma_{FSO} \geq \gamma_T$ . On the other hand, when  $\gamma_{FSO} < \gamma_T$ ,  $\gamma_c$  will equal to the sum of  $\gamma_{FSO}$  and  $\gamma_{RF}$ , where  $\gamma_{RF}$  is the receiver instantaneous SNR of the RF link. Thus, this proposed hybrid system with adaptive combining has two modes of operation which are:

- FSO only mode, as long as  $\gamma_{FSO} \geq \gamma_T$ .
- Combined FSO/RF mode, as long as  $\gamma_{FSO} < \gamma_T$ .

At the transmitter, the data is modulated using a Phase Shift Keying (PSK) digital modulation scheme, where the PSK modulated signal can be expressed as:

$$x(t) = \sum_k g(t - kT) \cos(2\pi f_s t + \phi_k) \quad (2.1)$$

where  $T$  denotes the symbol period,  $f_s$  is the frequency of the PSK subcarrier which must satisfy  $f_s = q/T$  with  $q \geq 1$ ,  $g(t)$  is the shaping pulse, and  $\phi_k \in [0, \dots, (M-1)\frac{2\pi}{M}]$  is the phase of the  $k$ th transmitted symbol with  $M$  is the modulation order, which depends upon the bit transmission rate  $R_b$  according to  $R_b = \log_2(M)/T$ . This PSK modulated signal is available for transmission through both FSO and RF links.

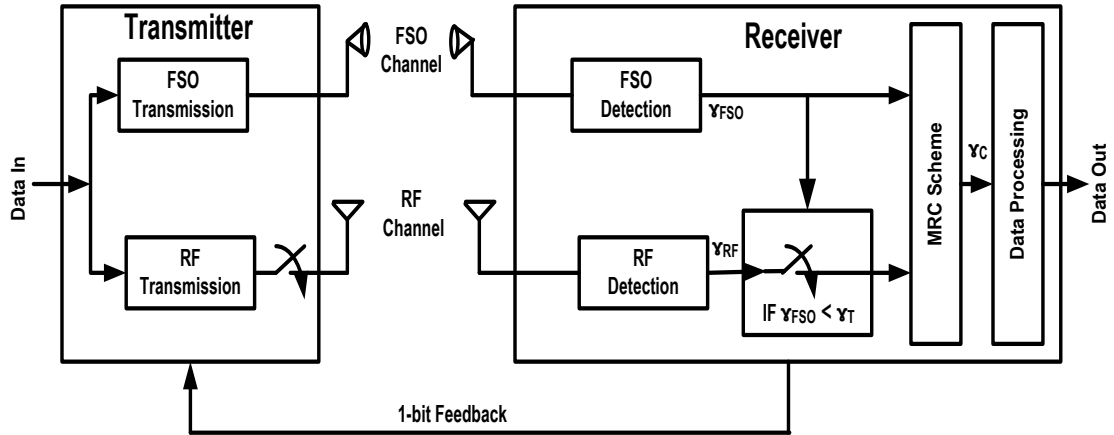


Figure 2.1: Hybrid FSO/RF system with adaptive combining

### 2.1.1 Modeling the FSO Link

We adopt for the FSO link Sub-carrier Intensity Modulation/Direct Detection (SIM/DD) system [52]. In such system, a DC bias is added to the PSK modulated signal to satisfy non-negativity input constraint of IM/DD systems, before it is used to modulate the intensity of the optical signal, specifically, a laser beam. Hence, the intensity of the transmitted optical signal can be written as [24]:

$$I(t) = P_{FSO}[1 + \mu x(t)], \quad (2.2)$$

where  $P_{FSO}$  is the transmitted optical power and  $\mu$  is the modulation index ( $0 < \mu < 1$ ) that ensured that the laser avoids over-modulation induced clipping.

At the FSO receiver, direct detection of the optical signal takes place, and then further demodulation of the sub-carrier follows to retrieve the data. After filtering the DC bias, the received discrete-time equivalent electrical signal can be modeled as [24]:

$$r_{FSO}[k] = \mu\eta P_{FSO}h_{FSO}G_{FSO}\sqrt{E_s}x[k] + n_{FSO}[k] \quad (2.3)$$

where  $\eta$  is the optical-to-electrical efficiency,  $x[k] = \cos \phi_k + j \sin \phi_k$ ,  $E_s = E_g/2$  is the average symbol energy with  $E_g$  is the energy of the shaping pulse and  $n_{FSO}[k]$  is the shot-noise which is modeled as additive white Gaussian noise (AWGN) with variance  $\sigma_{FSO}^2$ .  $h_{FSO}$  is the turbulence induced fading gain over the FSO link, with  $E[h_{FSO}]$  normalized to unity, where  $E[.]$  is the expectation operator.  $G_{FSO}$  is the optical power attenuation, given by Beers-Lambert law as  $G_{FSO} = \alpha_{FSO}z$  [26], with  $\alpha_{FSO}$  being the weather-dependent attenuation coefficient (in dB/Km) and  $z$  is the link range from the transmitter to the receiver. The attenuation  $G_{FSO}$  is considered as a fixed scaling factor, and no randomness exists in its behavior [17].

Assuming perfect alignment between FSO transmitter and receiver apertures<sup>1</sup>, and considering Gamma-Gamma turbulence-induced fading,  $h_{FSO}$  will have the following Probability Density Function (PDF) [20]:

$$f_{h_{FSO}}(h_{FSO}) = \frac{2(\alpha\beta)^{\frac{\alpha+\beta}{2}}}{\Gamma(\alpha)\Gamma(\beta)} h_{FSO}^{\frac{\alpha+\beta}{2}-1} K_{\alpha-\beta}(2\sqrt{\alpha\beta h_{FSO}}) \quad , h_{FSO} \geq 0. \quad (2.4)$$

---

<sup>1</sup>Perfect alignment between FSO transmitter and receiver apertures can be achieved by using Pointing, Acquisition and Tracking (PAT) systems. However, these PAT systems add extra hardware complexity to FSO systems.

where  $\alpha$  and  $\beta$  are parameters related to the atmospheric turbulences and  $K_\nu(\cdot)$  is the  $\nu$ th order modified Bessel function of the second kind defined as [53, Eq. (8.407)]. Typically,  $\alpha$  and  $\beta$  are the effective number of small-scale and large-scale eddies of the turbulent environment, respectively. According to the values of  $\alpha$  and  $\beta$ , the atmospheric turbulence can be modeled from weak to strong turbulence regimes because these parameters are directly related to the atmospheric turbulence conditions. Expressions for calculating the parameters  $\alpha$  and  $\beta$  for different propagation conditions can be found in [54]. Assuming spherical wave propagation, expressions for calculating  $\alpha$  and  $\beta$  in (2.4) are given by [54]:

$$\alpha = \left[ \exp \left( \frac{0.49\chi^2}{(1 + 0.18d^2 + 0.56\chi^{\frac{12}{5}})^{\frac{7}{6}}} \right) - 1 \right]^{-1} \quad (2.5)$$

$$\beta = \left[ \exp \left( \frac{0.51\chi^2(1 + 0.69\chi^{\frac{12}{5}})^{-\frac{5}{6}}}{(1 + 0.9d^2 + 0.62d^2\chi^{\frac{12}{5}})^{\frac{5}{6}}} \right) - 1 \right]^{-1} \quad (2.6)$$

where  $\chi^2 = 0.5C_n^2 k^{7/6} L^{11/6}$  is the Rytov variance and  $d = (kD^2/4L)^{1/2}$  with  $k = 2\pi/\lambda_{FSO}$  is the optical wave number. Here,  $C_n^2$ ,  $D$ , and  $\lambda_{FSO}$  are respectively the refractive index structure parameter, the diameter of the optical receiver aperture and the optical wavelength.

The instantaneous received electrical SNR of the FSO link is related to  $h_{FSO}$  as  $\gamma_{FSO} = \bar{\gamma}_{FSO} h_{FSO}^2$  [24], where  $\bar{\gamma}_{FSO}$  is the average electrical SNR which is defined as  $\bar{\gamma}_{FSO} = E_s \mu^2 \eta^2 P_{FSO}^2 G_{FSO}^2 / \sigma_{FSO}^2$  [24]. Using power transformation of random variables, it is easy to show that the PDF of  $\gamma_{FSO}$  is given by:

$$f_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{(\alpha\beta/\sqrt{\bar{\gamma}_{FSO}})^{\frac{\alpha+\beta}{2}}}{\Gamma(\alpha)\Gamma(\beta)} \gamma_{FSO}^{\frac{\alpha+\beta}{4}-1} K_{\alpha-\beta} \left( 2\sqrt{\frac{\alpha\beta}{\sqrt{\bar{\gamma}_{FSO}}}\gamma_{FSO}^{\frac{1}{2}}} \right), \gamma_{FSO} \geq 0. \quad (2.7)$$

By using [55, Eqs. (14)] to express  $K_{\alpha-\beta}(\cdot)$  in terms of Meijer G-function  $G_{p,q}^{m,n} \left( z \left| \begin{array}{c} a_1, \dots, a_p \\ b_1, \dots, b_q \end{array} \right. \right)$  defined as [53, Eq. (9.301)], and [53, Eq. (9.31.5)], (2.7) can be expressed as:

$$f_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{\gamma_{FSO}^{-1}}{2\Gamma(\alpha)\Gamma(\beta)} G_{0,2}^{2,0} \left( \frac{\alpha\beta}{\sqrt{\bar{\gamma}_{FSO}}}\gamma_{FSO}^{\frac{1}{2}} \left| \begin{array}{c} - \\ \alpha, \beta \end{array} \right. \right). \quad (2.8)$$

By using [56, Eq. (07.34.21.0084.01)], and some simple algebraic manipulations, the

CDF of  $\gamma_{FSO}$  can be expressed as:

$$F_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{2^{\alpha+\beta-2}}{\pi\Gamma(\alpha)\Gamma(\beta)} G_{1,5}^{4,1} \left( \frac{(\alpha\beta)^2}{16\bar{\gamma}_{FSO}} \gamma_{FSO} \left| \frac{1}{\frac{\alpha}{2}, \frac{\alpha+1}{2}, \frac{\beta}{2}, \frac{\beta+1}{2}, 0} \right. \right). \quad (2.9)$$

### 2.1.2 Modeling the RF Link

The electrical PSK-modulated signal, is up-converted to MMW RF (typically, 60 GHz) carrier frequency, to be transmitted over the RF link. The received discrete-time signal, after demodulation process, can be modeled as [24]:

$$r_{RF}[k] = \sqrt{G_{RF}P_{RF}}h_{RF}\sqrt{E_s}x[k] + n_{RF}[k], \quad (2.10)$$

where  $G_{RF}$  is the average power gain of the RF link,  $P_{RF}$  is the RF transmit power, and  $h_{RF}$  is the fading gain over the RF channel, with  $E[h_{RF}^2]$  normalized to unity.  $n_{RF}[k]$  is the zero-mean circularly symmetric AWGN component with variance  $\sigma_{RF}^2$ . The average power gain  $G_{RF}$  is defined as [24]:

$$G_{RF}[dB] = G_T + G_R - 20\log_{10} \left( \frac{4\pi z}{\lambda_{RF}} \right) - \alpha_{oxy}z - \alpha_{rain}z, \quad (2.11)$$

where  $G_T$  and  $G_R$  denote the transmit and receive antenna gains, respectively and  $\lambda_{RF}$  is the wavelength of the RF subsystem.  $\alpha_{oxy}$  and  $\alpha_{rain}$  are the attenuations caused by oxygen absorption<sup>2</sup> and rain, respectively. The noise variance in the RF channel is given by  $\sigma_{RF}^2 = WN_0N_F$  [24], where  $W$  is the RF bandwidth,  $N_0$  is the noise power spectral density and  $N_F$  is the noise figure of the RF receiver.

The instantaneous received SNR of the RF link  $\gamma_{RF}$  is given by  $\gamma_{RF} = \bar{\gamma}_{RF}h_{RF}^2$ , where  $\bar{\gamma}_{RF}$  is the average SNR of the RF link defined as  $\bar{\gamma}_{RF} = E_sP_{RF}G_{RF}/\sigma_{RF}^2$  [24].

The fading gain  $h_{RF}$  is modeled by Nakagami- $m$  distribution, which represents a wide variety of realistic Line-of-Sight (LOS), and Non-LOS (NLOS) fading channels encountered in practice [58]. Accordingly, the received SNR  $\gamma_{RF}$  will have the following PDF [59]:

$$f_{\gamma_{RF}}(\gamma_{RF}) = \frac{\left(\frac{m}{\bar{\gamma}_{RF}}\right)^m \gamma_{RF}^{m-1}}{\Gamma(m)} \exp\left(\frac{-m\gamma_{RF}}{\bar{\gamma}_{RF}}\right), \gamma_{RF} \geq 0. \quad (2.12)$$

<sup>2</sup>Oxygen absorption at 60 GHz attenuates the signal at all times, regardless of the weather [57].

By using [53, Eq. (3.351.1)], and some simple algebraic manipulations, the CDF of  $\gamma_{RF}$  can be expressed as:

$$F_{\gamma_{RF}}(\gamma_{RF}) = \frac{1}{\Gamma(m)} \gamma \left( m, \frac{m\gamma_{RF}}{\bar{\gamma}_{RF}} \right), \quad \gamma_{RF} \geq 0, \quad (2.13)$$

where  $\gamma(\cdot, \cdot)$  is the lower incomplete Gamma function defined in [53, Eq. (8.350.1)].

## 2.2 Outage Analysis of Hybrid FSO/RF System with Adaptive Combining

When the instantaneous output SNR  $\gamma_c$  falls below a given threshold  $\gamma_{out}$ , the communication system goes in a state called outage, in which the received SNR can't support the target BER of the system. The probability that the SNR  $\gamma_c$  falls below the outage threshold  $\gamma_{out}$  can be simply calculated by evaluating the CDF of  $\gamma_c$  at  $\gamma_{out}$  as  $P_{out} = F_{\gamma_c}(\gamma_{out})$ .

Based on the modes of operation of the proposed hybrid FSO/RF system, the CDF of  $\gamma_c$ , is given by:

$$\begin{aligned} F_{\gamma_c}(x) &= P_r[\gamma_{FSO} \geq \gamma_T, \gamma_{FSO} < x] + P_r[\gamma_{FSO} < \gamma_T, \gamma_{FSO} + \gamma_{RF} < x] \\ &= \begin{cases} F_1(x) & \text{if } x \leq \gamma_T \\ F_{\gamma_{FSO}}(x) - F_{\gamma_{FSO}}(\gamma_T) + F_2(x) & \text{if } x > \gamma_T, \end{cases} \end{aligned} \quad (2.14)$$

where  $F_1(x)$  is defined as:

$$F_1(x) = \int_0^x f_{\gamma_{FSO} + \gamma_{RF}}(y) dy, \quad (2.15)$$

and  $F_2(x)$  is defined as:

$$F_2(x) = \int_0^{\gamma_T} f_{\gamma_{FSO}}(\gamma_{FSO}) F_{\gamma_{RF}}(x - \gamma_{FSO}) d\gamma_{FSO}, \quad (2.16)$$

with  $F_{\gamma_{FSO}}(\cdot)$ , and  $F_{\gamma_{RF}}(\cdot)$  are given by (2.9), and (2.13) respectively.

Noting that the FSO and RF links are statistically independent,  $f_{\gamma_{FSO} + \gamma_{RF}}(y)$  in

(2.15) can be evaluated as:

$$f_{\gamma_{FSO}+\gamma_{RF}}(y) = \int_0^y f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(y - \gamma_{FSO}) d\gamma_{FSO}. \quad (2.17)$$

After substituting (2.8) and (2.12) into (2.17) and applying the binomial expansion defined in [53, Eq. (1.111)], and the series expansion of the exponential defined in [53, Eq. (1.211.1)], along with [56, Eq. (07.34.21.0084.01)],  $f_{\gamma_{FSO}+\gamma_{RF}}(y)$  can be evaluated as:

$$f_{\gamma_{FSO}+\gamma_{RF}}(y) = \frac{2^{\alpha+\beta-2} e^{\frac{-my}{\bar{\gamma}_{RF}}} \left(\frac{m}{\bar{\gamma}_{RF}}\right)^m y^{m-1}}{\pi \Gamma(\alpha) \Gamma(\beta) \Gamma(m)} \left\{ \sum_{n=0}^{\infty} \frac{\left(\frac{my}{\bar{\gamma}_{RF}}\right)^n}{n!} \sum_{i=0}^{m-1} \binom{m-1}{i} \right. \\ \left. \times (-1)^i G_{1,5}^{4,1} \left( \frac{(\alpha\beta)^2 y}{16\bar{\gamma}_{FSO}} \mid \begin{matrix} K_1 \\ K_2 \end{matrix} \right) \right\}, \quad (2.18)$$

where  $K_1 = 1 - n - i$  and  $K_2 = \frac{\alpha}{2}, \frac{\alpha+1}{2}, \frac{\beta}{2}, \frac{\beta+1}{2}, -n - i$ .

Substituting with (2.18) in (2.15), using the series expansion of the exponential, and applying [55, Eq. (26)],  $F_1(x)$  can be expressed as:

$$F_1(x) = \frac{2^{\alpha+\beta-2} \left(\frac{mx}{\bar{\gamma}_{RF}}\right)^m}{\pi \Gamma(\alpha) \Gamma(\beta) \Gamma(m)} \left\{ \sum_{n=0}^{\infty} \frac{\left(\frac{mx}{\bar{\gamma}_{RF}}\right)^n}{n!} \sum_{i=0}^{m-1} \binom{m-1}{i} (-1)^i \sum_{k=0}^{\infty} \frac{\left(\frac{-mx}{\bar{\gamma}_{RF}}\right)^k}{k!} \right. \\ \left. \times G_{2,6}^{4,2} \left( \frac{(\alpha\beta)^2 x}{16\bar{\gamma}_{FSO}} \mid \begin{matrix} K_3 \\ K_4 \end{matrix} \right) \right\}, \quad (2.19)$$

where  $K_3 = 1 - n - i, 1 - k - n - m$  and  $K_4 = \frac{\alpha}{2}, \frac{\alpha+1}{2}, \frac{\beta}{2}, \frac{\beta+1}{2}, -k - n - m, -n - i$ .

Substituting with (2.8) and (2.13) in (2.16),  $F_2(x)$  can be expressed in the integral form as:

$$F_2(x) = \int_0^{\gamma_T} \frac{\gamma(m, \frac{m(x-\gamma_{FSO})}{\bar{\gamma}_{RF}}) \gamma_{FSO}^{-1}}{2\Gamma(\alpha)\Gamma(\beta)\Gamma(m)} G_{0,2}^{2,0} \left( \frac{\alpha\beta\gamma_{FSO}^{1/2}}{\sqrt{\bar{\gamma}_{FSO}}} \mid \begin{matrix} - \\ \alpha, \beta \end{matrix} \right) d\gamma_{FSO}. \quad (2.20)$$

By using the series representation of  $\gamma(\cdot, \cdot)$ , defined in [53, Eqs. (8.352.1)], and then applying the binomial expansion rule, along with the series expansion of the expo-

nential, the term  $\gamma\left(m, \frac{m(x-\gamma_{FSO})}{\bar{\gamma}_{RF}}\right)$  in (2.20) can be represented by:

$$\gamma\left(m, \frac{m(x-\gamma_{FSO})}{\bar{\gamma}_{RF}}\right) = (m-1)! \left[ 1 - e^{\frac{-mx}{\bar{\gamma}_{RF}}} \sum_{n=0}^{\infty} \frac{\left(\frac{m\gamma_{FSO}}{\bar{\gamma}_{RF}}\right)^n}{n!} \sum_{k=0}^{m-1} \frac{\left(\frac{m}{\bar{\gamma}_{RF}}\right)^k}{k!} \times \sum_{j=0}^k \binom{k}{j} x^{k-j} (-\gamma_{FSO})^j \right]. \quad (2.21)$$

By plugging (2.21) in (2.20) and applying [56, Eq. (07.34.21.0084.01)],  $F_2(x)$  can be evaluated as:

$$F_2(x) = \frac{(m-1)!}{\Gamma(m)} F_{\gamma_{FSO}}(\gamma_T) - \left\{ \frac{2^{\alpha+\beta-2} e^{\frac{-mx}{\bar{\gamma}_{RF}}} (m-1)!}{\pi \Gamma(\alpha) \Gamma(\beta) \Gamma(m)} \sum_{n=0}^{\infty} \frac{(m\gamma_T/\bar{\gamma}_{RF})^n}{n!} \times \sum_{k=0}^{m-1} \frac{(mx/\bar{\gamma}_{RF})^k}{k!} \sum_{j=0}^k \binom{k}{j} \left(\frac{-\gamma_T}{x}\right)^j G_{1,5}^{4,1} \left( \frac{(\alpha\beta)^2 \gamma_T}{16\bar{\gamma}_{FSO}} \mid \begin{matrix} K_5 \\ K_6 \end{matrix} \right) \right\}, \quad (2.22)$$

where  $K_5 = 1 - n - j$  and  $K_6 = \frac{\alpha}{2}, \frac{\alpha+1}{2}, \frac{\beta}{2}, \frac{\beta+1}{2}, -n - j$ .

Finally, the CDF of  $\gamma_c$  is obtained after substituting (2.19) and (2.22) into (2.14).

## 2.3 Numerical Results

In this section, we present several numerical examples to illustrate our analysis. We assume fading severity over RF link of  $m=5$ . In Figs. 2.2 and 2.3, we consider clear weather condition, which is the hybrid FSO/RF system's operational condition most of the time. We used typical values of  $\alpha$  and  $\beta$  for strong atmospheric turbulence ( $\alpha = 2.064$ , and  $\beta = 1.342$  [60]), which has the dominant effect on hybrid system's performance in this case. In Figs. 2.4 and 2.5, we consider adverse weather conditions, mainly fog and rain, which may last shortly. In Fig. 2.4, we assume moderate rain weather condition with weather-dependent attenuation coefficient  $\alpha_{FSO} = 5.8$  dB/km, RF rain attenuation coefficient  $\alpha_{rain} = 5.6$  dB/km, and  $C_n^2 = 5 \times 10^{-15}$  [24]. In Fig. 2.5, we assume light fog weather condition with weather-dependent attenuation coefficient  $\alpha_{FSO} = 20$  dB/km, RF rain attenuation coefficient  $\alpha_{rain} = 0$  dB/km, and  $C_n^2 = 5 \times 10^{-15}$  [17]. The values of FSO and RF sub-systems parameters, used to obtain results in Figs. 2.4 and 2.5 are given in Table 2.1. Assume using binary PSK digital modulation,  $\gamma_T = 10.5$  dB to satisfy target BER of  $10^{-6}$ .

It can be seen from Fig. 2.2 that the hybrid FSO/RF system gives much better

Table 2.1: Parameters of FSO and RF subsystems

Parameter	Symbol	Value
FSO Subsystem		
Wavelength	$\lambda_{FSO}$	1550 nm
Shot Noise Variance	$\sigma_{FSO}^2$	$2 \times 10^{-14}$
Responsivity	$\eta$	0.5 A/W
Photodetector Diameter	D	20 cm
RF Subsystem		
Carrier Frequency	$f_{RF}$	60 GHz
Bandwidth	$W$	250 MHz
Transmit Antenna Gain	$G_T$	43 dBi
Receive Antenna Gain	$G_R$	43 dBi
Noise Power Spectral Density	$N_0$	-114 dBm/MHz
Receiver Noise Figure	$N_F$	5 dB
Oxygen Attenuation	$\alpha_{oxy}$	15.1 dB/Km

outage performance than using FSO-only or RF-only systems in clear weather conditions. Also, as expected, it can be observed that the performance of the hybrid system is improved with the increase of  $\bar{\gamma}_{RF}$ . The numerical results shown in Fig. 2.2 are obtained using  $n=30$  and  $k=30$  in (2.19) and  $n=30$  in (2.22). As can be observed from Fig. 2.2, evaluating the outage probability using the truncated values of (2.19) and (2.22) gives accurate results that coincide with the values of the outage probability obtained by evaluating the integrals in (2.15) and (2.16) using numerical methods.

It can be seen from Fig. 2.3 that, when  $\gamma_{out}$  is less than  $\gamma_T$ , the outage performance of the hybrid FSO/RF system is improved, because the system activates RF link before the FSO link goes in outage. In this case, and as expected, outage probability decreases as  $\bar{\gamma}_{RF}$  increases. On the other hand, when  $\gamma_{out}$  is greater than  $\gamma_T$ , the outage performance of the hybrid system does not decrease, as the RF link quality improves because the system goes in outage before it activates the RF link.

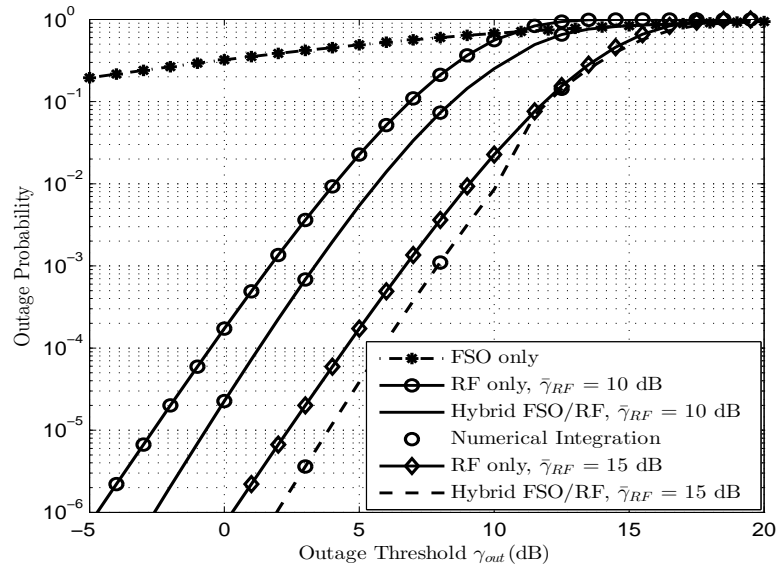


Figure 2.2: Outage probability of a hybrid FSO/RF system as a function of the outage threshold with  $\bar{\gamma}_{FSO} = 10$  dB.

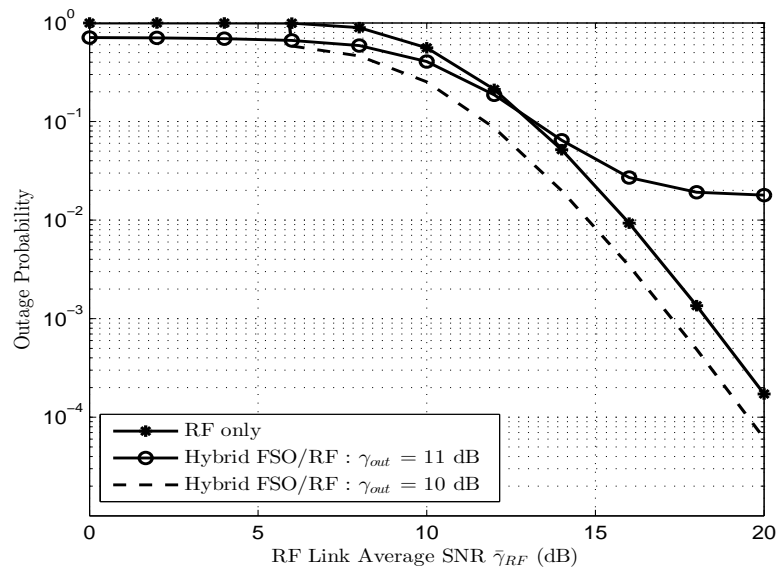


Figure 2.3: Outage probability of a hybrid FSO/RF system as a function of the average SNR of the RF link with  $\bar{\gamma}_{FSO} = 10$  dB compared to the RF-only system.

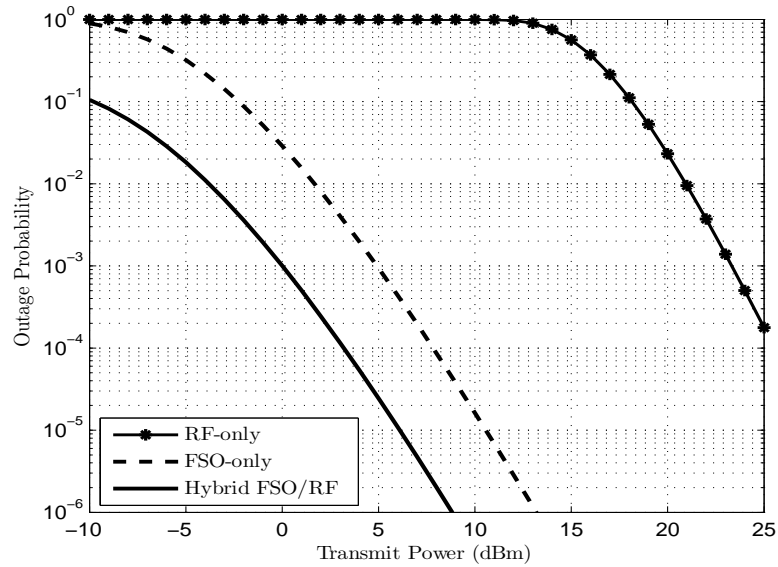


Figure 2.4: Outage probability of a hybrid FSO/RF system as a function of transmit power in moderate rain conditions, with  $\gamma_{out}=10$  dB, and link range  $z=4000$  m.

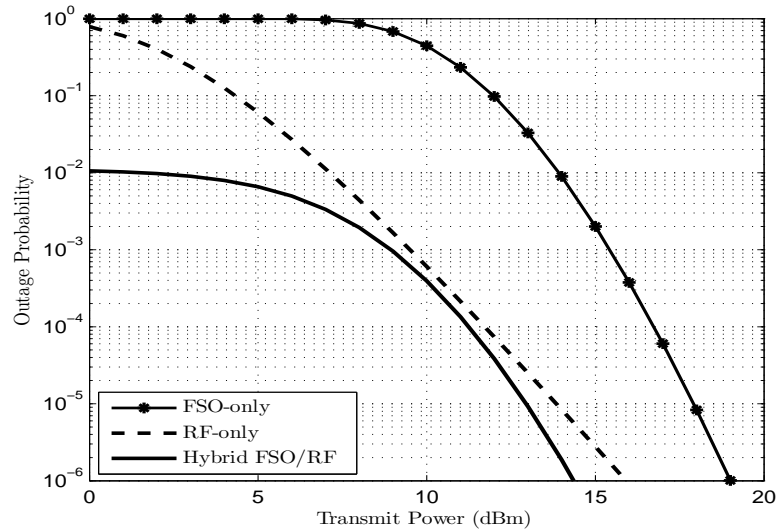


Figure 2.5: Outage probability of a hybrid FSO/RF system as a function of transmit power in light fog conditions, with  $\gamma_{out}=10$  dB, and link range  $z=2000$  m.

It can be seen from Fig. 2.4 that, FSO link's quality degrades due to weak atmospheric turbulence in rain conditions. As observed, considering the “five nines” reliability criterion which implies an outage performance of  $10^{-6}$ , there is an improvement by using the hybrid system of about 4 dB in transmit power over the FSO-only

system.

It can be seen from Fig. 2.5 that, FSO link's quality degrades much in fog conditions. Thus, activating the MMW RF link, which is not affected by fog conditions, greatly improves the outage performance of the hybrid system with an improvement of about 5 dB in transmit power over the FSO-only system considering the "five nines" reliability criterion.

## 2.4 Summery

In this chapter, we analyzed the performance of a hybrid FSO/RF transmission scheme based on adaptive combining. We offered a closed-form of the exact CDF of the received SNR for the proposed hybrid system, which is used to study its outage performance. Numerical results show that hybrid FSO/RF system with adaptive combining transmission scheme has superior outage performance compared to FSO-only and RF-only systems in all weather conditions and atmospheric turbulence regimes.

## Chapter 3

# Joint Adaptive Modulation and Combining for Hybrid FSO/RF Systems

In this chapter, we present and analyze a new transmission scheme for hybrid FSO/RF communication system based on joint adaptive modulation and adaptive combining. Specifically, the data rate on the FSO link is adjusted in discrete manner according to the FSO link's instantaneous received SNR. If the FSO link's quality is too poor to maintain the target BER, the system activates the RF link along with the FSO link. When the RF link is activated, simultaneous transmission of the same modulated data takes place on both links, where the received signals from both links are combined using MRC scheme. In this case, the data rate of the system is adjusted according to the instantaneous combined SNRs. We study the spectral and outage performances of the proposed joint adaptive hybrid FSO/RF system.

The remainder of the chapter is organized as follows. In section 3.1, we introduce the system and channel modeling. Subsequently, the performance metrics of the proposed adaptive hybrid system are introduced in section 3.2. Section 3.3 briefly introduces the performance metrics of switch-over hybrid system. Finally, Section 3.4 presents some numerical examples to express the performance of the proposed joint adaptive hybrid system followed by the chapter summary in section 3.5.

### 3.1 System and Channel Modeling

We consider hybrid FSO/RF system, which is composed of coherent/heterodyne FSO and RF communication subsystems. Coded digital baseband signal, created by signal source, is converted to analog electrical signal through electrical modulator, which can adaptively use one of  $N$  different  $M$ -square quadrature amplitude modulation (QAM) schemes.  $M$ -QAM is widely used in high-rate data transmissions over FSO links [61], and RF links [62], because of its high spectral efficiency, and ease of signal modulation/demodulation process. A particular constellation size  $M$  is chosen to achieve the highest possible spectral efficiency, while maintaining the instantaneous BER below the target value of  $\text{BER}_0$ . Let  $\gamma_{T_1}, \gamma_{T_2}, \dots, \gamma_{T_N}$  be the  $N$  different thresholds corresponding to constellation sizes of  $M = 4, 16, \dots, 2^{2N}$ , respectively such that  $\gamma_{T_1} < \gamma_{T_2} < \dots < \gamma_{T_N}$ . Note that  $\gamma_{T_{N+1}} = \infty$ . To meet a BER requirement of  $\text{BER}_0$ , the thresholds are set using [32]:

$$\gamma_{T_n} = (2^{2n} - 1) \left[ -\frac{2}{3} \ln(5 \text{BER}_0) \right], \quad n \geq 1, \quad (3.1)$$

where the instantaneous BER of coherent  $M$ -QAM of size  $2^{2n}$ , can be well approximated by [32]:

$$\text{BER}_n(\gamma_{T_n}) = 0.2 \exp \left( \frac{-1.5}{2^{2n} - 1} \gamma_{T_n} \right), \quad 2^{2n} \geq 4, \quad 0 \leq \gamma_{T_n} \leq 30\text{dB}. \quad (3.2)$$

#### 3.1.1 Modeling the FSO Link

At the FSO transmitter terminal, QAM electrical signal is mixed with an optical carrier, produced by an optical frequency Local Oscillator (LO) to produce the optical signal. At the FSO receiver terminal, the received optical signal under goes heterodyne detection process. The instantaneous SNR per symbol of the FSO receiver is given by [63, 64]:

$$\gamma_{FSO} = \bar{\gamma}_{FSO} h_{FSO}, \quad (3.3)$$

where  $\bar{\gamma}_{FSO}$  and  $h_{FSO}$  are respectively, the average SNR and the fading gain over the FSO link, with  $E[h_{FSO}]$  is normalized to unity, where  $E[\cdot]$  is the expectation operator. Assume using phase-locked loop (PLL) to compensate for phase noise in the received optical signal and using large enough LO power, such that thermal and background noises can be neglected [63]. In this case, the average SNR  $\bar{\gamma}_{FSO}$  is

given by  $\bar{\gamma}_{FSO} = 2E_{avg}\eta^2P_{LO}P_{FSO}G_{FSO}/\sigma_{FSO}^2$  [63, 64], where  $E_{avg}$ ,  $\eta$ ,  $P_{LO}$ ,  $P_{FSO}$ ,  $G_{FSO}$ , and  $\sigma_{FSO}^2$  are the average QAM symbol energy, photodetector responsivity, LO power, average transmitted optical power, optical power attenuation, and variance of shot noise which is modeled as AWGN, respectively. The shot noise variance  $\sigma_{FSO}^2$  is given by  $\sigma_{FSO}^2 = 2q\eta P_{LO}/T$  [63], where  $q$  is the electronic charge and  $1/T$  is the transmission rate in bits/second. The optical power attenuation  $G_{FSO}$  is given by Beers-Lambert law as  $G_{FSO} = \alpha_{FSO}z$  [26], with  $\alpha_{FSO}$  being the weather-dependent attenuation coefficient (in dB/Km) and  $z$  is the link range from the transmitter to the receiver. The attenuation  $G_{FSO}$  is considered as a fixed scaling factor, and no randomness exists in its behavior [17]. The fading gain is defined as  $h_{FSO} = h_a h_p$ , where  $h_a$  is Gamma-Gamma atmospheric turbulence-induced fading gain factor [54] and  $h_p$  is Gaussian pointing errors-induced fading gain factor [17].

Following the same procedure used in [65], it is easy to show that the PDF of  $\gamma_{FSO}$  is given by:

$$f_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{\xi^2 \gamma_{FSO}^{-1}}{\Gamma(\alpha)\Gamma(\beta)} G_{1,3}^{3,0} \left[ \frac{\xi^2 \alpha \beta \gamma_{FSO}}{(\xi^2 + 1) \bar{\gamma}_{FSO}} \middle| \begin{matrix} \xi^2 + 1 \\ \xi^2, \alpha, \beta \end{matrix} \right], \quad (3.4)$$

where  $\xi$  is the ratio between the equivalent beam radius  $\omega_{eq}$  and the pointing error (jitter) standard deviation  $\sigma_s$  given by  $\xi = \omega_{eq}/2\sigma_s$ . Here,  $\omega_{eq}^2 = \omega_z^2 \sqrt{\pi} \text{erf}(\nu)/2\nu \exp(-\nu^2)$ , where  $\text{erf}(\cdot)$  is the error function and  $\omega_z$  is the beam radius calculated at distance  $z$  from the transmitter aperture and  $\nu = \sqrt{\pi}D/2\sqrt{2}\omega_z$  with  $D$  is the photodetector diameter.  $\omega_z$  is given by  $\omega_z = \theta_0 z$ , where  $\theta_0$  is the transmit divergence at  $1/e^2$ .  $\Gamma(\cdot)$  in (3.4) is the standard Gamma function with  $\alpha$  and  $\beta$  are the scintillation parameters that are related to the refractive index structure parameter  $C_n^2$  [54].  $G[\cdot]$  is the Meijer G-function as defined in [53, Eq. (9.301)]. By using [56, Eq. (07.34.21.0084.01)] and some simple algebraic manipulations, the CDF of  $\gamma_{FSO}$  can be expressed as:

$$F_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{\xi^2}{\Gamma(\alpha)\Gamma(\beta)} G_{2,4}^{3,1} \left[ \frac{\xi^2 \alpha \beta \gamma_{FSO}}{(\xi^2 + 1) \bar{\gamma}_{FSO}} \middle| \begin{matrix} 1, \xi^2 + 1 \\ \xi^2, \alpha, \beta, 0 \end{matrix} \right]. \quad (3.5)$$

### 3.1.2 Modeling the RF Link

At the RF transmitter, QAM electrical signal's frequency is up-converted using 60 GHz RF carrier, produced by RF LO. The instantaneous received SNR from the RF

branch, denoted by  $\gamma_{RF}$ , can be given by [24]:

$$\gamma_{RF} = \bar{\gamma}_{RF} h_{RF}^2, \quad (3.6)$$

where  $h_{RF}$  is the fading gain over the RF channel, with  $E[h_{RF}^2]$  normalized to unity, and  $\bar{\gamma}_{RF}$  is the average SNR of the RF channel, given by  $\bar{\gamma}_{RF} = E_{avg} P_{RF} G_{RF} / \sigma_{RF}^2$  [24], with  $E_{avg}$ ,  $P_{RF}$ ,  $\sigma_{RF}^2$ , and  $G_{RF}$  are respectively, average QAM symbol energy, transmitted RF power, noise variance, assuming zero-mean circularly symmetric AWGN, and average power gain of the RF channel, which is given by [24]:

$$G_{RF}[dB] = G_T + G_R - 20 \log_{10} \left( \frac{4\pi z}{\lambda_{RF}} \right) - \alpha_{oxy} z - \alpha_{rain} z, \quad (3.7)$$

where  $G_T$  and  $G_R$  denote the transmit and receive antenna gains, respectively,  $\lambda_{RF}$  is the wavelength of the RF subsystem,  $\alpha_{oxy}$  and  $\alpha_{rain}$  are the attenuations caused by oxygen absorption and rain, respectively and  $z$  is the link distance. The noise variance in the RF channel is given by [24],  $\sigma_{RF}^2 = W N_0 N_F$ , where  $W$  is the RF bandwidth,  $N_0$  is the noise power spectral density and  $N_F$  is the noise figure of the RF receiver.

The fading gain  $h_{RF}$  follows Nakagami- $m$  distribution, which represents a wide variety of realistic LOS and non LOS fading channels encountered in practice [58]. The PDF and CDF of  $\gamma_{RF}$  are respectively given by [59]:

$$f_{\gamma_{RF}}(\gamma_{RF}) = \left( \frac{m}{\bar{\gamma}_{RF}} \right)^m \frac{\gamma_{RF}^{m-1}}{\Gamma(m)} \exp \left( \frac{-m\gamma_{RF}}{\bar{\gamma}_{RF}} \right), \quad (3.8)$$

$$F_{\gamma_{RF}}(\gamma_{RF}) = \frac{1}{\Gamma(m)} \gamma \left( m, \frac{m\gamma_{RF}}{\bar{\gamma}_{RF}} \right). \quad (3.9)$$

where  $\gamma(\cdot, \cdot)$  is the lower incomplete Gamma function defined in [53, Eq. (8.350.1)].

## 3.2 Performance Analysis of the Proposed Joint Adaptive Scheme

To achieve the maximum spectral efficiency, the FSO link uses the modulation scheme  $2^{2N}$ -QAM as long as  $\gamma_{FSO}$  is greater than or equal to  $\gamma_{TN}$ . If  $\gamma_{FSO}$  decreases beyond  $\gamma_{TN}$ , the receiver checks another threshold  $\gamma_{Tn}$  in a descending order until one

threshold satisfies  $\gamma_{FSO} \geq \gamma_{T_n}$ . In this case, the receiver sends a feedback signal to the transmitter indicating the modulation scheme  $2^{2n}$ -QAM should be used without activating RF subsystem. If the thresholds checking process reaches  $\gamma_{T_1}$  and  $\gamma_{FSO}$  is less than  $\gamma_{T_1}$ , the receiver sends a feedback signal to activate the RF link along with the FSO link for simultaneous transmission of the same data. Therefore, the feedback required is  $\lceil \log_2(N + 1) \rceil$  bits for the first stage. At the receiver terminal, the data transmitted along both links will be combined using MRC combiner. In this case, the receiver SNR, denoted by  $\gamma_c$ , will equal to the sum of  $\gamma_{FSO}$  and  $\gamma_{RF}$ . Note that  $\gamma_c$  is equal to  $\gamma_{FSO}$  as long as  $\gamma_{FSO} \geq \gamma_{T_1}$ . To this end, the receiver checks whether  $\gamma_c$  is greater than or equal to  $\gamma_{T_N}$ . If so, the receiver sends a feedback signal for the transmitter to use the modulation scheme  $2^{2N}$ -QAM on both FSO link and RF link. If not, the receiver checks another threshold  $\gamma_{T_n}$  in a descending order until one threshold satisfies  $\gamma_c \geq \gamma_{T_n}$ . In this case, the receiver sends a feedback signal to the transmitter to select the modulation scheme  $2^{2n}$ -QAM. If the receiver thresholds checking process reaches  $\gamma_{T_1}$  and  $\gamma_c < \gamma_{T_1}$ , the receiver sends a signal to suspend data transmission over both FSO and RF links<sup>1</sup>. In this second stage, if necessary, the feedback load is again  $\lceil \log_2(N + 1) \rceil$  bits. The average feedback of the proposed adaptive hybrid system is  $\lceil \log_2(N + 1) \rceil (1 + \text{Pr}[\gamma_{FSO} < \gamma_{T_1}])$  bits. Fig. 3.1 summarizes the joint adaptive modulation and combining operation of the the hybrid FSO/RF system.

Before we study the performance of this joint adaptive scheme, we need to deduce the CDF of  $\gamma_c$ . Based on the modes of operation of this joint adaptive scheme, the CDF of  $\gamma_c$ , is given by:

$$\begin{aligned}
 F_{\gamma_c}(x) &= \text{Pr}[\gamma_{FSO} \geq \gamma_{T_1}, \gamma_{FSO} < x] + \text{Pr}[\gamma_{FSO} < \gamma_{T_1}, \gamma_{FSO} + \gamma_{RF} < x] \\
 &= \begin{cases} F_1(x), & \text{if } x \leq \gamma_{T_1} \\ F_{\gamma_{FSO}}(x) - F_{\gamma_{FSO}}(\gamma_{T_1}) + F_2(x), & \text{if } x > \gamma_{T_1}, \end{cases} \quad (3.10)
 \end{aligned}$$

where  $F_1(x)$  is defined as:

$$F_1(x) = \int_0^x f_{\gamma_{FSO} + \gamma_{RF}}(y) dy, \quad (3.11)$$

---

<sup>1</sup>When data transmission is suspended, pilot signal is assumed to be continuously transmitted over the FSO link to check its status as it is the main channel of the system that provides high data rate transmission.

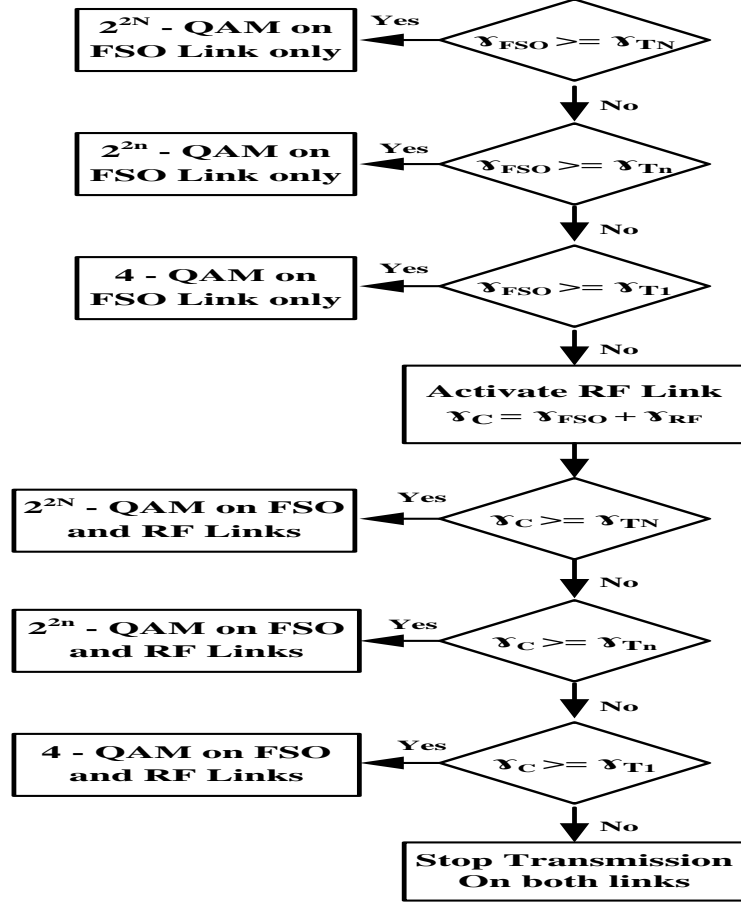


Figure 3.1: Flow chart of the operation of the joint adaptive hybrid FSO/RF scheme.

and  $F_2(x)$  is defined as:

$$F_2(x) = \int_0^{\gamma_{T1}} f_{\gamma_{FSO}}(\gamma_{FSO}) F_{\gamma_{RF}}(x - \gamma_{FSO}) d\gamma_{FSO}. \quad (3.12)$$

Noting that the FSO and RF links are statistically independent,  $f_{\gamma_{FSO}+\gamma_{RF}}(y)$  in (3.11) can be evaluated as:

$$f_{\gamma_{FSO}+\gamma_{RF}}(y) = \int_0^y f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(y - \gamma_{FSO}) d\gamma_{FSO}. \quad (3.13)$$

After substituting (3.4) and (3.8) into (3.13) and applying the binomial expansion, and the series expansion of the exponential function, along with [56, Eq. (07.34.21.0084.01)],

$f_{\gamma_{FSO}+\gamma_{RF}}(y)$  can be evaluated as:

$$f_{\gamma_{FSO}+\gamma_{RF}}(y) = \frac{\xi^2 e^{\frac{-my}{\bar{\gamma}_{RF}}} \left(\frac{m}{\bar{\gamma}_{RF}}\right)^m y^{m-1}}{\Gamma(\alpha)\Gamma(\beta)\Gamma(m)} \left\{ \sum_{n=0}^{\infty} \frac{\left(\frac{my}{\bar{\gamma}_{RF}}\right)^n}{n!} \sum_{i=0}^{m-1} \binom{m-1}{i} (-1)^i \right. \\ \left. \times G_{2,4}^{3,1} \left[ \frac{\xi^2 \alpha \beta y}{(\xi^2 + 1) \bar{\gamma}_{FSO}} \middle| \begin{matrix} 1-n-i, \xi^2+1 \\ \xi^2, \alpha, \beta, -n-i \end{matrix} \right] \right\}. \quad (3.14)$$

Substituting with (3.14) in (3.11), using the series expansion of the exponential function, and applying [56, Eq. (07.34.21.0084.01)],  $F_1(x)$  can be expressed as:

$$F_1(x) = \frac{\xi^2 \left(\frac{mx}{\bar{\gamma}_{RF}}\right)^m}{\Gamma(\alpha)\Gamma(\beta)\Gamma(m)} \left\{ \sum_{n=0}^{\infty} \frac{\left(\frac{mx}{\bar{\gamma}_{RF}}\right)^n}{n!} \sum_{i=0}^{m-1} \binom{m-1}{i} (-1)^i \sum_{k=0}^{\infty} \frac{\left(\frac{-mx}{\bar{\gamma}_{RF}}\right)^k}{k!} \right. \\ \left. \times G_{3,5}^{3,2} \left[ \frac{\xi^2 \alpha \beta x}{(\xi^2 + 1) \bar{\gamma}_{FSO}} \middle| \begin{matrix} 1-n-i, 1-k-n-m, \xi^2+1 \\ \xi^2, \alpha, \beta, -k-n-m, -n-i \end{matrix} \right] \right\}. \quad (3.15)$$

Substituting with (3.4) and (3.9) in (3.12),  $F_2(x)$  can be expressed in the integral form as:

$$F_2(x) = \int_0^{\gamma_{T1}} \frac{\gamma\left(m, \frac{m(x-\gamma_{FSO})}{\bar{\gamma}_{RF}}\right) \xi^2 \gamma_{FSO}^{-1}}{\Gamma(\alpha)\Gamma(\beta)\Gamma(m)} \times G_{1,3}^{3,0} \left[ \frac{\xi^2 \alpha \beta}{(\xi^2 + 1) \bar{\gamma}_{FSO}} \frac{\gamma_{FSO}}{\bar{\gamma}_{RF}} \middle| \begin{matrix} \xi^2+1 \\ \xi^2, \alpha, \beta \end{matrix} \right] d\gamma_{FSO}. \quad (3.16)$$

By using the series representation of  $\gamma(a, x)$  in (3.16) defined in [53, Eqs. (8.352.1)], and then applying the binomial expansion rule along with the series expansion of the exponential function, the term  $\gamma\left(m, \frac{m(x-\gamma_{FSO})}{\bar{\gamma}_{RF}}\right)$  can be represented by:

$$\gamma\left(m, \frac{m(x-\gamma_{FSO})}{\bar{\gamma}_{RF}}\right) = (m-1)! \left\{ 1 - e^{\frac{-mx}{\bar{\gamma}_{RF}}} \sum_{n=0}^{\infty} \frac{\left(\frac{m\gamma_{FSO}}{\bar{\gamma}_{RF}}\right)^n}{n!} \sum_{k=0}^{m-1} \frac{\left(\frac{m}{\bar{\gamma}_{RF}}\right)^k}{k!} \right. \\ \left. \sum_{j=0}^k \binom{k}{j} x^{k-j} (-\gamma_{FSO})^j \right\}. \quad (3.17)$$

By plugging (3.17) in (3.16) and applying [56, Eq. (07.34.21.0084.01)],  $F_2(x)$  can be

evaluated as:

$$F_2(x) = \frac{(m-1)!}{\Gamma(m)} F_{\gamma_{FSO}}(\gamma_{T1}) - \left\{ \frac{\xi^2 e^{\frac{-mx}{\bar{\gamma}_{RF}}} (m-1)!}{\Gamma(\alpha)\Gamma(\beta)\Gamma(m)} \sum_{n=0}^{\infty} \frac{(m\gamma_{T2}/\bar{\gamma}_{RF})^n}{n!} \sum_{k=0}^{m-1} \frac{(mx/\bar{\gamma}_{RF})^k}{k!} \sum_{j=0}^k \binom{k}{j} \times \left( \frac{-\gamma_{T1}}{x} \right)^j G_{2,4}^{3,1} \left[ \frac{\xi^2 \alpha \beta \gamma_{T1}}{(\xi^2 + 1) \bar{\gamma}_{FSO}} \middle| \begin{matrix} 1-n-j, \xi^2+1 \\ \xi^2, \alpha, \beta, -n-j \end{matrix} \right] \right\}. \quad (3.18)$$

Finally, the CDF of  $\gamma_c$  is obtained after substituting (3.15) and (3.18) into (3.10).

### 3.2.1 Average Spectral Efficiency

The average spectral efficiency of the proposed adaptive hybrid FSO/RF system, defined as the average number of bits transmitted over each symbol period [32], is given by:

$$\eta^{Adapt} = \sum_{n=1}^N 2n [F_{\gamma_c}(\gamma_{T_{n+1}}) - F_{\gamma_c}(\gamma_{T_n})]. \quad (3.19)$$

### 3.2.2 Outage Probability

When  $\gamma_{FSO} < \gamma_{T1}$ , and  $\gamma_c$  also falls below  $\gamma_{T1}$ , the communication system goes into outage state, in which the received SNR can't support the target BER of the system and data transmission is suspended over both links. The outage probability of the adaptive hybrid FSO/RF system can be simply calculated by evaluating the CDF of  $\gamma_c$  at  $\gamma_{T1}$  as:

$$P_{out}^{Adapt} = F_{\gamma_c}(\gamma_{T1}) = F_1(\gamma_{T1}). \quad (3.20)$$

### 3.2.3 Average Bit-Error Rate

The average BER of the proposed adaptive hybrid FSO/RF system, defined as the ratio of the average number of erroneously received bits over the total average number of transmitted bits [32], is given by:

$$\langle BER \rangle = \frac{1}{\eta^{Adapt}} \sum_{n=1}^N 2n \overline{BER}_n, \quad (3.21)$$

where  $\overline{BER}_n$  is the average error rate of using constellation of size  $2^{2n}$ , given by:

$$\overline{BER}_n = G_1 + G_2, \quad (3.22)$$

with  $G_1$  corresponds to the FSO-only mode and is defined as:

$$G_1 = \int_{\gamma_{T_n}}^{\gamma_{T_{n+1}}} BER_n(\gamma_{FSO}) f_{\gamma_{FSO}}(\gamma_{FSO}) d\gamma_{FSO}, \quad (3.23)$$

and  $G_2$  represents the combined FSO/RF mode and is defined as:

$$G_2 = \int_{\gamma_{T_n}}^{\gamma_{T_{n+1}}} \int_0^{\gamma_{T_1}} BER_n(\gamma_c) f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(\gamma_c - \gamma_{FSO}) d\gamma_{FSO} d\gamma_c. \quad (3.24)$$

$G_1$  and  $G_2$  can be evaluated using numerical methods with  $BER_n(\cdot)$ ,  $f_{\gamma_{FSO}}(\cdot)$ , and  $f_{\gamma_{RF}}(\cdot)$  are given respectively by (3.2), (3.4), and (3.8).

### 3.3 Performance Analysis of Switch-Over Scheme with Adaptive Modulation

For comparison purposes, we introduce here the performance metrics of switch-over hybrid FSO/RF system [30]. To have fair comparison, we assume using the same adaptive modulation scheme that was used with our proposed system.

#### 3.3.1 Average Spectral Efficiency

The average spectral efficiency of the switch-over hybrid FSO/RF system in this case is given by:

$$\eta^{Switch} = \sum_{n=1}^N 2n \left\{ [F_{\gamma_{FSO}}(\gamma_{T_{n+1}}) - F_{\gamma_{FSO}}(\gamma_{T_n})] + F_{\gamma_{FSO}}(\gamma_{T_1}) \right. \\ \left. \times [F_{\gamma_{RF}}(\gamma_{T_{n+1}}) - F_{\gamma_{RF}}(\gamma_{T_n})] \right\}. \quad (3.25)$$

### 3.3.2 Outage Probability

When  $\gamma_{FSO} < \gamma_{T1}$ , and  $\gamma_{RF}$  also falls below  $\gamma_{T1}$ , the communication system goes into outage. In this case, the outage probability of the hybrid system can be evaluated as:

$$P_{out}^{Switch} = F_{\gamma_{FSO}}(\gamma_{T1})F_{\gamma_{RF}}(\gamma_{T1}). \quad (3.26)$$

## 3.4 Numerical Results

In this section we present several numerical examples to illustrate the math formulation and to study the proposed system's performance. We will consider three different  $2^{2n}$ -QAM modulation schemes with  $n = 1, 2$ , and  $3$ , where the corresponding thresholds  $\gamma_{Tn}$ , assuming  $BER_0 = 10^{-6}$  can be calculated using (3.1). The relevant parameters of the FSO and RF subsystems considered for the numerical results are given in Table 3.1. The strongest atmospheric turbulence commonly occurs when weather is clear and becomes weaker as the weather condition gets worse by means of either fog or rain. We consider in our numerical examples the scenario of clear weather condition and strong atmospheric turbulence ( $C_n^2 = 2 \times 10^{-13}$ ), with weather-dependent attenuation coefficient  $\alpha_{FSO} = 0.44$  dB/km and RF rain attenuation  $\alpha_{rain} = 0$  dB/km, along with pointing error effects [17]. We assume RF channel fading severity of  $m = 5$  in all Figures.

In Fig. 3.2, we plot the average spectral efficiency of the proposed adaptive hybrid FSO/RF system as a function of the transmitted power of the FSO link  $P_{FSO}$ . It can be seen from Fig. 3.2, that average spectral efficiency increases as the FSO link's quality improves by increasing  $P_{FSO}$ . Also, we can observe that with sufficient high  $P_{FSO}$ , the average spectral efficiency of the adaptive hybrid system is the same as that of FSO-only system and switch-over hybrid system which in this case relies on FSO link. This is because the FSO link's quality is good to support the target BER alone without the need of activating the RF link. On the other hand, as the FSO link's quality degrades due to strong atmospheric turbulence in clear weather conditions, the RF link is activated along with the FSO link which leads to a significant improvement in the average spectral efficiency of the adaptive hybrid system over both switch-over hybrid FSO/RF and FSO-only systems, as can be seen from Fig. 3.2. The numerical results shown in Fig. 3.2 for the average spectral efficiency of the proposed adaptive hybrid FSO/RF system are obtained using  $n=30$  and  $k=30$  in (3.15) and  $n=30$  in

Table 3.1: Parameters of FSO and RF subsystems

Parameter	Symbol	Value
FSO Subsystem		
Wavelength	$\lambda_{FSO}$	1550 nm
Transmission Rate	$1/T$	1 Gbit/s
Responsivity	$\eta$	0.75 A/W
Photodetector Diameter	D	20 cm
Transmit divergence at $1/e^2$	$\theta_0$	2.5 mrad
Jitter standard deviation	$\sigma_s$	30 cm
Link distance	$z$	1000 m
RF Subsystem		
Carrier Frequency	$f_{RF}$	60 GHz
Bandwidth	$W$	250 MHz
Transmit Power	$P_{RF}$	-10 dBm
Transmit Antenna Gain	$G_T$	44 dBi
Recieve Antenna Gain	$G_R$	44 dBi
Noise Power Spectral Density	$N_0$	-114 dBm/MHz
Receiver Noise Figure	$N_F$	5 dB
Oxygen Attenuation	$\alpha_{oxy}$	15.1 dB/Km

(3.18), which are then plugged in (3.10) to be used in evaluating (3.19). As can be observed, evaluating the average spectral efficiency using the truncated values of (3.15) and (3.18) gives accurate results that coincide with the values that are obtained by evaluating the integrals in (3.11) and (3.12) using numerical methods before plugged in (3.10) to evaluate (3.19).

In Fig. 3.3, we plot the outage probability of the proposed adaptive hybrid system as a function of  $P_{FSO}$ . It can be seen that the proposed adaptive hybrid system gives an outage performance much better than that of switch-over hybrid system or FSO-only system with the same adaptive modulation scheme. In Fig. 3.4, we plot the average BER of the proposed adaptive hybrid system as a function of  $P_{FSO}$ . It can be shown that, the proposed adaptive hybrid system can achieve an average BER which is less than the target instantaneous BER ( $10^{-6}$  in our numerical examples). As expected, the average BER is improved as the optical link's quality increases.

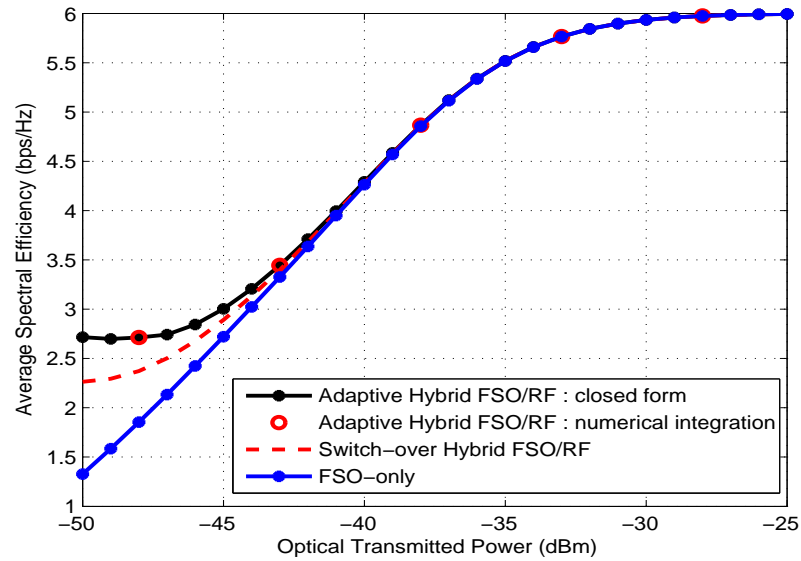


Figure 3.2: Average spectral efficiency of the proposed hybrid FSO/RF system as a function of the transmitted power of the FSO link.

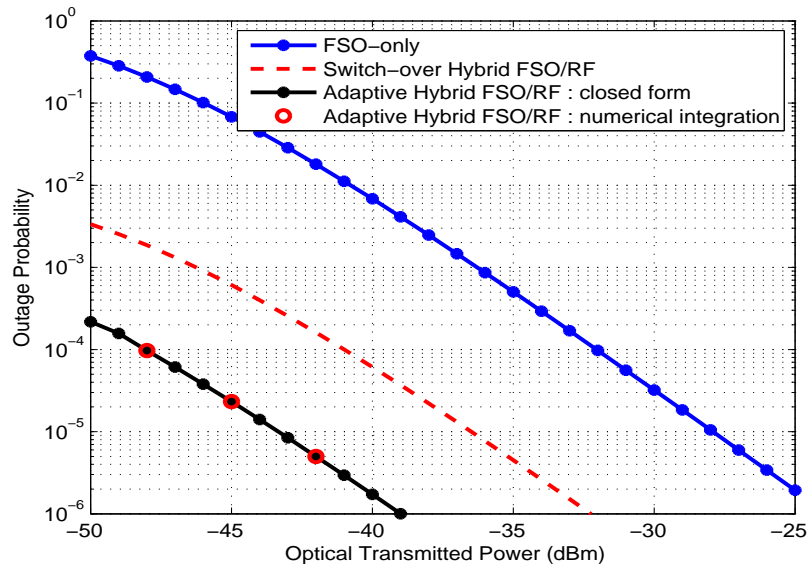


Figure 3.3: Outage probability of the proposed hybrid FSO/RF system as a function of the transmitted power of the FSO link.

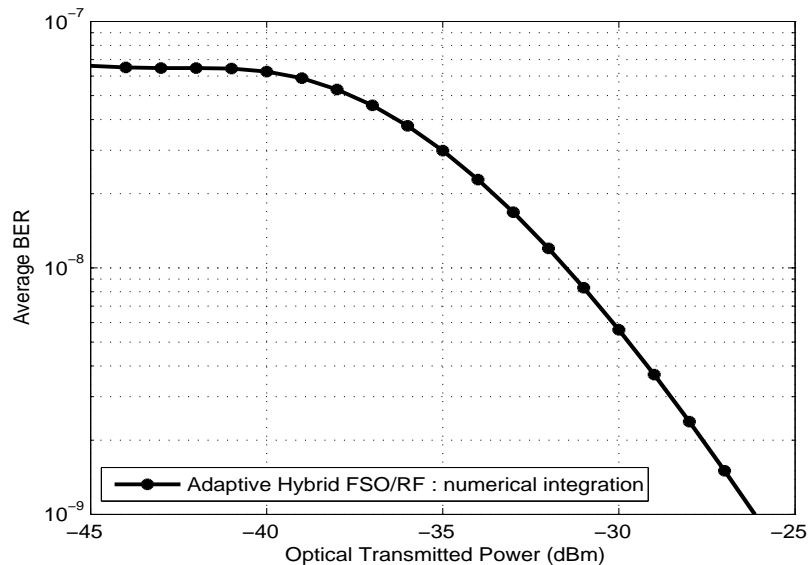


Figure 3.4: Average BER of the proposed hybrid FSO/RF system as a function of the transmitted power of the FSO link.

It is worth to mention that similar superior performance of the proposed adaptive hybrid FSO/RF system over both FSO-only and switch-over hybrid FSO/RF systems is expected in other weather conditions, mainly in fog and rain. In rain conditions, FSO link is not affected and thus the communication system can relay on it without needing to activate the RF link. On the other hand, FSO link is affected by fog which will degrade its performance, thus activating the RF link which is not affected by fog, along with the FSO link, will support the FSO link and maintain a reliable communication channel.

### 3.5 Summery

In this chapter, we presented a new hybrid FSO/RF system based on joint adaptive modulation and adaptive combining scheme. We offered a novel closed-form of the exact CDF of the received SNR for the proposed adaptive hybrid FSO/RF system. The performance metrics of the proposed adaptive hybrid system, mainly average spectral efficiency, outage probability, and average BER are studied. Numerical results showed that the proposed adaptive hybrid FSO/RF system has superior spectral efficiency and outage performance compared to that of switch-over hybrid FSO/RF and FSO-only systems, while maintaining good average BER.

## Chapter 4

# Power Adaptation Based on Truncated Channel Inversion for Hybrid FSO/RF Transmission with Adaptive Combining

In this chapter, we consider power adaptation strategies based on truncated channel inversion for hybrid FSO/RF system employing adaptive combining. Specifically, we adaptively set the RF link transmission power when FSO link quality is unacceptable to ensure constant combined SNR at receiver. Two adaptation strategies are proposed. One strategy depends on the received RF SNR, while the other one depends on the combined SNR of both links. We study the outage probability of the hybrid FSO/RF system with and without power adaptation.

The remainder of the chapter is organized as follows. In section 4.1, we introduce the system and channel models. In section 4.2, we introduce the power allocation strategies, and the outage analysis of the proposed system namely, the outage probability and the outage capacity. Finally, section 4.3 presents some numerical examples to investigate the performance of the hybrid system with and without power adaptation. Further power adaptation for FSO link is introduced in section 4.4, followed by the conclusion in section 4.5.

## 4.1 System and Channel Modeling

We consider a hybrid FSO/RF system, where the FSO link is active all the time with constant transmitted power. To maintain a target data rate, the received SNR should not be less than a predetermined target value denoted by  $\gamma_T$ . When the instantaneous SNR at the receiver of the FSO link denoted by  $\gamma_{FSO}$ , falls below the threshold  $\gamma_T$ , FSO link alone can't support the high data rate transmission. In this case, the receiver sends a feedback signal on the FSO link to activate the RF link along with the FSO link to help maintain the link reliability. When the RF link is activated, simultaneous transmission of the same data on both links takes place. At the receiver, the data received over both links will be combined using an MRC combiner. It is important to clarify that in case of using both FSO and RF links, the data rate of FSO link may be reduced to be the same as that of the RF link to facilitate diversity reception. The receiver SNR, denoted by  $\gamma_c$ , will be equal to  $\gamma_{FSO}$  when  $\gamma_{FSO} \geq \gamma_T$ . When  $\gamma_{FSO} < \gamma_T$ ,  $\gamma_c$  will be equal to the sum of  $\gamma_{FSO}$  and  $\gamma_{RF}$  where  $\gamma_{RF}$  is the receiver SNR of the RF link. In this case, the transmitted power over the RF link is adapted to maintain the constant received SNR  $\gamma_T$ , i.e., to keep  $\gamma_{FSO} + \gamma_{RF} = \gamma_T$ . We will discuss the power adaptation policy in the following section.

### 4.1.1 Modeling the FSO Link

We assume that the FSO link experiences Gamma-Gamma fading due to atmospheric turbulence, and atmospheric loss along with pointing error impairments, for which the PDF of the received irradiance  $I$  is given by [65, Eq. (11)] (or equivalently using [53, Eq. (9.31.5)]):

$$f_I(I) = \frac{\xi^2 I^{-1}}{\Gamma(\alpha)\Gamma(\beta)} G_{1,3}^{3,0} \left[ \frac{\alpha\beta I}{A_0 G_{FSO}} \mid \begin{matrix} \xi^2+1 \\ \xi^2, \alpha, \beta \end{matrix} \right], \quad I \geq 0, \quad (4.1)$$

where  $\xi$  is the ratio between the equivalent beam radius at the FSO receiver aperture and the pointing error (jitter) standard deviation at the FSO receiver,  $A_0$  is a constant term that defines the pointing error loss [17],  $\Gamma(\cdot)$  is the standard Gamma function, and  $\alpha$  and  $\beta$  are the effective number of small-scale and large-scale eddies of the turbulent environment, respectively. Different values of  $\alpha$  and  $\beta$  corresponds to different turbulence regimes. Expressions for calculating the parameters  $\alpha$  and  $\beta$  for different propagation conditions can be found in [54]. In Eq. (4.1),  $G[\cdot]$  is the Meijer G-function as defined in [53, Eq. (9.301)], and  $G_{FSO}$  is the optical power at-

tenuation, given by Beers-Lambert law as  $G_{FSO} = \alpha_{FSO}z$  [26], with  $\alpha_{FSO}$  being the weather-dependent attenuation coefficient (in dB/Km) and  $z$  is the link range from the transmitter to the receiver. The attenuation  $G_{FSO}$  is considered as a fixed scaling factor, and no randomness exists in its behavior [17].

Considering sub-carrier modulated FSO communication system, in which an electrical sub-carrier signal is pre-modulated<sup>1</sup> with the information bits before being used to modulate the optical signal for transmission, there are two techniques for FSO signal detection at the receiver side, which are Intensity Modulation/Direct Detection (IM/DD) [12] and Coherent Modulation/Heterodyne Detection (CM/HD) [13]. A unified expression for the PDF of  $\gamma_{FSO}$ , considering the two types of FSO detection, is given in a general form as [66]:

$$f_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{\xi^2 \gamma_{FSO}^{-1}}{r\Gamma(\alpha)\Gamma(\beta)} G_{1,3}^{3,0} \left[ \frac{\xi^2 \alpha \beta}{(\xi^2 + 1)} \left( \frac{\gamma_{FSO}}{\bar{\gamma}_{FSO_r}} \right)^{\frac{1}{r}} \middle| \begin{matrix} \xi^2 + 1 \\ \xi^2, \alpha, \beta \end{matrix} \right], \quad \gamma_{FSO} \geq 0, \quad (4.2)$$

where  $r$  is the parameter defining the type of FSO detection technique (i.e.,  $r=1$  represents CM/HD technique and  $r=2$  represents IM/DD technique) and  $\bar{\gamma}_{FSO_r}$ <sup>2</sup> is the average SNR of FSO link.

By using [56, Eq. (07.34.21.0084.01)] and some simple algebraic manipulations, the CDF of  $\gamma_{FSO}$  can be expressed as:

$$F_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{\xi^{2r\alpha+\beta-2}}{(2\pi)^{r-1}\Gamma(\alpha)\Gamma(\beta)} G_{r+1,3r+1}^{3r,1} \left[ \frac{B\gamma_{FSO}}{\bar{\gamma}_{FSO_r}} \middle| \begin{matrix} 1, K_1 \\ K_2, 0 \end{matrix} \right], \quad \gamma_{FSO} \geq 0, \quad (4.3)$$

where  $B = \left( \frac{\xi^2 \alpha \beta}{(\xi^2 + 1)r^2} \right)^r$ ,  $K_1 = \frac{\xi^2 + 1}{r}, \dots, \frac{\xi^2 + r}{r}$  has  $r$  terms, and  $K_2 = \frac{\xi^2}{r}, \dots, \frac{\xi^2 + r - 1}{r}, \frac{\alpha}{r}, \dots, \frac{\alpha + r - 1}{r}, \frac{\beta}{r}, \dots, \frac{\beta + r - 1}{r}$  has  $3r$  terms.

### 4.1.2 Modeling the RF Link

At the RF transmitter, the digitally modulated electrical signal, which is the same as the one in FSO subsystem, is up-converted using 60 GHz RF carrier. The up-converted RF signal is transmitted and received using  $L$  branches RF transmis-

<sup>1</sup>For example, by using  $M$ -QAM digital modulation scheme, which is widely used in high-rate data transmissions over FSO links [61], and RF links [62], because of its high spectral efficiency and ease of signal modulation/demodulation process.

<sup>2</sup>For CM/HD,  $\bar{\gamma}_{FSO_1} = \eta_e E[I]/N_0$  [66], with  $\eta_e$  is the effective photoelectric conversion ratio,  $N_0$  symbolizes the AWGN sample, and  $E[I]$  is the expectation of  $I$ , which by using [55, Eq. (24)] is given by  $E[I] = \xi^2 A_0 G_{FSO}/(\xi^2 + 1)$ . For IM/DD,  $\bar{\gamma}_{FSO_2} = (\eta_e E[I])^2/N_0$  [66].

sion/reception scheme. The received SNR from each RF branch, denoted by  $\gamma_{i_{RF}}$ , follows independent and identical distribution (i.i.d) Nakagami- $m$  fading distribution with PDF given by [67]:

$$f_{\gamma_{i_{RF}}}(\gamma_{RF}) = \left(\frac{m}{\bar{\gamma}_{RF}}\right)^m \frac{\gamma_{RF}^{m-1}}{\Gamma(m)} \exp\left(\frac{-m\gamma_{RF}}{\bar{\gamma}_{RF}}\right), \quad \gamma_{RF} \geq 0, \quad (4.4)$$

where  $\bar{\gamma}_{RF}$  is the average SNR of the  $i$ th channel with  $1 \leq i \leq L$ , and  $m$  is a parameter indicating fading severity.  $\bar{\gamma}_{RF}$  and  $m$  are assumed to be common on all the  $L$  diversity branches. The overall received SNR of the RF link  $\gamma_{RF}$  will be that after the MRC combination of all the  $L$  RF channels, such that  $\gamma_{RF} = \sum_{i=1}^L \gamma_{i_{RF}}$ , the PDF of which is given by: [67]

$$f_{\gamma_{RF}}(\gamma_{RF}) = \left(\frac{m}{\bar{\gamma}_{RF}}\right)^{mL} \frac{\gamma_{RF}^{mL-1}}{\Gamma(mL)} \exp\left(\frac{-m\gamma_{RF}}{\bar{\gamma}_{RF}}\right), \quad \gamma_{RF} \geq 0. \quad (4.5)$$

By using [53, Eq. (3.351.1)], and some simple algebraic manipulations, the CDF of  $\gamma_{RF}$  can be expressed as:

$$F_{\gamma_{RF}}(\gamma_{RF}) = \frac{1}{\Gamma(mL)} \gamma \left(mL, \frac{m\gamma_{RF}}{\bar{\gamma}_{RF}}\right), \quad \gamma_{RF} \geq 0, \quad (4.6)$$

where  $\gamma(\cdot, \cdot)$  is the lower incomplete Gamma function defined in [53, Eq. (8.350.1)].

## 4.2 Power Allocation Strategies and Outage Analysis

We assume constant FSO transmitting power all the time. When  $\gamma_{FSO} < \gamma_T$ , the RF link is activated along with the FSO link and the RF link transmitted power  $P_{RF}$  is adapted to maintain the required constant received SNR  $\gamma_T$ . We introduce here two different policies for RF link power adaptation. Both of them are based on the TCI principle [32].

### 4.2.1 TCI For RF Link Based on $\gamma_{RF}$

#### Power Adaptation Policy

In this power adaptation policy, the transmitter uses the CSI (specifically,  $\gamma_{FSO}$  and  $\gamma_{RF}$ ) to maintain the target received SNR  $\gamma_T$ . Since the power adaptation is performed after activating the RF link, the RF link SNR is adaptively changed to fill the gap between  $\gamma_{FSO}$  and  $\gamma_T$  such that  $\gamma_{RF} + \gamma_{FSO} = \gamma_T$ . The RF power is adapted as long as the received RF SNR is above a certain threshold denoted by  $\gamma_{0_I}$ . Otherwise, data transmission is suspended. We will refer to this policy as  $\gamma_{RF}$ -based TCI which is mathematically given by:

$$\frac{P_{RF}(\gamma_{RF}, \gamma_{FSO})}{\bar{P}_{RF}} = \begin{cases} \frac{\gamma_T - \gamma_{FSO}}{\gamma_{RF}}, & \text{if } \gamma_{RF} \geq \gamma_{0_I} \\ 0, & \text{if } \gamma_{RF} < \gamma_{0_I}, \end{cases} \quad (4.7)$$

where  $\gamma_{0_I}$  satisfies the average power constraint of RF link transmitter given by:

$$\int_0^{\gamma_T} \int_{\gamma_{0_I}}^{\infty} \frac{P_{RF}(\gamma_{RF}, \gamma_{FSO})}{\bar{P}_{RF}} f_{\gamma_{RF}}(\gamma_{RF}) f_{\gamma_{FSO}}(\gamma_{FSO}) d\gamma_{RF} d\gamma_{FSO} = 1, \quad (4.8)$$

where  $\bar{P}_{RF}$  is the average transmitted power over the RF link.

By substituting (4.2) and (4.5) in (4.8), and using [53, Eq. (3.381.9)] and [56, Eq. (07.34.21.0084.01)], the constraint in (4.8) can be expressed as:

$$A_1 \Gamma\left(mL - 1, \frac{m\gamma_{0_I}}{\bar{\gamma}_{RF}}\right) \left\{ G_{r+1, 3r+1}^{3r, 1} \left[ \frac{B\gamma_T}{\bar{\gamma}_{FSO_r}} \middle|_{K_2, 0}^{1, K_1} \right] - G_{r+1, 3r+1}^{3r, 1} \left[ \frac{B\gamma_T}{\bar{\gamma}_{FSO_r}} \middle|_{K_2, -1}^{0, K_1} \right] \right\} = 1, \quad (4.9)$$

where  $A_1 = \xi^2 r^{\alpha+\beta-2} m \gamma_T / (2\pi)^{r-1} \bar{\gamma}_{RF} \Gamma(\alpha) \Gamma(\beta) \Gamma(mL)$ , and  $\Gamma(\cdot, \cdot)$  is the upper incomplete Gamma function defined in [53, Eq. (8.350.2)]. As with most TCI schemes, the value for  $\gamma_{0_I}$  that satisfies (4.9) can be found using numerical methods, such as bisection method and Newton method [68].

#### Outage Probability For $\gamma_{RF}$ -based TCI

According to this policy, the hybrid system goes into outage state if the RF link received SNR  $\gamma_{RF}$  goes below  $\gamma_{0_I}$ . The probability of outage in this case can be

calculated as:

$$\begin{aligned} P_{out} &= \Pr[\gamma_{FSO} < \gamma_T] \Pr[\gamma_{RF} < \gamma_{0I}]. \\ &= F_{\gamma_{FSO}}(\gamma_T) F_{\gamma_{RF}}(\gamma_{0I}), \end{aligned} \quad (4.10)$$

where  $F_{\gamma_{FSO}}(\cdot)$  and  $F_{\gamma_{RF}}(\cdot)$  are given by (4.3) and (4.6), respectively.

## 4.2.2 TCI For RF Link Based on $\gamma_{RF} + \gamma_{FSO}$

### Power Adaptation Policy

This RF link power adaptation policy is similar to the first one. However, the RF power is adapted as long as the overall SNR after MRC combination of the RF link and the FSO link (i.e.,  $\gamma_{RF} + \gamma_{FSO}$ ) is above a certain threshold denoted by  $\gamma_{0II}$ . Otherwise, data transmission is suspended. We will refer to this policy as  $\gamma_{RF} + \gamma_{FSO}$ -based TCI which is given by:

$$\frac{P_{RF}(\gamma_{RF}, \gamma_{FSO})}{\bar{P}_{RF}} = \begin{cases} \frac{\gamma_T - \gamma_{FSO}}{\gamma_{RF}}, & \text{if } \gamma_{RF} + \gamma_{FSO} \geq \gamma_{0II} \\ 0, & \text{if } \gamma_{RF} + \gamma_{FSO} < \gamma_{0II}, \end{cases} \quad (4.11)$$

where  $\gamma_{0II}$  satisfies the average power constraint over the RF link given by:

$$\int_0^{\gamma_T} \int_{\gamma_{0II} - \gamma_{FSO}}^{\infty} \frac{P_{RF}(\gamma_{RF}, \gamma_{FSO})}{\bar{P}_{RF}} f_{\gamma_{RF}}(\gamma_{RF}) f_{\gamma_{FSO}}(\gamma_{FSO}) d\gamma_{RF} d\gamma_{FSO} = 1. \quad (4.12)$$

By substituting (4.2) and (4.5) in (4.12), and using the binomial expansion defined in [53, Eq. (1.111)] and the series expansion of the exponential defined in [53, Eq. (1.211.1)], along with [53, Eq. (3.351.2)] and [56, Eq. (07.34.21.0084.01)], the constraint in (4.12) can be expressed as:

$$\begin{aligned} A_2 e^{\frac{-m\gamma_{0II}}{\bar{\gamma}_{RF}}} \sum_{n=0}^{\infty} \frac{(m\gamma_T/\bar{\gamma}_{RF})^n}{n!} \sum_{i=0}^{mL-2} \frac{(m\gamma_{0II}/\bar{\gamma}_{RF})^i}{i!} \sum_{k=0}^i \binom{i}{k} \left(\frac{-\gamma_T}{\gamma_{0II}}\right)^k \left\{ \right. \\ \left. G_{r+1,3r+1}^{3r,1} \left[ \frac{B\gamma_T}{\bar{\gamma}_{FSO_r}} \middle|_{K_2, -n-k}^{1-n-k, K_1} \right] - G_{r+1,3r+1}^{3r,1} \left[ \frac{B\gamma_T}{\bar{\gamma}_{FSO_r}} \middle|_{K_2, -n-k-1}^{-n-k, K_1} \right] \right\} = 1, \end{aligned} \quad (4.13)$$

where  $A_2 = \xi^2 r^{\alpha+\beta-2} m(mL-2)! \gamma_T / (2\pi)^{r-1} \Gamma(\alpha) \Gamma(\beta) \Gamma(mL) \bar{\gamma}_{RF}$ . Similar to  $\gamma_{0I}$ , the value for  $\gamma_{0II}$  that satisfies (4.13) can be found using numerical methods. When

using (4.13) to search for the value of  $\gamma_{0_{II}}$ , it is sufficient to use  $n = 40$  to obtain stable values with accuracy to the fourth digit. This can be observed from Table 4.1 and Table 4.2, where we consider  $\gamma_T=10$  dB, typical values of  $\alpha$  and  $\beta$  for weak atmospheric turbulence regime ( $\alpha=2.902$ , and  $\beta=2.51$ ) [60],  $\bar{\gamma}_{FSO_r}=0$  dB,  $\xi = 1$ , Nakagami parameter  $m=2$ , and  $L=1$  to obtain the values of  $\gamma_{0_{II}}$  for different values of  $\bar{\gamma}_{RF}$ .

Table 4.1: Values of  $\gamma_{0_{II}}$  considering CM/HD ( $r=1$ ) with different values of  $n$

$\bar{\gamma}_{RF}$ (dB)	$n = 30$	$n = 35$	$n = 40$	$n = 45$
0	6.2125	6.2142	6.2142	6.2142
1	5.5250	5.5250	5.5251	5.5251
8	4.3291	4.3291	4.3291	4.3291
12	1.9091	1.9091	1.9091	1.9091

Table 4.2: Values of  $\gamma_{0_{II}}$  considering IM/DD ( $r=2$ ) with different values of  $n$

$\bar{\gamma}_{RF}$ (dB)	$n = 30$	$n = 35$	$n = 40$	$n = 45$
0	7.2243	7.2264	7.2265	7.2265
4	4.9315	4.9315	4.9315	4.9315
10	3.5144	3.5144	3.5144	3.5144
12	1.2882	1.2882	1.2882	1.2882

### Outage Probability for $\gamma_{RF} + \gamma_{FSO}$ -based TCI

According to this policy, the hybrid system goes into outage state if MRC combination of the FSO and RF links failed to support a received SNR of  $\gamma_{RF} + \gamma_{FSO} \geq \gamma_{0_{II}}$ . The

probability of outage in this case can be calculated as:

$$\begin{aligned}
P_{out} &= P_r[\gamma_{FSO} < \gamma_T, \gamma_{FSO} + \gamma_{RF} < \gamma_{0II}]. \\
&= \int_0^{\gamma_{0II}} \int_0^{\min[\gamma_T, \gamma_{0II} - \gamma_{RF}]} f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(\gamma_{RF}) d\gamma_{FSO} d\gamma_{RF} \\
&= \int_0^{\gamma_{0II} - \gamma_T} \int_0^{\gamma_T} f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(\gamma_{RF}) d\gamma_{FSO} d\gamma_{RF} \\
&\quad + \int_{\gamma_{0II} - \gamma_T}^{\gamma_{0II}} \int_0^{\gamma_{0II} - \gamma_{RF}} f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(\gamma_{RF}) d\gamma_{FSO} d\gamma_{RF}.
\end{aligned} \tag{4.14}$$

If  $\gamma_T > \gamma_{0II}$ , which is the case most of the time, then (4.14) will be given by:

$$\begin{aligned}
P_{out} &= \int_0^{\gamma_{0II}} \int_0^{\gamma_{0II} - \gamma_{RF}} f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(\gamma_{RF}) d\gamma_{FSO} d\gamma_{RF}. \\
&= \int_0^{\gamma_{0II}} f_{\gamma_{RF}}(\gamma_{RF}) F_{\gamma_{FSO}}(\gamma_{0II} - \gamma_{RF}) d\gamma_{RF}.
\end{aligned} \tag{4.15}$$

By substituting (4.3) and (4.5) in (4.15), making change of variable, and using the series expansion of the exponential, along with [56, Eq. (07.34.21.0084.01)], (4.15) can be evaluated as:

$$P_{out} = \frac{\xi^2 r^{\alpha + \beta - 2} e^{-\frac{m\gamma_{0II}}{\bar{\gamma}_{RF}}} \left(\frac{m\gamma_{0II}}{\bar{\gamma}_{RF}}\right)^{mL}}{(2\pi)^{r-1} \Gamma(\alpha) \Gamma(\beta)} \sum_{n=0}^{\infty} \left\{ \frac{\left(\frac{m\gamma_{0II}}{\bar{\gamma}_{RF}}\right)^n}{n!} G_{r+2, 3r+2}^{3r, 2} \left[ \frac{B\gamma_{0II}}{\bar{\gamma}_{FSO_r}} \middle| \begin{matrix} -n, 1, K_1 \\ K_2, 0, -n-mL \end{matrix} \right] \right\}. \tag{4.16}$$

### 4.2.3 Outage Capacity

Practically speaking, outage capacity applies to slowly-varying channels [32], which is the case with FSO and MMW RF channels with bit-duration much smaller than the channels coherence time [17, 28]. The outage capacity is defined as the maximum data rate that can be maintained in all non-outage channel states times the probability

of non-outage. The outage capacity associated with a given outage probability  $P_{out}$  normalized to the communication channel bandwidth  $B$  can be expressed as [69]:

$$\frac{C(P_{out})}{B} = [1 - P_{out}] \log_2(1 + K\gamma_T), \quad (4.17)$$

where  $K$  is a constant term such that  $K = 1$  for heterodyne detection giving an exact result and  $K = e/(2\pi)$  for IM/DD giving a lower-bound result. The outage probability  $P_{out}$  in (4.17) is given by either (4.10) or (4.16) according to the power adaptation policy used on the RF link.

### 4.3 Hybrid FSO/RF System with Adaptive Combining Only

In this section, we analyze the outage probability of the hybrid FSO/RF system without power adaptation. We assume that the outage threshold denoted by  $\gamma_{out}$  is smaller than the switching threshold  $\gamma_T$ . Otherwise, the hybrid system will enter outage before activating RF link. When the FSO link SNR  $\gamma_{FSO}$  falls below  $\gamma_T$ , and the instantaneous receiver SNR  $\gamma_c = \gamma_{FSO} + \gamma_{RF}$  falls below the outage threshold  $\gamma_{out}$ , the communication link can not support a target BER and goes into outage state. In this case, the outage probability of the hybrid FSO/RF system without power adaptation can be calculated as:

$$\begin{aligned} P_{out} &= P_r[\gamma_{FSO} < \gamma_T, \gamma_{FSO} + \gamma_{RF} < \gamma_{out}] \\ &= \int_0^{\gamma_{out}} f_{\gamma_{FSO} + \gamma_{RF}}(y) dy. \end{aligned} \quad (4.18)$$

Noting that the FSO and RF links are statistically independent,  $f_{\gamma_{FSO} + \gamma_{RF}}(y)$  in (4.18) can be evaluated as:

$$f_{\gamma_{FSO} + \gamma_{RF}}(y) = \int_0^y f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(y - \gamma_{FSO}) d\gamma_{FSO}, \quad (4.19)$$

where  $f_{\gamma_{FSO}}(\cdot)$  and  $f_{\gamma_{RF}}(\cdot)$  are given by (4.2) and (4.5), respectively. Finally,

$$P_{out} = \int_0^{\gamma_{out}} \int_0^y f_{\gamma_{FSO}}(\gamma_{FSO}) f_{\gamma_{RF}}(y - \gamma_{FSO}) d\gamma_{FSO} dy, \quad (4.20)$$

which can be numerically evaluated.

## 4.4 Numerical results

In this section we present several numerical examples to investigate the performance of the two proposed power adaptation strategies. Note that in all numerical results, we assume using optical wavelength  $\lambda_{FSO} = 1550$  nm [70]. Also, note that for the numerical results shown in Figs. 4.2, 4.4, and 4.5 we assume no RF diversity, i.e.,  $L = 1$ .

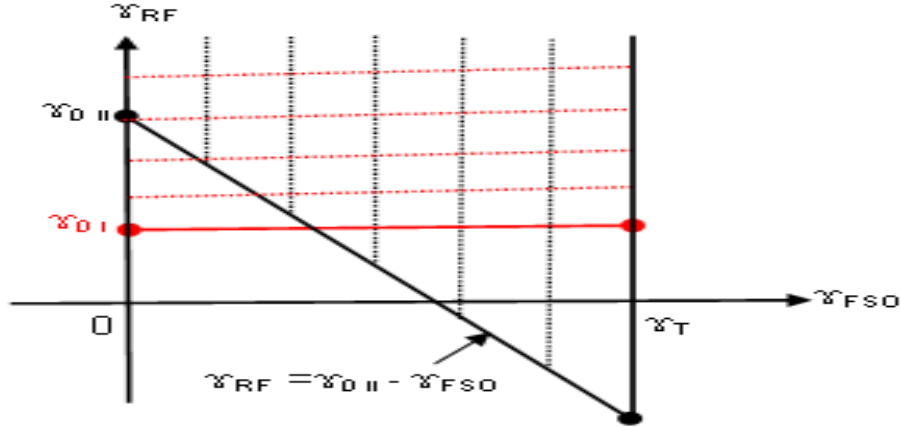


Figure 4.1: Integration regions of Eqs. (4.8) and (4.12).

In Fig. 4.2, we plot the outage probability of the hybrid system with and without power adaptation as a function of the average RF link SNR  $\bar{\gamma}_{RF}$ . We assume weak atmospheric turbulence ( $\alpha=2.902$ , and  $\beta=2.51$ ) affecting the FSO link with pointing error effect of  $\xi = 1$ , and RF link fading severity of  $m = 2$ . It can be seen from Fig. 4.2 that considering either CM/HD technique (Fig. 4.2a) or IM/DD technique (Fig. 4.2b), using the  $\gamma_{RF}$ -based TCI adaptation policy gives better outage performance than using the  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation policy. This is because that under the same conditions of the FSO and RF links,  $\gamma_{0I}$  is less than  $\gamma_{0II}$ . To explain this, let  $f(\gamma_{RF}, \gamma_{FSO}) = \frac{P_{RF}(\gamma_{RF}, \gamma_{FSO})}{\bar{P}_{RF}} f_{\gamma_{RF}}(\gamma_{RF}) f_{\gamma_{FSO}}(\gamma_{FSO})$ . We need the integration of

$f(\gamma_{RF}, \gamma_{FSO})$  over the red shaded area in Fig. 4.1 to be equal to 1, according to (4.8), and also we need the integration of  $f(\gamma_{RF}, \gamma_{FSO})$  over the black shaded area in Fig. 4.1 to be equal to 1, according to (4.12). If we assume that  $\gamma_{0_I}$  is greater than or equal to  $\gamma_{0_{II}}$ , then the integration of  $f(\gamma_{RF}, \gamma_{FSO})$  over the red shaded area will be greater than 1 which is impossible according to the constraint in (4.8). Thus,  $\gamma_{0_I}$  is less than  $\gamma_{0_{II}}$ . The analytical results for the outage probability of the hybrid system with  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation policy shown in Fig. 4.2 are obtained using  $n=30$  in (4.16). As can be observed, evaluating the outage probability with the truncated values of  $n=30$  gives accurate results as compared with the values obtained by evaluating the integral in (4.15) using numerical methods. It can also be seen from Fig. 4.2, that applying power adaptation (either  $\gamma_{RF}$ -based TCI or  $\gamma_{RF} + \gamma_{FSO}$ -based TCI) policy greatly improves the outage performance of the hybrid system over the case without using power adaptation. Note that we had used numerical integration to evaluate the outage probability for the hybrid system without power adaptation, given in (4.20), with outage threshold  $\gamma_{out}=9.5$  dB. Note also that the value  $\gamma_{out}=9.5$  dB is less than  $\gamma_T=10$  dB so that the hybrid system switches to the MRC combination of the FSO and RF links before the FSO link alone goes in outage.

In Fig. 4.3, we examine the effect of the RF link diversity on the outage performance of the hybrid FSO/RF system with both power adaptation policies (Fig. 4.3a and Fig. 4.3b). It can be seen from Fig. 4.3, that as the number of the RF branches increases, the outage performance of the hybrid system greatly improves. Intuitively, the same observation shown in Fig. 4.3 is also applicable when using CM/HD technique.

In Fig. 4.4, we examine the outage performance of the proposed hybrid FSO/RF system in the presence of strong atmospheric turbulence ( $\alpha=2.064$ , and  $\beta=1.342$ ) affecting the FSO link with less severe pointing error effect of  $\xi = 4$ , and RF link fading severity of  $m = 2$ . It can be seen from Fig. 4.4, that the hybrid FSO/RF system employing either of the two proposed power adaptation policies achieves superior outage performance compared to the performance of the system without power adaptation in this case also.

In Fig. 4.5, we plot the outage capacity of the hybrid system with power adaptation as a function of the average RF link SNR  $\bar{\gamma}_{RF}$ . We assume weak atmospheric turbulence ( $\alpha=2.902$ , and  $\beta=2.51$ ) affecting the FSO link with pointing error effect of  $\xi = 1$ , and RF link fading severity of  $m = 2$ . It can be seen from Fig. 4.5 that considering either CM/HD technique (Fig. 4.5a) or IM/DD technique (Fig. 4.5b),

using  $\gamma_{RF}$ -based TCI adaptation policy leads to higher outage capacity than using  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation policy. This is because using  $\gamma_{RF}$ -based TCI adaptation policy achieves smaller outage probability than  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation policy. However, when  $\bar{\gamma}_{RF}$  becomes high, the outage capacity obtained when using  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation policy becomes the same as that obtained when using  $\gamma_{RF}$ -based TCI adaptation policy. This is because both  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation policy and  $\gamma_{RF}$ -based TCI adaptation policy achieve almost the same outage probability with high values of  $\bar{\gamma}_{RF}$ .

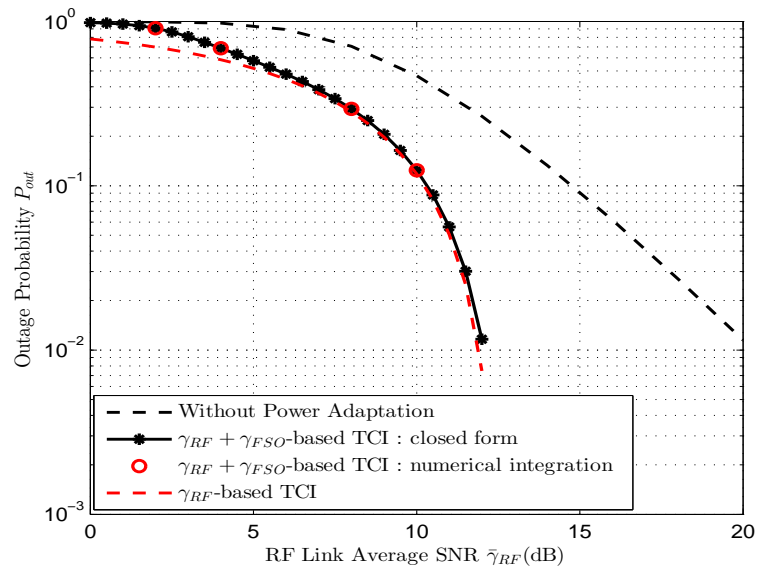
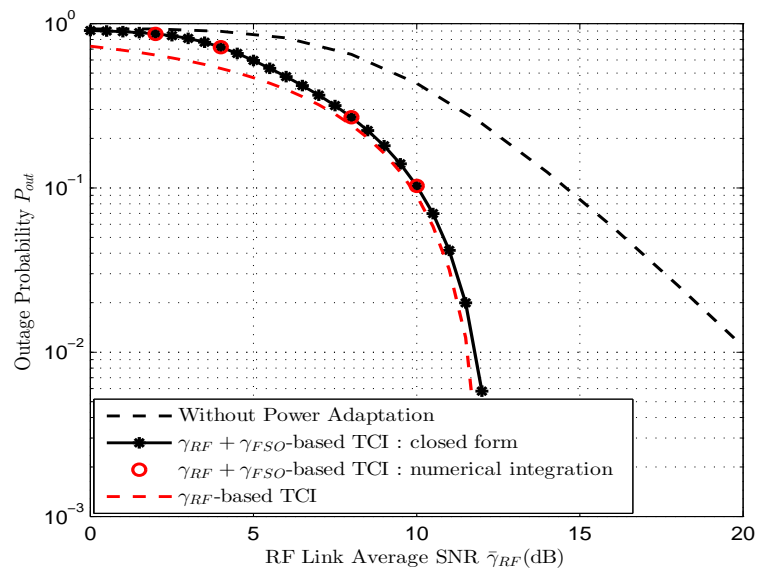
(a) Using CM/HD technique with FSO link ( $r=1$ )(b) Using IM/DD technique with FSO link ( $r=2$ )

Figure 4.2: Outage probability of hybrid FSO/RF system with and without power adaptation as a function of the average SNR of the RF link with  $\gamma_T=10$  dB, Nakagami parameter  $m=2$ , weak atmospheric turbulence ( $\alpha=2.902$ , and  $\beta=2.51$ ),  $\bar{\gamma}_{FSO_r}=0$  dB, and  $\xi = 1$ .

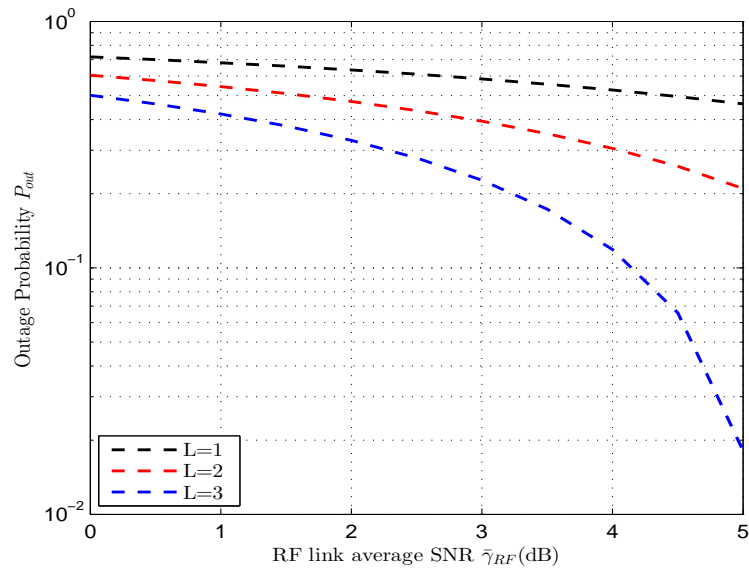
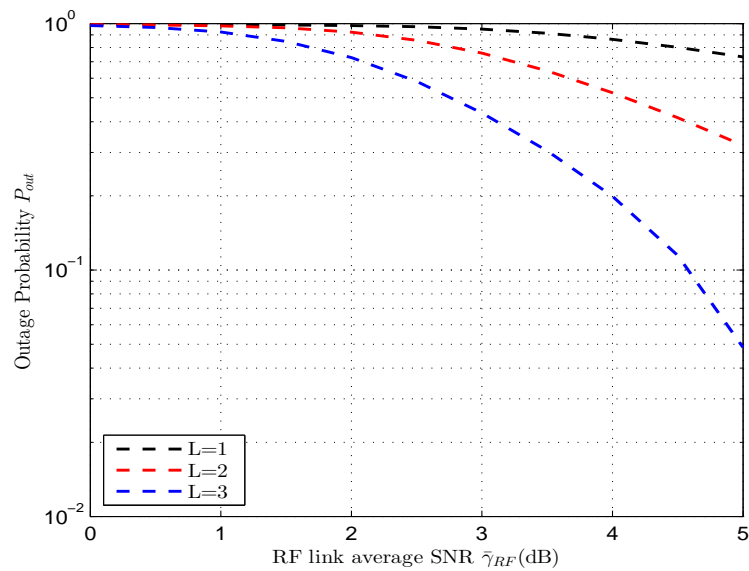
(a) Using  $\gamma_{RF}$ -Based TCI(b) Using  $\gamma_{RF} + \gamma_{FSO}$ -Based TCI

Figure 4.3: Outage probability of hybrid FSO/RF system with power adaptation as a function of the average SNR of the RF link considering IM/DD FSO detection technique, with  $\gamma_T=10$  dB, Nakagami parameter  $m=2$ , weak atmospheric turbulence ( $\alpha=2.902$ , and  $\beta=2.51$ ),  $\bar{\gamma}_{FSO_2}=0$  dB, and  $\xi = 1$ .

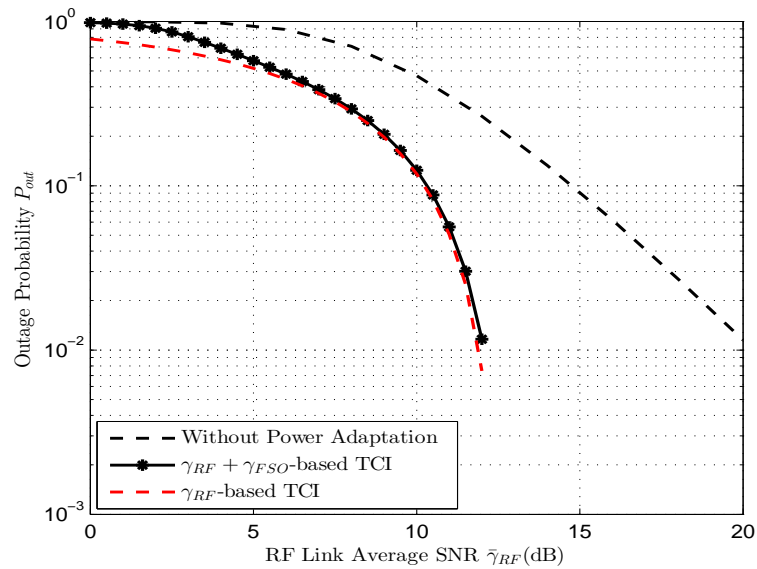
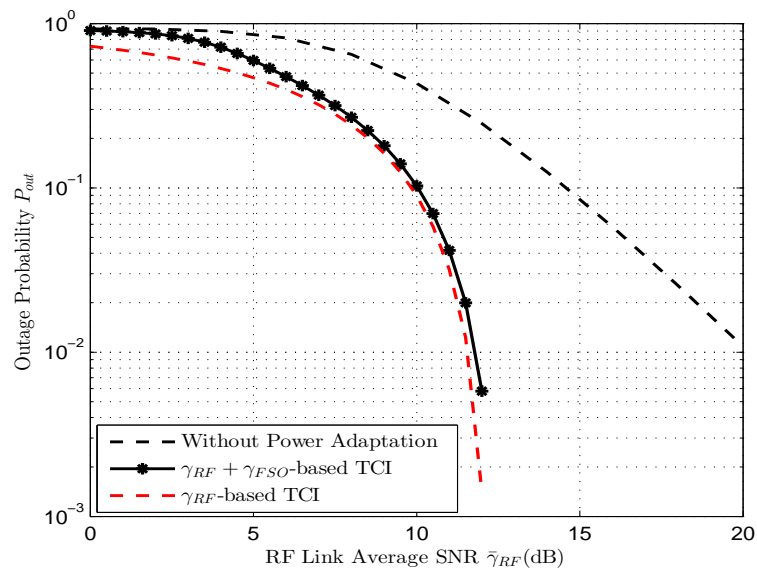
(a) Using CM/HD technique with FSO link ( $r=1$ )(b) Using IM/DD technique with FSO link ( $r=2$ )

Figure 4.4: Outage probability of hybrid FSO/RF system with and without power adaptation as a function of the average SNR of the RF link with  $\gamma_T=10$  dB, Nakagami parameter  $m=2$ , strong atmospheric turbulence ( $\alpha=2.064$ , and  $\beta=1.342$ ),  $\bar{\gamma}_{FSO_r}=0$  dB, and  $\xi = 4$ .

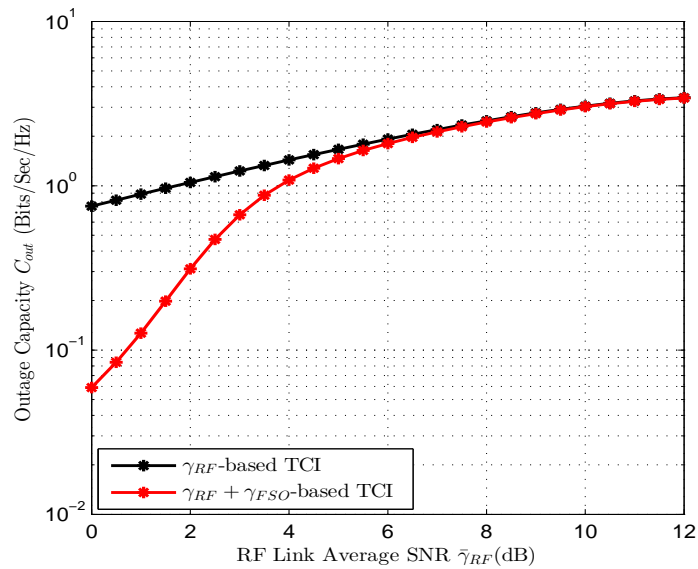
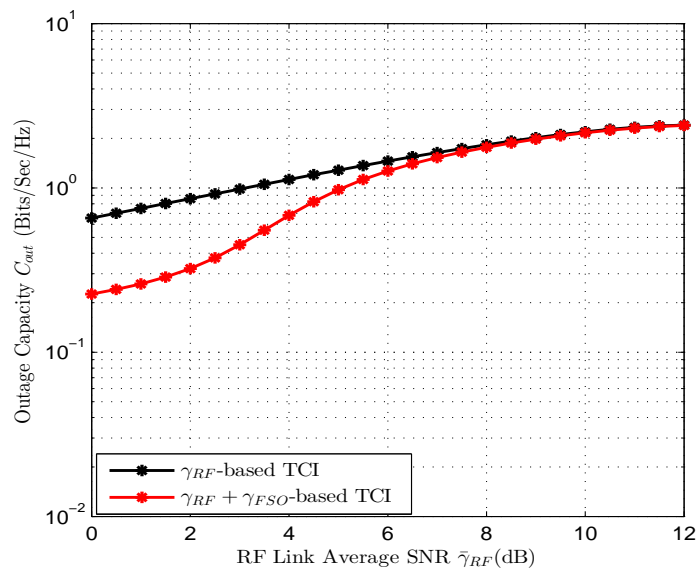
(a) Using CM/HD technique with FSO link ( $r=1$ )(b) Using IM/DD technique with FSO link ( $r=2$ )

Figure 4.5: Outage capacity of hybrid FSO/RF system with power adaptation as a function of the average SNR of the RF link with  $\gamma_T=10$  dB, Nakagami parameter  $m=2$ , weak atmospheric turbulence ( $\alpha=2.902$ , and  $\beta=2.51$ ),  $\bar{\gamma}_{FSO_r}=0$  dB, and  $\xi = 1$ .

## 4.5 Power Adaptation on FSO Link

To conserve more power, the transmit power over the FSO link can be adapted according to the following modified TCI policy:

$$\frac{P_{FSO}(\gamma_{FSO})}{P_{FSOmax}} = \begin{cases} \frac{\gamma_T}{\gamma_{FSO}}, & \text{if } \gamma_{FSO} \geq \gamma_T \\ 1, & \text{if } \gamma_{FSO} < \gamma_T. \end{cases} \quad (4.21)$$

According to this power adaptation policy, FSO power denoted by  $P_{FSO}$  gradually increases when the FSO link is in good quality (i.e.,  $\gamma_{FSO} \geq \gamma_T$ ) to reach its maximum value of  $P_{FSOmax}$  when the FSO link quality is bad (i.e.,  $\gamma_{FSO} < \gamma_T$ ). In other words, we use constant FSO power of  $P_{FSOmax}$  when  $\gamma_{FSO} < \gamma_T$ . Thus, this additional power adaptation for FSO link can further improve the power efficiency of the hybrid FSO/RF system, while maintaining the same outage performance of the system.

## 4.6 Summery

In this chapter, we introduced low complexity power adaptation strategy to hybrid FSO/RF systems with adaptive combining. Two power adaptation policies based on a modified TCI were implemented on the RF link of the hybrid system. We analyzed the outage performance of the proposed adaptive system and closed forms for the outage probabilities were derived. Numerical results showed that the hybrid system with power adaptation had superior outage performance compared to outage performance of the same system without power adaptation, while conserving RF power. Also, numerical results showed that  $\gamma_{RF}$ -based TCI adaptation policy achieves better outage performance than  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation policy.

## Chapter 5

# Cross Layer Analysis of Point-to-Multi-Point Hybrid FSO/RF Network

In this chapter, we consider a P2MP hybrid FSO/RF data transmission network, which consists of a number of remote nodes along with a central node. Each remote node in the network is connected to the central node via a primary FSO link. A common backup RF link is shared among all the remote nodes, where we adopt the simple switch-over hybrid FSO/RF approach. Using a common RF channel will have the major advantages of: 1) sharing the scarce RF spectrum, 2) preventing the generation of unnecessary RF interference to the environment, and 3) conserving the RF power. We study the performance of a single remote node (tagged node) rather than studying the overall system performance. Studying the tagged node allow us to investigate several performance criteria such as throughput from central node to the tagged node, the average transmit buffer size, the symbol queuing delay in the transmit buffer, the efficiency of the queuing system, the symbol loss probability, and the RF link utilization.

The remainder of the chapter is organized as follows. In section 5.1, we introduce the P2MP Hybrid FSO/RF network model and central node - remote node channel model. In section 5.2, we introduce the steady state system performance model. We study different performance metrics for the tagged node in section 5.3. Finally, section 5.4 presents some numerical examples to investigate the performance of the proposed P2MP network, followed by the chapter summary in section 5.5.

## 5.1 P2MP Network and Channel modeling

### 5.1.1 P2MP Hybrid FSO/RF Network Modeling

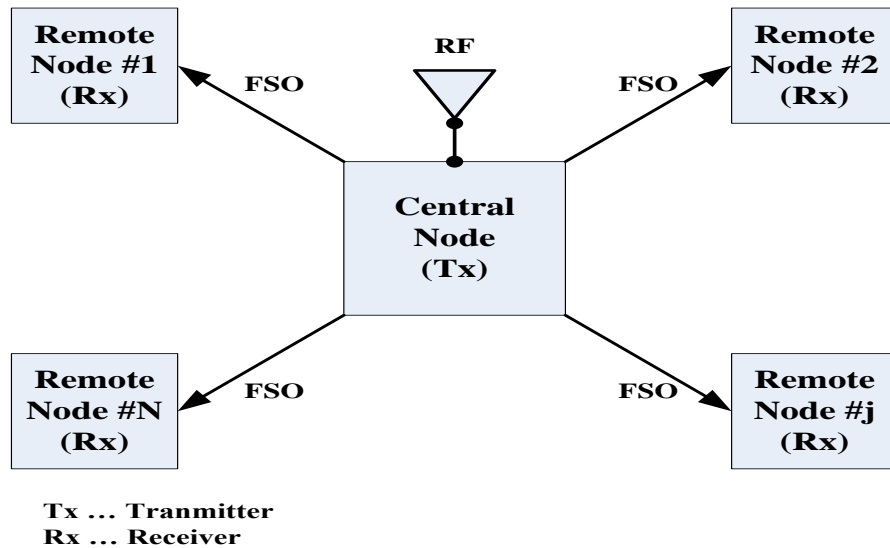


Figure 5.1: General block diagram of a P2MP Hybrid FSO/RF network.

The general block diagram of a P2MP hybrid FSO/RF network is shown in Fig. 5.1. This network consists of a central node and  $N$  remote nodes. The central node is equipped with  $N$  optical transmitters and one RF transmitter. Each remote node in the network is equipped with one optical receiver and one RF receiver. Each remote node of the network is connected to the central node through a separate primary FSO link. The central node is assumed to be aware of the quality of the  $N$  FSO links through  $N$  feedback channels. The RF transmitter of the central node is assigned a certain RF channel, which is used as a backup channel for data transmission to any remote node in case of the failure of its corresponding FSO link.

Through out the chapter, we will adopt the following assumptions:

1. When more than one FSO link fail, the central node will use the RF link to communicate with one of the corresponding remote nodes on an equal priority basis.
2. Non-saturated traffic condition is assumed. Specifically, the central node may or may not have data symbols for transmission to all  $N$  remote nodes over each time step.

3. All FSO links follow the same statistical fading distribution.
4. The data is transmitted over the FSO and RF links at the same rate.
5. No error control policy is implemented between the remote node and the central node.
6. The central node receives perfectly the states of the  $N$  FSO channels and the back-up RF channel based on feedback from the remote nodes.

The hybrid FSO/RF system used for data transmission from the central node to any remote node is composed of coherent/heterodyne FSO and RF data transmission subsystems. In this hybrid system, coded digital baseband signal, created by the signal source, is converted to an analog electrical signal through  $M$ -QAM electrical modulator.  $M$ -QAM is widely used in high-rate data transmissions over FSO links [61], and RF links [62], because of its high spectral efficiency, and low signal modulation/demodulation complexity. The QAM signal will be transmitted using either the FSO link or the RF link. At the FSO transmitter, QAM electrical signal is mixed with an optical carrier, produced by an optical frequency LO to produce the optical signal. At the FSO receiver, the received optical signal undergoes heterodyne detection process. At the RF transmitter, the frequency of the QAM electrical signal is up-converted using 60 GHz RF carrier, produced by an RF LO.

For the data transmission from the central node to any remote node, we adopt a switch-over hybrid FSO/RF transmission scheme. In this transmission scheme, only the FSO link is used for data transmission as long as the instantaneous SNR at the optical receiver of the remote node, denoted by  $\gamma_{FSO}$ , is above a certain threshold, defined by  $\gamma_T$ . When  $\gamma_{FSO}$  falls below the predetermined threshold  $\gamma_T$ , the remote node sends a 1-bit feedback signal to inform the central node to use the RF link<sup>1</sup> for data transmission. To meet a minimum BER requirement of  $BER_0$ , the threshold  $\gamma_T$  is set as [32]:

$$\gamma_T = (M - 1) \left[ -\frac{2}{3} \ln(5 BER_0) \right], \quad M \geq 4 \quad (5.1)$$

---

<sup>1</sup>Note that the remote node is not aware whether or not the RF link is being used by the central node to transmit data to another remote node.

## 5.1.2 Central node - Remote node Channel Modeling

### Modeling the FSO Link

The instantaneous SNR per symbol of the FSO receiver is given by [63, 64]:

$$\gamma_{FSO} = \bar{\gamma}_{FSO} h_{FSO}, \quad (5.2)$$

where  $\bar{\gamma}_{FSO}$  and  $h_{FSO}$  are respectively, the average SNR and the fading gain over the FSO link, with  $E[h_{FSO}]$  is normalized to unity, where  $E[.]$  is the expectation operator. Assume using PLL to compensate for phase noise in the received optical signal and using large enough LO power, such that thermal and background noises can be neglected, then average SNR  $\bar{\gamma}_{FSO}$  can be given by [63, 64]:

$$\bar{\gamma}_{FSO} = \frac{2E_{avg}\eta^2 P_{LO} P_{FSO} G_{FSO}}{\sigma_{FSO}^2}, \quad (5.3)$$

where  $E_{avg}$ ,  $\eta$ ,  $P_{LO}$ ,  $P_{FSO}$ ,  $G_{FSO}$ , and  $\sigma_{FSO}^2$  are respectively, the average QAM symbol energy, photodetector responsivity, LO power, average transmitted optical power, attenuation factor, and variance of shot noise which is modeled as AWGN. The attenuation factor  $G_{FSO}$  (in dB) is determined by the Beers-Lambert law as  $G_{FSO} = \alpha_{FSO} z$  [26], where  $\alpha_{FSO}$  denotes the weather attenuation coefficient (in dB/Km) and  $z$  is the link distance. The fading gain over the FSO link is defined as  $h_{FSO} = h_a h_p$  [65], where  $h_a$  is Gamma-Gamma atmospheric turbulence-induced fading gain factor [54] and  $h_p$  is Gaussian pointing errors-induced fading gain factor [17].

Following the same procedure used in [65], it is easy to show that the PDF of  $\gamma_{FSO}$  is given by:

$$f_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{\xi^2 \gamma_{FSO}^{-1}}{\Gamma(\alpha)\Gamma(\beta)} G_{1,3}^{3,0} \left[ \frac{\xi^2 \alpha \beta \gamma_{FSO}}{(\xi^2 + 1) \bar{\gamma}_{FSO}} \middle| \begin{matrix} \xi^2 + 1 \\ \xi^2, \alpha, \beta \end{matrix} \right], \quad (5.4)$$

where  $\xi$  is the ratio between the equivalent beam radius and the pointing error (jitter) standard deviation  $\sigma_s$  given by  $\xi = \omega_{eq}/2\sigma_s$  [17]. Here,  $\omega_{eq}^2 = \omega_z^2 \sqrt{\pi} \text{erf}(\nu)/2\nu \exp(-\nu^2)$ , where  $\text{erf}(\cdot)$  is the error function and  $\omega_z$  is the optical beam radius at distance  $z$  from the transmitter aperture and  $\nu = \sqrt{\pi} D/2\sqrt{2}\omega_z$  with  $D$  is the photodetector diameter.  $\omega_z$  is given by  $\omega_z = \theta_0 z$ , where  $\theta_0$  is the transmit divergence at  $1/e^2$ .  $\Gamma(\cdot)$  and  $G[.]$  in (5.4) are respectively, the standard Gamma function and the Meijer G-function

as defined in [53, Eq. (9.301)] with  $\alpha$  and  $\beta$  are the scintillation parameters. The parameters  $\alpha$  and  $\beta$  are related to the refractive index structure parameter  $C_n^2$  where the atmospheric turbulence can be modeled from weak to strong turbulence regimes. Assuming spherical optical wave propagation, expressions for calculating  $\alpha$  and  $\beta$  in (5.4) are given by [54]:

$$\alpha = \left[ \exp \left( \frac{0.49\chi^2}{(1 + 0.18d^2 + 0.56\chi^{12/5})^{7/6}} \right) - 1 \right]^{-1} \quad (5.5)$$

$$\beta = \left[ \exp \left( \frac{0.51\chi^2(1 + 0.69\chi^{12/5})^{-5/6}}{(1 + 0.9d^2 + 0.62d^2\chi^{12/5})^{5/6}} \right) - 1 \right]^{-1}, \quad (5.6)$$

where  $\chi^2 = 0.5C_n^2k^{7/6}z^{11/6}$  is the Rytov variance,  $d = (kD^2/4z)^{1/2}$ , and  $k = 2\pi/\lambda_{FSO}$  is the optical wave number with  $\lambda_{FSO}$  is the optical wavelength.

By using [56, Eq. (07.34.21.0084.01)] and some simple algebraic manipulations, the CDF of  $\gamma_{FSO}$  can be expressed as:

$$F_{\gamma_{FSO}}(\gamma_{FSO}) = \frac{\xi^2}{\Gamma(\alpha)\Gamma(\beta)} G_{2,4}^{3,1} \left[ \frac{\xi^2\alpha\beta\gamma_{FSO}}{(\xi^2 + 1)\bar{\gamma}_{FSO}} \middle| \begin{matrix} 1, \xi^2+1 \\ \xi^2, \alpha, \beta, 0 \end{matrix} \right]. \quad (5.7)$$

## Modeling the RF Link

The instantaneous SNR per symbol of the RF receiver is given by  $\gamma_{RF} = \bar{\gamma}_{RF}h_{RF}^2$  [24], where  $h_{RF}$  is the fading gain over the RF channel, with  $E[h_{RF}^2]$  normalized to unity, and  $\bar{\gamma}_{RF}$  is the average SNR of the RF channel. The average SNR  $\bar{\gamma}_{RF}$  is given by [24]:

$$\bar{\gamma}_{RF} = \frac{E_{avg}P_{RF}G_{RF}}{\sigma_{RF}^2}, \quad (5.8)$$

where  $P_{RF}$ ,  $\sigma_{RF}^2$ , and  $G_{RF}$  are respectively, transmitted RF power, noise variance, assuming zero-mean circularly symmetric AWGN, and average power gain of the RF channel. The average power gain  $G_{RF}$  is given by [24]:

$$G_{RF}[dB] = G_T + G_R - 20\log_{10} \left( \frac{4\pi z}{\lambda_{RF}} \right) - \alpha_{oxy}z - \alpha_{rain}z, \quad (5.9)$$

where  $G_T$  and  $G_R$  denote the transmit and receive antenna gains, respectively,  $\lambda_{RF}$  is the wavelength of the RF channel, and  $\alpha_{oxy}$  and  $\alpha_{rain}$  are the attenuations caused

by oxygen absorption<sup>2</sup> and rain, respectively. The variance of the noise in the RF channel is given by  $\sigma_{RF}^2 = WN_0N_F$  [24], where  $W$  is the RF bandwidth,  $N_0$  is the noise power spectral density and  $N_F$  is the noise figure of the RF receiver.

The fading gain  $h_{RF}$  over the RF channel follows Nakagami- $m$  distribution, which represents a wide variety of realistic LOS [59], and non LOS fading channels encountered in practice [58]. Using power transformation of random variables, it is easy to show that the PDF of  $\gamma_{RF}$  is given by [59]:

$$f_{\gamma_{RF}}(\gamma_{RF}) = \left(\frac{m}{\bar{\gamma}_{RF}}\right)^m \frac{\gamma_{RF}^{m-1}}{\Gamma(m)} \exp\left(-\frac{m\gamma_{RF}}{\bar{\gamma}_{RF}}\right). \quad (5.10)$$

By using [53, Eq. (3.351.1)], and some simple algebraic manipulations, the CDF of  $\gamma_{RF}$  can be expressed as:

$$F_{\gamma_{RF}}(\gamma_{RF}) = \frac{1}{\Gamma(m)} \gamma\left(m, \frac{m\gamma_{RF}}{\bar{\gamma}_{RF}}\right), \quad (5.11)$$

where  $\gamma(\cdot, \cdot)$  is the lower incomplete Gamma function defined in [53, Eq. (8.350.1)].

## 5.2 Steady State System Performance Modeling

Since all the remote nodes are identical, we can study the system performance by focusing on one remote node, which we called the tagged node. We will use the term “other nodes” to refer to the  $N - 1$  remaining remote nodes.

### 5.2.1 Probability of Data Transmission Link Availability for a Tagged Node

We derive the probability that there is a link available for data transmission from the central node to a tagged node. We define  $a$  to be the probability that a certain FSO link is in poor quality and can't be used for data transmission from the central node to the corresponding remote node, which is given by:

$$a = P_r[\gamma_{FSO} < \gamma_T] = F_{\gamma_{FSO}}(\gamma_T), \quad (5.12)$$

where  $F_{\gamma_{FSO}}(\cdot)$  is given by (5.7).

---

<sup>2</sup>Oxygen absorption at 60 GHz attenuates the signal at all times, regardless of the weather [57].

As we are using the same type of digital modulation on both FSO and RF links, we will use the same threshold  $\gamma_T$  to measure the quality of the RF link from the central node to the tagged node. We define  $b$  to be the probability that the RF link is in poor quality and can't be used for data transmission by the central node, which is given by:

$$b = P_r[\gamma_{RF} < \gamma_T] = F_{\gamma_{RF}}(\gamma_T), \quad (5.13)$$

where  $F_{\gamma_{RF}}(\cdot)$  is given by (5.11).

Considering the FSO link from the central node to a tagged remote node, we define  $P_n$  to be the probability that  $n$  FSO links out of the remaining  $N - 1$  FSO links are in poor condition and the central node needs to use the back-up RF link for data transmission to the corresponding  $n$  remote nodes at a given time step. In this case,  $P_n$  is given by the binomial distribution as:

$$P_n = \binom{N-1}{n} a^n (1-a)^{N-n-1}, \quad n = 0, 1, 2, \dots, N-1. \quad (5.14)$$

Given that the FSO link to the tagged node is in poor quality and the RF link is in good quality, we define  $P_{RF}$  to be the probability that the central node uses the RF link to transmit data to the tagged node. Based on assumption (1),  $P_{RF}$  is given by:

$$\begin{aligned} P_{RF} &= P_r[\text{No other nodes need RF}] \\ &\quad + P_r[\text{tagged node and one other node need RF}]/2 \\ &\quad + P_r[\text{tagged node and two other nodes need RF}]/3 \\ &\quad + \dots \\ &\quad + P_r[\text{All other nodes need RF}]/N \\ &= P_0 + \frac{1}{2}P_1 + \frac{1}{3}P_2 + \dots + \frac{1}{N}P_{N-1} \\ &= \sum_{n=0}^{N-1} \frac{1}{n+1} P_n. \end{aligned} \quad (5.15)$$

Substituting with (5.14) in (5.15) and after some algebraic manipulations with the help of the binomial theorem [71, Eq. (1.2.1.1)],  $P_{RF}$  can be given in a more simplified form as:

$$P_{RF} = \frac{1}{aN} [1 - (1-a)^N]. \quad (5.16)$$

Note that, substituting with  $N = 1$  in (5.16) leads to  $P_{RF} = 1$  which corresponds to the case of point to point data transmission link from the central node to the tagged remote node with the RF link always available for data transmission conditioning that it is in good quality.

According to the quality of the FSO link from the central node to the tagged node, either the FSO link or the RF link is used for data transmission. For the RF link to be used for data transmission to a tagged node, it should be in a good quality and is not used for data transmission to another node. Thus, the probability that there is a link available for data transmission from the central node to the tagged node, denoted by  $P_{avl}$ , is defined as:

$$P_{avl} = \underbrace{1 - a}_{\text{Probability of using FSO link}} + \underbrace{a(1 - b)P_{RF}}_{\text{Probability of using RF link}}. \quad (5.17)$$

Substituting (5.16) in (5.17),  $P_{avl}$  will be given by:

$$P_{avl} = 1 - a + \left(\frac{1 - b}{N}\right)[1 - (1 - a)^N]. \quad (5.18)$$

## 5.2.2 Discrete-Time Markov Chain Model for the Tagged Node

The central node assigns a first-in-first-out (FIFO) transmit buffer of size  $B$  symbols for every remote node. The data symbols arrive at the transmit buffer at rate  $R_{in}$  symbols/second. This symbol rate  $R_{in}$  is related to the input data rate  $r$  in bits/second by  $R_{in} = r/\log_2 M$ , where  $M$  is the order of the  $M$ -QAM scheme used. The symbol arrival rate  $R_{in}$  is assumed to be the same for all the  $N$  transmit buffers. We define  $R_{out}$  as the symbol departure rate. To prevent transmit buffer overflow, we must ensure that  $R_{out}$  is greater than or equal to  $R_{in}$ . Here, the symbol arrival rate  $R_{in}$  changes over time with maximum value equal to  $R_{out}$ .

The number of symbols stored in the transmit buffer represent the state of the buffer. Thus, the buffer is in state  $\alpha_i$  when there are  $i$  symbols in the buffer (i.e., in the queue) ready for transmission. The future state of the buffer depends only on its current state and the change from one state to another will occur at discrete time values corresponding to symbol arrival and departure events. Thus, we can use the discrete-time Markov chain to model the states of the transmit buffer for the tagged node. The time step of the discrete-time Markov chain, denoted by  $T$ , is chosen

as [72]:

$$T = \frac{1}{\max(R_{in}, R_{out})} = \frac{1}{R_{out}}. \quad (5.19)$$

We define the probability of symbol arrival  $\omega$  as the probability that a symbol arrives at the buffer within the time step  $T$ . Or in other words,  $\omega$  is the probability that a time step  $T$  has a symbol.

Based on our choice for the time step  $T$  in (5.19), the resulting Markov chain is a single-arrival, single-departure queue. The corresponding state transition diagram of the transmit buffer of the tagged node is shown in Fig. 5.2. In Fig. 5.2,  $f_0 = 1 - \omega + \omega P_{avl}$ ,  $v = \omega(1 - P_{avl})$ ,  $u = (1 - \omega)P_{avl}$ ,  $f = 1 - (u + v)$ , and  $f_B = 1 - u$  are the states transition probabilities.

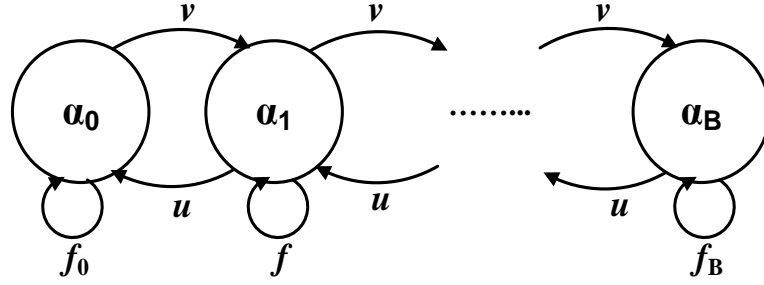


Figure 5.2: The state transition diagram for the transmit buffer of a tagged node.

The corresponding state transition matrix  $\mathbf{P}$  is given by:

$$\mathbf{P} = \begin{bmatrix} f_0 & u & 0 & \dots & 0 & 0 & 0 \\ v & f & u & \dots & 0 & 0 & 0 \\ 0 & v & f & \dots & 0 & 0 & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & f & u & 0 \\ 0 & 0 & 0 & \dots & v & f & u \\ 0 & 0 & 0 & \dots & 0 & v & f_B \end{bmatrix} \quad (5.20)$$

The steady state distribution vector  $\mathbf{s}$  corresponding to Fig. 5.2 and (5.20) is given by:

$$\mathbf{s} = [s_0 \quad s_1 \quad \dots \quad s_B]^T, \quad (5.21)$$

where  $s_i$ ,  $0 \leq i \leq B$ , is the probability that the transmit buffer of the tagged node is

in state  $\alpha_i$ , satisfying the condition:

$$\sum_{i=0}^B s_i = 1. \quad (5.22)$$

At steady state, the distribution vector  $\mathbf{s}$  settles down to a unique value and satisfies the following equation [72]:

$$\mathbf{P} \mathbf{s} = \mathbf{s}, \quad (5.23)$$

where  $\mathbf{s}$  in this case is an eigen vector for the state transition matrix  $\mathbf{P}$  with corresponding eigen value equals to 1. From (5.23), we can write the following set of difference equations:

$$v s_0 - u s_1 = 0 \quad (5.24)$$

$$v s_0 - v s_1 - u s_1 + u s_2 = 0 \quad (5.25)$$

$$v s_{i-1} - v s_i - u s_i + u s_{i+1} = 0, \quad 0 < i < B \quad (5.26)$$

The solution of this set of difference equations can be given in general form as [72]:

$$s_i = \rho^i s_0, \quad 0 \leq i \leq B, \quad (5.27)$$

where

$$\rho = \frac{v}{u} = \frac{\omega(1 - P_{avl})}{(1 - \omega)P_{avl}}. \quad (5.28)$$

The solution for  $s_0$  is obtained by substituting (5.27) in (5.22) which gives:

$$\sum_{i=0}^B \rho^i s_0 = 1. \quad (5.29)$$

After some algebraic manipulations of (5.29), we can obtain  $s_0$  as:

$$s_0 = \frac{1 - \rho}{1 - \rho^{B+1}}. \quad (5.30)$$

Combining (5.27) and (5.30) the steady state distribution for the other states is given by:

$$s_i = \frac{(1 - \rho)\rho^i}{1 - \rho^{B+1}}, \quad 0 \leq i \leq B. \quad (5.31)$$

## 5.3 Performance Metrics for the Tagged Node

The steady state distribution vector  $\mathbf{s}$  allows us to analyze the various performance metrics as explained in the following subsections.

### 5.3.1 Throughput from Central Node to the Tagged Node

We define the throughput  $Th$  as the probability of transmitting a symbol over a symbol period. Conditioning on the status of the buffer,  $Th$  can be calculated as:

$$Th = \omega P_{avl} s_0 + \sum_{i=1}^B P_{avl} s_i, \quad (5.32)$$

where the first term on the RHS is the probability a symbol leaves the buffer when the buffer is empty. The second term on the RHS is the probability a symbol leaves the buffer when it is not empty. Using (5.22), the expression in (5.32) becomes:

$$Th = P_{avl}[1 - s_0(1 - \omega)]. \quad (5.33)$$

The throughput in units of symbols/second is given by:

$$th = Th R_{out} \quad [\text{symbols/second}] \quad (5.34)$$

### 5.3.2 Average Buffer Size

The average buffer size  $Q_a$  is the average number of symbols in the buffer, which can be expressed as:

$$Q_a = \sum_{i=0}^B i s_i. \quad (5.35)$$

The above expression represents the weighted sum of the number of symbols in the buffer. Substituting (5.31) in (5.35) and using [71, Eq. (1.2.2.3)] the average buffer

size after simplification is given by:

$$Q_a = \frac{\rho[1 - (B + 1)\rho^B + B\rho^{B+1}]}{(1 - \rho)(1 - \rho^{B+1})}. \quad (5.36)$$

### 5.3.3 Average Buffer Queuing Delay

The average queuing delay  $T_q$  is the average number of time steps that a symbol spends in the buffer before being transmitted. Using Little's result, this delay is given by [72]:

$$T_q = \frac{Q_a}{Th}. \quad (5.37)$$

The average queuing delay in units of seconds is given by:

$$t_q = \frac{Q_a}{th} \quad [\text{seconds}]. \quad (5.38)$$

### 5.3.4 Symbol Loss Probability

A symbol is lost when it arrives to a full transmit buffer and the symbol at the head of the queue does not leave. The symbol loss probability  $P_L$  is given by:

$$P_L = \omega s_B (1 - P_{avl}). \quad (5.39)$$

The symbol loss rate  $R_L$  in units of symbols/second is given by:

$$R_L = P_L R_{out} \quad [\text{symbols/second}]. \quad (5.40)$$

As a verification of the results, we can see that:

$$\omega = Th + P_L, \quad (5.41)$$

which is consistent to the traffic conservation principle [72], dictating that the input data rate must equal the output symbol rate plus the symbol loss rate.

### 5.3.5 Efficiency of the Queue

The efficiency of the queue  $\varphi$  is defined as the ratio of probability of a symbol leaving the buffer relative to the probability that a symbol arriving at the buffer. This can

be expressed as:

$$\varphi = \frac{Th}{w} = \frac{P_{avl}[1 - s_0(1 - w)]}{w}, \quad (5.42)$$

The efficiency  $\varphi$  gives an indication of symbol loss due to buffer overflow. A value of  $\varphi = 1$  implies no buffer overflow. A value of  $\varphi < 1$  implies buffer overflow and potential symbol loss.

### 5.3.6 RF Link Utilization

The probability that the RF link is needed in a given time step, denoted by  $N_e$ , can be calculated as:

$$\begin{aligned} N_e &= 1 - \{\text{Pr}[\gamma_{FSO} \geq \gamma_T]\}^N \\ &= 1 - \{1 - \text{Pr}[\gamma_{FSO} < \gamma_T]\}^N \\ &= 1 - (1 - a)^N. \end{aligned} \quad (5.43)$$

Then the RF link utilization  $U$  defined as the probability that the RF link is used in a given time step can be calculated as:

$$U = (1 - b)N_e. \quad (5.44)$$

## 5.4 Numerical Results

In this section, we present several numerical examples to illustrate our analysis. We assume RF channel fading severity of  $m=5$ . Assume using 16-QAM digital modulation,  $\gamma_T$  is chosen to be equal to 21 dB to satisfy a minimum target BER of  $10^{-6}$ . The relevant parameters of the FSO and RF subsystems considered for the numerical results in this paper are provided in Table 5.1 [17], [24], and [64]. The average QAM symbol energy  $E_{avg}$  is assumed to be normalized to unity. The strongest atmospheric turbulence commonly occurs when weather is clear and becomes weaker as the weather condition gets worse by means of either fog or rain. The values of  $C_n^2$  varies from  $10^{-15}$  to  $2 \times 10^{-13}$  as the atmospheric turbulence strength varies from weak to strong [17]. Mainly, the FSO link is affected by foggy weather. Thus, we consider in our numerical examples the scenario of moderate foggy weather condition with weather attenuation coefficient  $\alpha_{FSO} = 42.2$  dB/Km and moderate atmospheric turbulence with  $C_n^2 = 5 \times 5^{-14}$  and no rain with RF rain attenuation  $\alpha_{rain} = 0$  dB/Km.

Note that, under foggy weather condition and no rain and by using the parameters given in Table 5.1,  $a = 0.90$  and  $b = 0.22$ . These values of  $a$  and  $b$  are used in Figs. 5.3 - 5.7. In Fig. 5.8 we use arbitrary values of  $a$  with  $b = 0.22$ .

Table 5.1: Parameters of FSO and RF subsystems

Parameter	Symbol	Value
FSO Subsystem		
Wavelength	$\lambda_{FSO}$	1550 nm
Oscillator Power	$P_{LO}$	$10^{-2}$ W
Shot Noise Variance	$\sigma_{FSO}^2$	$5 \times 10^{-12}$
Responsivity	$\eta$	0.5 A/W
Photodetector Diameter	D	20 cm
Transmit Power	$P_{FSO}$	15 dBm
Transmit divergence at $1/e^2$	$\theta_0$	2.5 mrad
Jitter standard deviation	$\sigma_s$	30 cm
Link distance	$z$	1000 m
RF Subsystem		
Carrier Frequency	$f_{RF}$	60 GHz
Bandwidth	$W$	250 MHz
Transmit Power	$P_{RF}$	25 dBm
Transmit Antenna Gain	$G_T$	43 dBi
Receive Antenna Gain	$G_R$	43 dBi
Noise Power Spectral Density	$N_0$	-114 dBm/MHz
Receiver Noise Figure	$N_F$	5 dB
Oxygen Attenuation	$\alpha_{oxy}$	15.1 dB/Km

In Fig. 5.3, we plot the throughput  $Th$  as function of the symbol arrival probability  $\omega$  for different values of  $N$ . The throughput goes into two phases viz linear and saturation. The linear phase occurs at low  $\omega$  values. The saturation phase occurs for higher values of  $\omega$ . The transition point occurs when the buffer is not empty (i.e.,  $s_0 = 0$ ). From (5.30), this condition occurs when  $\rho = 1$ . From (5.28),  $\rho = 1$  occurs when the symbol arrival probability  $\omega = P_{avl}$ . Therefore, the linear phase of the throughput occurs in the region  $\omega \in [0, P_{avl})$ . The saturation phase of the throughput occurs in the region  $\omega \in [P_{avl}, 1]$ . Furthermore, at saturation the throughput decreases with increasing  $N$ . This is due to the increasing competition to access the shared RF link.

The dotted red line in Fig. 5.3 shows the throughput of the tagged node when there is no backup RF link. It is worth noting that this throughput is independent of value of  $N$ . While all the other lines show the cases when there is a backup RF link.

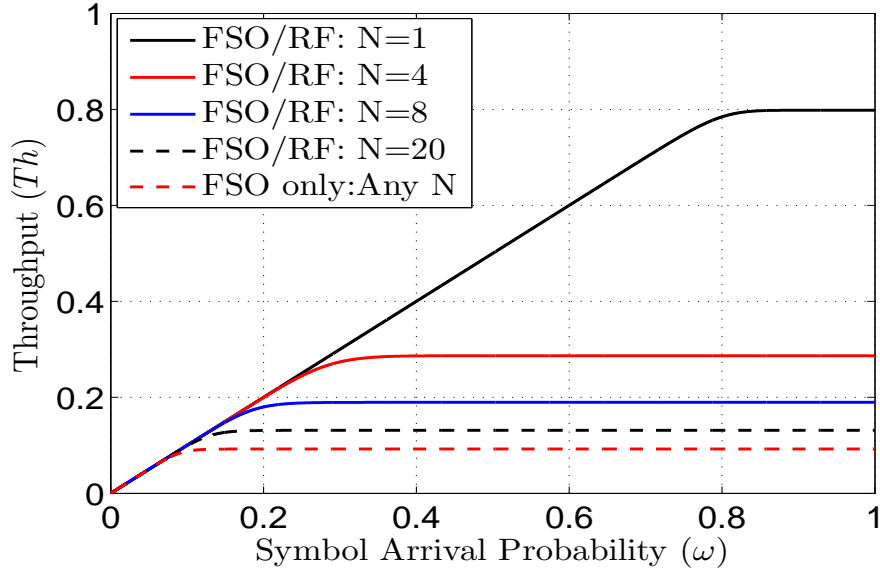


Figure 5.3: Throughput with  $B = 10$  symbols.

It can be seen that using a common backup RF link had improved the throughput.

It is worth to mention that numerical simulations have shown that reducing the buffer size  $B$  results in smoother transitions between the linear and the saturation phases of the throughput. The buffer size  $B$  has no impact on the saturation values.

In Fig. 5.4, we plot the average buffer size  $Q_a$  as function of the symbol arrival probability  $\omega$  for different values of  $N$ . Fig. 5.4 shows two situations for  $N = 1$ . The first situation is the red dotted line when there is no backup RF link. In this situation, the buffer starts filling at low symbol arrival probabilities. This is because the FSO link is in bad quality due to the foggy weather. The second situation is the solid black line when there is backup RF link and only one remote node. In this situation, the buffer starts filling at high symbol arrival probabilities. This is because the central node uses the backup RF link. The average buffer size  $Q_a$  increases with smaller values of  $\omega$  as  $N$  increases. The average buffer size  $Q_a$  saturates at the maximum buffer size  $B$  as expected.

In Fig. 5.5, we plot the average queuing delay  $T_q$  as function of the symbol arrival probability  $\omega$  for different values of  $N$ . The average queuing delay  $T_q$  shows an S-type behavior, where it starts at low values then starts increasing after a certain symbol arrival probability value. It then saturates. The saturation value increases with increasing values of  $N$ . The best performance occurs for the case when there is a single remote node with a backup RF link. The worst performance occurs when

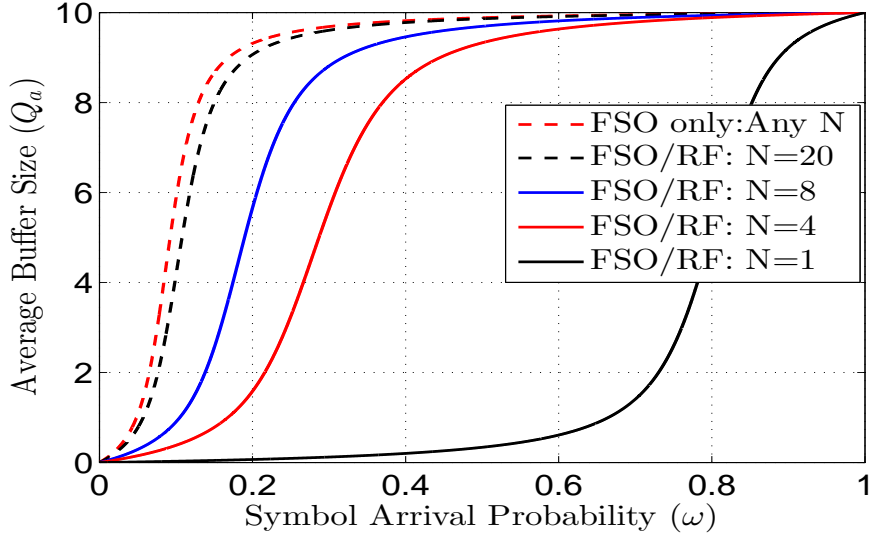


Figure 5.4: Average buffer size with  $B = 10$  symbols.

there is no backup RF link. For the cases that  $N > 1$  and there is a backup RF link shown in the figure by the red, blue, and dotted black lines, it is noted that the average queuing delay  $T_q$  is not equal to zero at very low value of  $\omega$ . This is because, as  $N$  increases the probability  $P_{avl}$  decreases and a symbol will wait in the buffer until a link is available for its transmission. The dotted red line indicates the case when using the FSO links only without a backup RF link. We note the same observation of non-zero delay at very low value of  $\omega$ . This is because there is no backup RF link and the symbol will wait until the FSO link becomes available. The special case for  $N = 1$  shown in the figure by the black line will have the least average queuing delay  $T_q$ .

In Fig. 5.6, we plot the symbol loss probability  $P_L$  as function of the symbol arrival probability  $\omega$  for different values of  $N$ . The symbol loss probability goes into two phases viz zero loss and linear. The zero loss phase occurs at low  $\omega$  values. The linear phase occurs for higher values of  $\omega$ . The transition point occurs when the buffer is full with probability  $s_B > 0$ . This condition is equivalent to the condition  $s_0 = 0$ . From (5.30), this condition occurs when  $\rho = 1$ . From (5.28), this occurs when the symbol arrival probability  $\omega = P_{avl}$ . Therefore, the zero loss phase of the symbol loss probability occurs in the region  $\omega \in [0, P_{avl}]$ . The linear phase of the symbol loss probability occurs in the region  $\omega \in [P_{avl}, 1]$ .

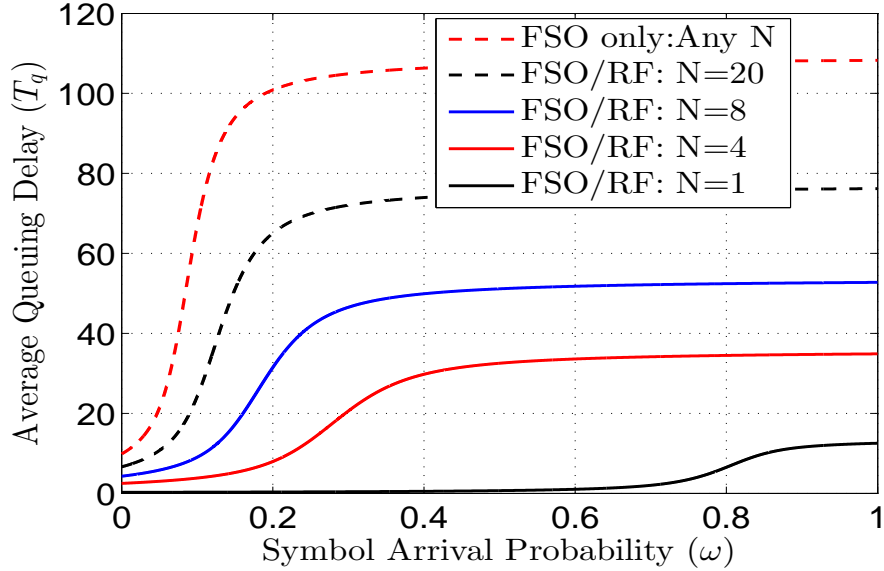


Figure 5.5: Average queuing delay with  $B = 10$  symbols.

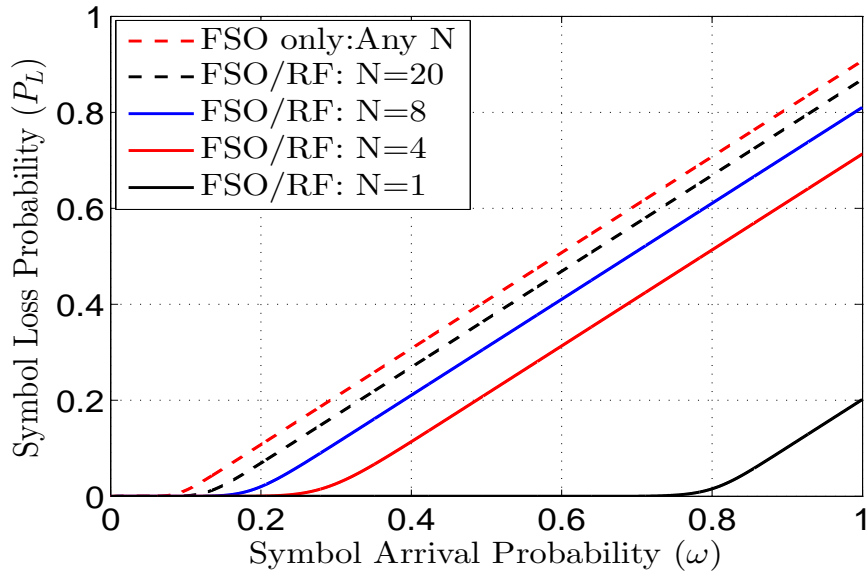


Figure 5.6: Symbol loss probability with  $B = 10$  symbols.

In Fig. 5.7, we plot the efficiency  $\varphi$  as function of the symbol arrival probability  $\omega$  for different values of  $N$ . The efficiency  $\varphi$  goes into two phases viz unity efficiency and decreasing efficiency. The unity efficiency phase occurs at low  $\omega$  values. The decreasing efficiency occurs for higher values of  $\omega$ . The transition point occurs when the buffer is not empty (i.e.,  $s_0 = 0$ ). From (5.30), this condition occurs when  $\rho = 1$ .

From (5.28), this occurs when the symbol arrival probability  $\omega = P_{avl}$ . Therefore, the unity efficiency phase occurs in the region  $\omega \in [0, P_{avl})$ . The decreasing efficiency phase occurs in the region  $\omega \in [P_{avl}, 1]$ . Furthermore, the efficiency decreases as  $N$  increases. This is due to the increasing competition to access the shared RF link. The dotted red line in Fig. 5.7 shows the efficiency of the tagged node when there is no backup RF link. It is worth noting that this efficiency is independent of value of  $N$ . While all the other lines show the cases when there is a backup RF link. It can be seen that using a common backup RF link had improved the efficiency.

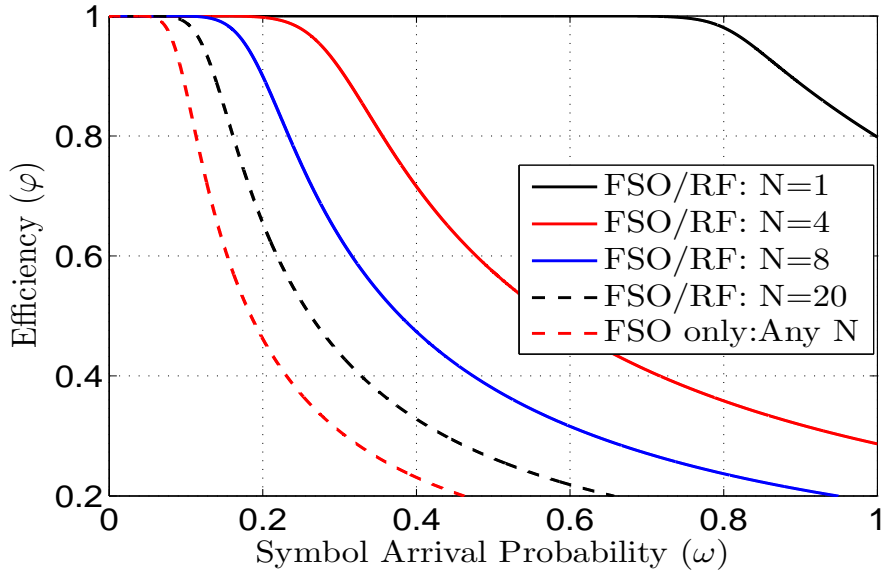


Figure 5.7: Efficiency with  $B = 10$  symbols.

In Fig. 5.8, we plot the RF utilization  $U$  as function of the number of the remote nodes  $N$  for different values of the poor quality probability of the FSO link  $a$ . The RF utilization  $U$  increases as  $N$  increases until it saturates. This is because, as  $N$  increases the probability that more FSO links are in poor quality increases and thus more remote nodes will need to access the RF link. The value of the saturation depends on the quality of the RF link. For a fixed value of  $N$ , the RF link utilization increases as the FSO link quality degrades.

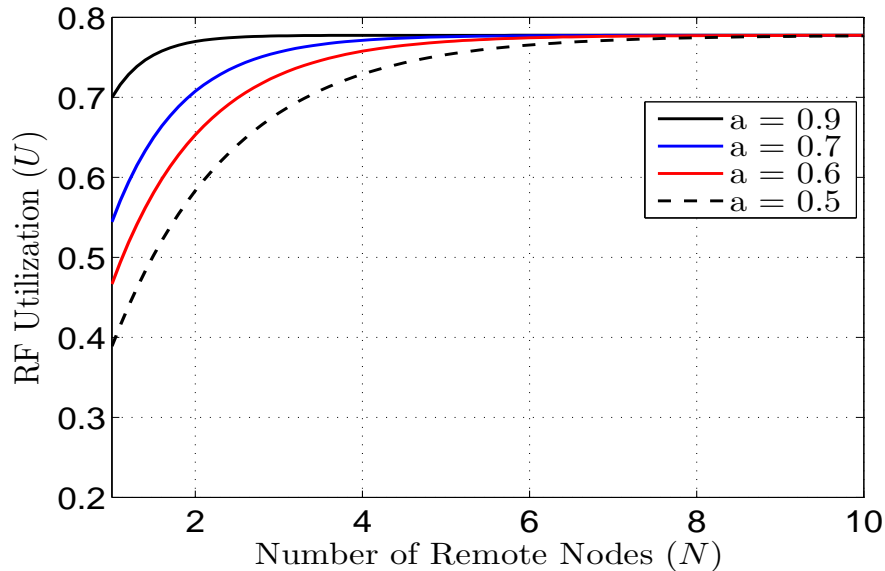


Figure 5.8: RF channel utilization

## 5.5 Summary

In this chapter, we proposed a novel P2MP network based on hybrid FSO/RF transmission system. A common backup RF link is used by the central node for data transmission to any remote node in case of the failure of its corresponding FSO link. The central node assigns a transmit buffer for every remote node. We studied the performance of a single remote node (tagged node) rather than studying the overall system performance. A discrete-time Markov chain model was developed for the transmit buffer of the link between the central node and the tagged remote node. Studying the tagged node allowed us to investigate several performance criteria such as throughput from central node to the tagged node, the average transmit buffer size, the symbol queuing delay in the transmit buffer, the efficiency of the queuing system, the symbol loss probability, and the RF link utilization. Numerical examples showed that the P2MP Hybrid FSO/RF network achieves considerable performance improvement over the P2MP FSO-only network.

## Chapter 6

# Dual-Hop VLC/RF Transmission System with Energy Harvesting Relay under Hard Delay Constraint

In this chapter, we introduce a dual-hop VLC/RF system as a new hybrid VLC/RF approach to extend the coverage of indoor VLC systems. In this approach, a second-hop RF link is used to extend the coverage of a first-hop VLC link by introducing a relay between the two hops. In order to reduce power consumption, the relay is equipped with a Photovoltaic module that harvests indoor light energy and converts it into electrical energy. The relay uses the harvested energy to retransmit the data received over the first-hop VLC link to a mobile terminal over the second-hop RF link. We investigate the data packet transmission performance of the proposed system. A main Quality-of-Service (QoS) requirement in many data services such as video and real-time multimedia streaming, high throughput file transfers and Voice-over-IP is to transmit a data packet within a strict end-to-end delay constraint. Considering the QoS requirement of transmitting a data packet of certain size from the data source to the mobile terminal within a strict time delay constraint, the probability of data packet loss is analyzed.

The remainder of the chapter is organized as follows. In section 6.1, we introduce the system and channel models of the dual-hop VLC/RF transmission system with energy harvesting relay. In section 6.2, we introduce the model for the indoor light

energy harvesting at the relay. In section 6.3, we present the packet loss probability analysis of the proposed hybrid transmission system. Finally, section 6.4 presents some numerical examples to investigate the performance of the introduced system, followed by the chapter summary in section 6.5.

## 6.1 Dual-Hop VLC/RF Transmission System Modeling

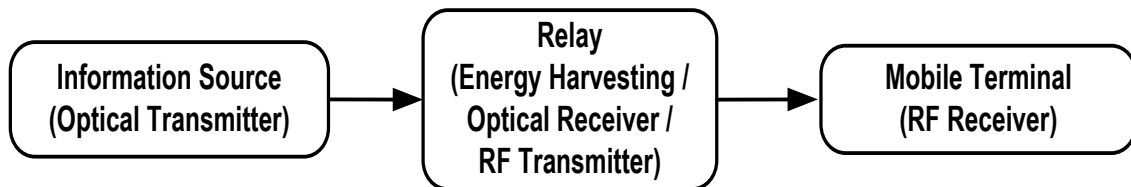


Figure 6.1: General block diagram of a dual-hop hybrid VLC/RF transmission system with energy harvesting relay.

The general block diagram of a dual-hop hybrid VLC/RF transmission system with energy harvesting relay is shown in Fig. 6.1. We assume here a time division relaying scheme which composes of two time slots. In the first time slot of duration  $T_1$  seconds, the source terminal uses a LED optical transmitter to transmit a data packet of size  $B$  bits over the VLC channel to the relay. At the same time, the relay harvests light energy from indoor artificial light sources and from sunlight energy entering the room. In the second time slot of duration  $T_2$  seconds, the relay harvests more light energy from the available indoor light sources and uses the harvested energy to retransmit the data packet to the mobile terminal over the second-hop RF channel. With the introduction of parameter  $\alpha \in [0, 1)$ , we specify the portion of  $T_2$  used for the excess light energy harvesting as  $\alpha T_2$  and the portion of  $T_2$  used for data packet retransmission as  $(1 - \alpha)T_2$  as shown in Fig. 6.2. It is worth to mention here that there is no harvested energy during the RF transmission duration  $(1 - \alpha)T_2$ . This is because during the RF transmission, the harvested energy storage device (for example a battery) is discharging and simultaneous charging and discharging for the storage device is very challenging to implement. The relay is assumed to have a buffer to hold the data packet for the time duration of  $\alpha T_2$  before the data packet retransmission process begins.

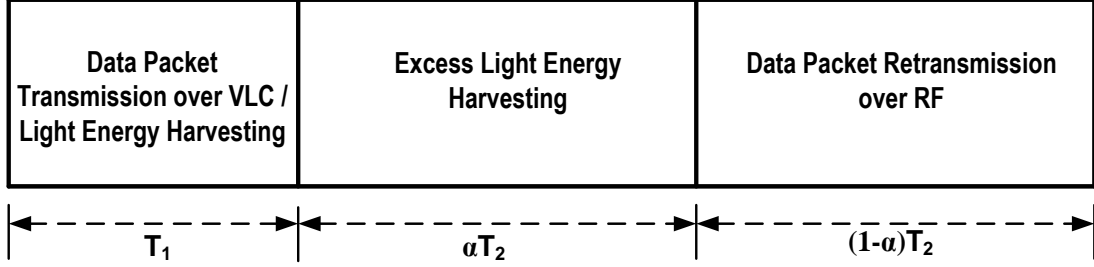


Figure 6.2: Equivalent time representation of the dual-hop hybrid VLC/RF transmission system with energy harvesting relay.

To comply with a certain QoS requirement, the total time to transmit one data packet from the source terminal to the mobile terminal  $T_1 + T_2$  must not exceed a strict delay constraint of  $T_d$  seconds.

### 6.1.1 Modeling the First-hop from LED Source to Relay

We assume that the VLC channel can support data rate up to one Gbits/second [73]. Then, the duration of the first time slot  $T_1$  is related to the first-hop data rate, denoted by  $R_1$ , as

$$T_1 = \frac{B}{R_1} \quad [\text{Second}]. \quad (6.1)$$

The relay terminal is assumed to be located in a fixed position, where the photo-detector<sup>1</sup> used for data detection at the relay has a clear LOS link to the LED source. Since the VLC channel gain depends mainly on the irradiance angle, the incidence angle of the optical signal and the distance from the LED to the photo-detector [45], which are fixed in this case, the VLC channel is considered a static channel with constant data rate  $R_1$  here.

### 6.1.2 Modeling the Second-hop from Relay to Mobile Terminal

The relay will use the harvested energy during  $T_1$  and  $\alpha T_2$  for its data packet retransmission to the mobile terminal during  $(1 - \alpha)T_2$ . In the steady state, the initial stored energy present at the start of the data packet transmission over the VLC channel will

<sup>1</sup>This photo-detector can be a passive device that does not require an additional power supply for data detection [49].

be equal to the energy remaining in the harvested energy storage device after the RF retransmission of the data packet. Here, we assume that the digital signal processing operation to retrieve the data at the relay, before the RF retransmission process, only consumes a very small portion of the harvested energy, which can be neglected. Thus, the total RF retransmission energy equals to the total harvested energy. Then under the steady state condition, the total RF retransmission power, denoted by  $P_2$ , in this case is given by:

$$P_2 = \frac{P_h(T_1 + \alpha T_2)}{(1 - \alpha)T_2}, \quad (6.2)$$

where  $P_h$  is the electrical power that is converted from the light energy harvested over time duration of  $T_1 + \alpha T_2$  and stored in the storage device.

Accordingly, the instantaneous received SNR at the mobile terminal, denoted by  $\gamma_2$ , can be written as [32]:

$$\begin{aligned} \gamma_2 &= \frac{|h_2|^2 P_2}{G_2 \sigma} \\ &= \frac{|h_2|^2 P_h (T_1 + \alpha T_2)}{G_2 \sigma (1 - \alpha) T_2}, \end{aligned} \quad (6.3)$$

where  $|h_2|^2$  is the RF channel power gain with  $E[|h_2|^2]$  normalized to unity, where  $E[\cdot]$  is the expectation operator, and  $\sigma$  is the power of the AWGN noise.  $G_2$  in (6.3) is the second-hop path loss defined as [74]:

$$G_2 = \left( \frac{4\pi d_0}{\lambda} \right)^2 \left( \frac{d_2}{d_0} \right)^\gamma, \quad (6.4)$$

with  $\lambda$  is the RF carrier wavelength,  $d_0$  is the reference distance ( $d_0 = 1\text{m}$  for indoor environment [74]),  $d_2$  is the distance from the relay to the mobile terminal, and  $\gamma$  is the path loss exponent (typically,  $\gamma$  takes values 1.6 - 1.8 for indoor situations [74]).

The RF fading gain  $|h_2|$  is modeled by Nakagami- $m$  distribution, which represents a wide variety of realistic LOS and non LOS fading channels encountered in practice [58]. The PDF of  $|h_2|^2$  is given by [59]:

$$f_{|h_2|^2}(z) = \frac{m^m z^{m-1}}{\Gamma(m)} \exp(-mz), \quad z \geq 0, \quad (6.5)$$

where  $m$  is the Nakagami- $m$  parameter indicating the fading severity over the second-hop RF channel. By using [53, Eq. (3.351.1)], and some simple algebraic manipula-

tions, the CDF of  $|h_2|^2$  can be expressed as:

$$F_{|h_2|^2}(z) = \frac{1}{\Gamma(m)} \gamma(m, mz), \quad z \geq 0, \quad (6.6)$$

where  $\gamma(\cdot, \cdot)$  is the lower incomplete Gamma function defined in [53, Eq. (8.350.1)].

The highest data rate that can be supported by the second-hop RF channel, denoted by  $R_2$ , is related to the SNR  $\gamma_2$  and is given by the well-known Shannon formula as [32]:

$$R_2 = W \log_2(1 + \gamma_2) \quad [\text{bits/second}], \quad (6.7)$$

where  $W$  is the RF channel bandwidth in Hertz (Hz).

## 6.2 Modeling Energy Harvesting at the Relay

We now propose a statistical model for the harvested energy which will be used in analyzing the packet loss probability in the next section. The relay is equipped with an excess photovoltaic module<sup>2</sup> which harvests light energy from indoor artificial light sources and sunlight energy entering the room and converts it into electrical energy. The harvested electrical power by the photovoltaic cell  $P_h$  is given by [50]:

$$P_h = 0.75 I_{sc} V_{oc}, \quad (6.8)$$

where  $I_{sc}$  and  $V_{oc}$  are, respectively, the short circuit current and the open circuit voltage of the photovoltaic cell. The short circuit current  $I_{sc}$  varies with the variations in the light intensity  $I$  as  $I_{sc} = CI$ , where  $C$  is a constant that depends on the type of the photovoltaic cell used<sup>3</sup> and its manufacture parameters [50]. The open circuit voltage  $V_{oc}$  is related to  $I_{sc}$  as [50]:

$$V_{oc} = V_t \ln \left( \frac{I_{sc}}{I_0} + 1 \right), \quad (6.9)$$

where  $V_t$  is the thermal voltage ( $V_t \approx 25$  mVolt) and  $I_0$  is the dark saturation current of the photovoltaic cell, which is the photovoltaic cell leakage current in the absence of

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<sup>2</sup>Note that, this photovoltaic module is different from the photo-detector that is used for data packet reception over the VLC channel.

<sup>3</sup>For example the amorphous silicon (a-Si) photovoltaic cells which have a relatively high efficiency at low light levels, compared to other types of photovoltaic cells [51], that makes them particularly suited for indoor uses.

light ( $I_0$  is in the order of  $10^{-9} \sim 10^{-12}$  Ampere [75]). Thus, the harvested electrical power  $P_h$  in (6.8) can be rewritten as:

$$P_h = 0.75 V_t I_{sc} \ln \left( \frac{I_{sc}}{I_0} + 1 \right). \quad (6.10)$$

Due to the random motion of the people within the room, the photovoltaic module is susceptible to shadowing effect and will receive various reflected light components. Thus, the intensity of the incident light on the photovoltaic cell  $I$  is a random variable which can be modeled by the common Log-normal distribution in such cases [32]. Accordingly, the short circuit current of the photovoltaic cell  $I_{sc}$ , which depends on the incident light intensity  $I$ , is also a random variable that follows the Log-normal distribution  $I_{sc} \sim \text{LN}(\mu_x, \sigma_x)$ , where  $\mu_x$  and  $\sigma_x$  are the mean and the standard deviation of  $I_{sc}$ . Then, the PDF of  $I_{sc}$  is given by:

$$f_{I_{sc}}(x) = \frac{1}{x\sqrt{2\pi}\sigma_{\ln x}} \exp \left[ -\frac{(\ln(x) - \mu_{\ln x})^2}{2\sigma_{\ln x}^2} \right], \quad (6.11)$$

where  $\mu_{\ln x}$  and  $\sigma_{\ln x}$  are the mean and standard deviation of the logarithmic samples of  $I_{sc}$  and are related to  $\mu_x$  and  $\sigma_x$  by [56]:

$$\mu_{\ln x} = \ln \left( \frac{\mu_x^2}{\sqrt{\mu_x^2 + \sigma_x^2}} \right), \quad \sigma_{\ln x} = \sqrt{\ln \left( \frac{\sigma_x^2}{\mu_x^2} + 1 \right)}. \quad (6.12)$$

**Proposition 1.** *The output power from the photovoltaic cell can be modeled as a Log-normal distribution,  $P_h \sim \text{LN}(\mu_y, \sigma_y)$ , where  $\mu_y$  and  $\sigma_y$  are the mean and the standard deviation of  $P_h$ . Then, the PDF of  $P_h$  is given by:*

$$f_{P_h}(y) = \frac{1}{y\sqrt{2\pi}\sigma_{\ln y}} \exp \left[ -\frac{(\ln(y) - \mu_{\ln y})^2}{2\sigma_{\ln y}^2} \right], \quad (6.13)$$

where  $\mu_{\ln y}$  and  $\sigma_{\ln y}$  are the mean and standard deviation of the logarithmic samples of  $P_h$  and are related to  $\mu_y$  and  $\sigma_y$  by:

$$\mu_{\ln y} = \ln \left( \frac{\mu_y^2}{\sqrt{\mu_y^2 + \sigma_y^2}} \right), \quad \sigma_{\ln y} = \sqrt{\ln \left( \frac{\sigma_y^2}{\mu_y^2} + 1 \right)}. \quad (6.14)$$

The mean  $\mu_y$  of  $P_h$  is calculated as:

$$\mu_y = \int_0^{\infty} 0.75V_t x \ln \left( \frac{x}{I_0} + 1 \right) f_{I_{sc}}(x) dx, \quad (6.15)$$

which can be evaluated by numerical integration, and the standard deviation  $\sigma_y$  of  $P_h$  is calculated as:

$$\sigma_y = V_t \sigma_x \left[ \frac{\mu_x}{\mu_x + I_0} + \ln \left( \frac{\mu_x}{I_0} + 1 \right) \right]. \quad (6.16)$$

*Proof:* see appendix A.

### 6.3 Packet Loss Probability Analysis of the Dual-hop VLC/RF system

The main goal here is to successfully transmit the data packet within a fixed time duration of  $T_d$ . An important performance metric in this case is the packet loss probability.

Given the total transmission time constraint  $T_d$ , the data packet retransmission time duration of  $(1 - \alpha)T_2$  must not exceed the value of  $T_d - T_1 - \alpha T_2$ . As such the relay must retransmit the data packet with minimum data rate of  $R_{2T}$  given by:

$$R_{2T} = \frac{B}{T_d - T_1 - \alpha T_2} \quad (6.17)$$

to satisfy the strict end-to-end delay constraint of  $T_d$ .

The data packet will be lost if the data rate in (6.17) exceeds the Shannon limit given in (6.7). Or in other words, the data packet will be lost if the RF channel can not support the requirement of this minimum data rate  $R_{2T}$ . Then the probability of data packet loss is given by:

$$P_{PL} = P_r[R_2 < R_{2T}]. \quad (6.18)$$

Substituting with (6.7) in (6.18) and after some mathematical manipulation, (6.18) can be rewritten as:

$$P_{PL} = P_r[\gamma_2 < \gamma_{2T}], \quad (6.19)$$

where  $\gamma_{2T} = 2^{\frac{R_{2T}}{W}} - 1$ .

This means that the packet is lost if the received SNR  $\gamma_2$  at the mobile terminal is less than the threshold value of  $\gamma_{2T}$ . This can happen due to insufficient harvested light energy at the relay or poor RF channel from the relay to the mobile terminal. Thus, after substitution with (6.3) in (6.19),  $P_{PL}$  can be calculated as:

$$\begin{aligned} P_{PL} &= P_r \left[ \frac{|h_2|^2 P_h(T_1 + \alpha T_2)}{G_2 \sigma (1 - \alpha) T_2} < \gamma_{2T} \right] \\ &= P_r \left[ |h_2|^2 < \frac{A}{P_h} \right], \end{aligned} \quad (6.20)$$

where  $A = G_2 \sigma \gamma_{2T} (1 - \alpha) T_2 / (T_1 + \alpha T_2)$ .

Conditioning on  $P_h$ , the probability of packet loss  $P_{PL}$  in (6.20) is given by:

$$\begin{aligned} P_{PL} &= \int_0^\infty P_r \left[ |h_2|^2 < \frac{A}{y} \mid y \right] f_{P_h}(y) dy \\ &= \int_0^\infty \frac{\gamma \left( m, m \frac{A}{y} \right)}{\Gamma(m)} \frac{1}{y \sqrt{2\pi} \sigma_{\ln y}} \exp \left[ -\frac{(\ln(y) - \mu_{\ln y})^2}{2\sigma_{\ln y}^2} \right] dy. \end{aligned} \quad (6.21)$$

By using the change of variable  $t = \frac{\ln(y) - \mu_{\ln y}}{\sqrt{2} \sigma_{\ln y}}$ ,  $P_{PL}$  in (6.21) can be rewritten as:

$$P_{PL} = \frac{1}{\sqrt{\pi} \Gamma(m)} \int_{-\infty}^{\infty} f(t) e^{-t^2} dt, \quad (6.22)$$

where  $f(t) = \gamma \left( m, mA e^{-(\sqrt{2}\sigma_{\ln y} t + \mu_{\ln y})} \right)$ , with  $\gamma(\cdot, \cdot)$  as the lower incomplete Gamma function defined in [53, Eq. (8.350.1)].

The term  $\int_{-\infty}^{\infty} f(t) e^{-t^2} dt$  in (6.22) has the form of the Gaussian-Hermite integration which can be closely approximated as [76]:

$$\int_{-\infty}^{\infty} f(t) e^{-t^2} dt \approx \sum_{i=1}^N \omega_i f(t_i), \quad (6.23)$$

where  $t_i$  and  $\omega_i$  are abscissas and weight factors for the Gaussian-Hermite integration.  $t_i$  and  $\omega_i$  for different values of  $N$  are available in [76, Table (25.10)], or can be calculated by a simple MATLAB program. Therefore,  $P_{PL}$  can be approximately

calculated in a closed form as:

$$P_{PL} = \frac{1}{\sqrt{\pi} \Gamma(m)} \sum_{i=1}^N \omega_i f(t_i). \quad (6.24)$$

There is a trade-off between the portion of the second time slot  $\alpha T_2$  consumed for excess light energy harvesting and the time portion  $(1 - \alpha)T_2$  used for data packet retransmission over the second-hop. If  $\alpha$  is large, more light energy will be harvested and more power will be available for the retransmission process, while less time will be available for the data packet retransmission process. On the other hand, if  $\alpha$  is small, less light energy will be harvested and less power will be available for the retransmission process, although the time available for the data packet retransmission process is large in this case. Thus, we optimize the parameter  $\alpha$  in terms of minimizing the data packet loss probability.

The optimal parameter  $\alpha^*$ , which minimizes the packet loss probability  $P_{PL}$  can be obtained by solving  $\partial P_{PL}/\partial \alpha = 0$  for  $\alpha$ . However, it will be difficult to obtain the optimal  $\alpha^*$  in closed form. As an alternative method, we can treat the problem as one-dimensional optimization problem with uncertainty range of  $[0, 1)$ , and use numerical methods, such as Golden-section search method [68] to search for the optimal  $\alpha^*$ .

## 6.4 Numerical Results

In this section, we present numerical examples to illustrate our analysis. We assume that a data packet of size  $B = 8000$  bits is to be transmitted from the LED source to the mobile terminal within the time delay constraint of  $T_d = 1000$  micro seconds. The LED source is transmitting with data rate of  $R_1 = 1$  Gbits/second. We assume the mean and the standard deviation of the short-circuit of the photovoltaic cell to be  $\mu_x = 3 \times 10^{-5}$  Ampere and  $\sigma_x = 0.5 \times 10^{-5}$  Ampere. The RF carrier frequency is  $f = 2.4$  GHz and the RF channel bandwidth is  $W = 20$  MHz which are taken from the WiFi 802.11 g protocol, along with RF AWGN power of  $\sigma = 5 \times 10^{-12}$  Watt and RF fading severity of  $m = 3$ .

In Fig. 6.3, we plot the packet loss probability as function of the parameter  $\alpha$  for different values of the distance  $d_2$  from the relay to the mobile terminal and a fixed path loss exponent of  $\gamma = 1.6$ . The numerical results shown in Fig. 6.3 are obtained using  $N=30$  in (6.24). It can be observed that evaluating  $P_{PL}$  using the

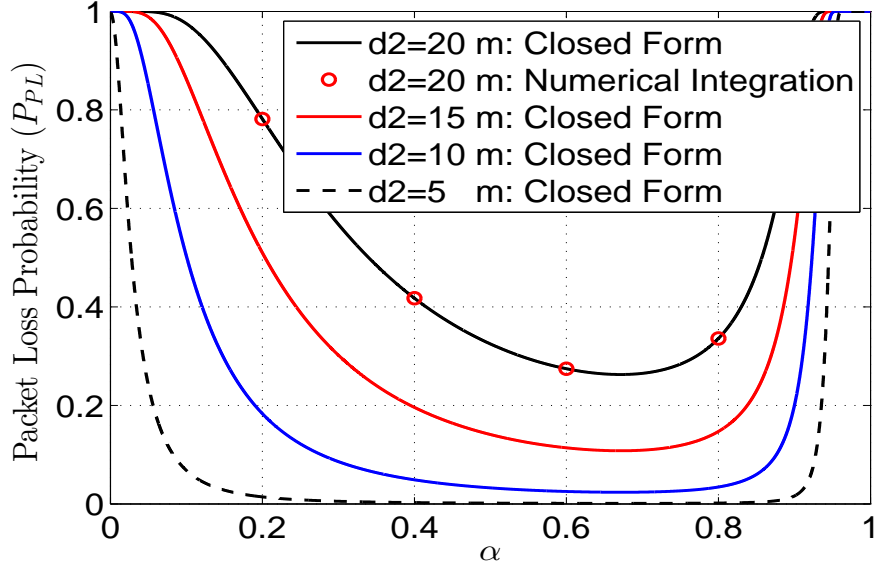


Figure 6.3: Packet loss probability for different values of  $d_2$  with  $\gamma = 1.6$ .

approximated closed form gives accurate results that coincide with the values of  $P_{PL}$  obtained by evaluating the integral in (6.21) using numerical methods. Starting from a small value of  $\alpha$  close to zero in Fig. 6.3,  $P_{PL}$  decreases with the increase of  $\alpha$  until it reaches its minimum value at  $\alpha^*$ . This is because, as  $\alpha$  increases, more light energy is harvested at the relay and thus more electrical power is available for data packet retransmission process. However, as  $\alpha$  increases over  $\alpha^*$ , the time available for data packet retransmission is reduced and the data rate  $R_{2T}$  increases. Although more light energy was harvested, the RF channel can not support the minimum required data rate  $R_{2T}$  to maintain the time delay constraint of  $T_d$ . Thus,  $P_{PL}$  starts to increase. By numerical search, we can find that the optimal portion of the second-hop time duration  $T_2$  to harvest more light energy is  $\alpha^* = 0.6713$  in this case. By simple calculation, we can find that  $R_{2T} = 24.5$  Mbits/second at  $\alpha = \alpha^*$ . We can observe that the value of  $\alpha^*$  is independent of the distance  $d_2$ . This could be explained with the aid of (6.20) and (6.24). Performing the partial differentiation of  $P_{PL}$  in (6.24) with respect to  $\alpha$  will include performing the partial differentiation of  $A$  defined in (6.20) with respect to  $\alpha$ . As  $G_2$  is a multiplicative term of  $A$ , then when equating the partial derivative with zero to find the optimal  $\alpha$ , the term  $G_2$  will be eliminated. Thus,  $G_2$  does not affect the value of  $\alpha^*$ .

For a fixed value of  $\alpha$  in Fig. 6.3, the available power for RF transmission is fixed. Therefore, as the remote terminal moves far away from the relay (i.e.,  $d_2$  increases),

the performance of the hybrid VLC/RF transmission system degrades, as expected.

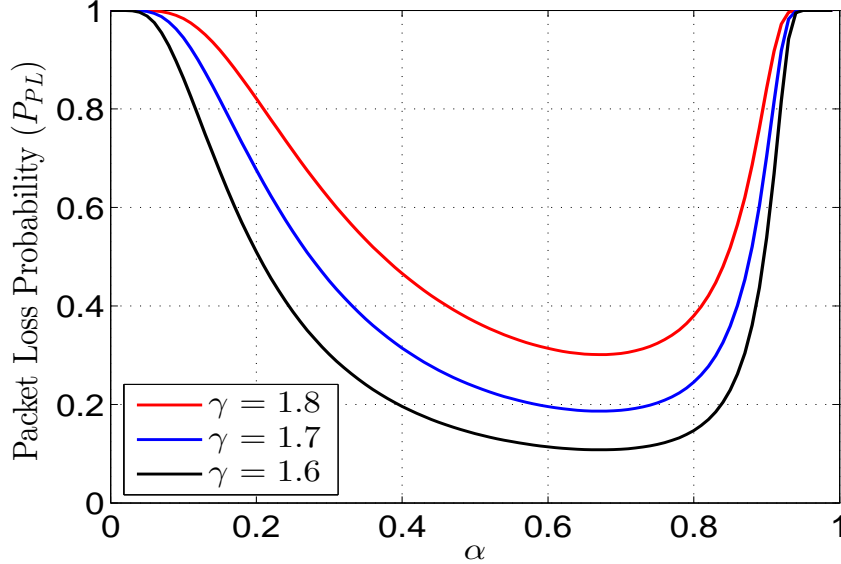


Figure 6.4: Packet loss probability for different values of  $\gamma$  with  $d_2 = 15m$ .

In Fig. 6.4, we plot the packet loss probability as function of the parameter  $\alpha$  for different values of the path loss exponent  $\gamma$  and fixed value of the remote terminal distance from the relay of  $d_2 = 15$  m. It can be seen from Fig. 6.4, that as  $\gamma$  increases, the packet loss probability increases due to the increase of the RF channel path loss.

In Fig. 6.5, we plot the packet loss probability  $P_{PL}$  as function of the parameter  $\alpha$  for different values of the packet size  $B$  and fixed value of the remote terminal distance from the relay of  $d_2 = 15$  m and a fixed path loss exponent of  $\gamma = 1.6$ . The relation between  $P_{PL}$  and  $\alpha$  follows the same trend as in Fig. 6.3. It can be seen that increasing the packet size  $B$  leads to an increase in the packet loss probability for the same value of  $\alpha$ . This can be explained with the aid of (6.17). Increasing the packet size  $B$  leads to proportionate increase in the RF transmission rate  $R_{2T}$ . This leads to increase in packet loss probability  $P_{PL}$ . It can be noticed that as  $B$  increases, the optimal value  $\alpha^*$  decreases.

It is worth noting that the value of  $\mu_x$  reflect the amount of light energy that can be harvested. Thus, as  $\mu_x$  increases, more electrical power on average will be available for the data packet retransmission process over the second-hop RF channel, and thus the probability of packet loss will decrease and all the curves in Fig. 6.3 and Fig. 6.4 will go down. Also, it is worth noting that the system performance in terms of the data packet loss probability is improved by increasing the delay time constraint

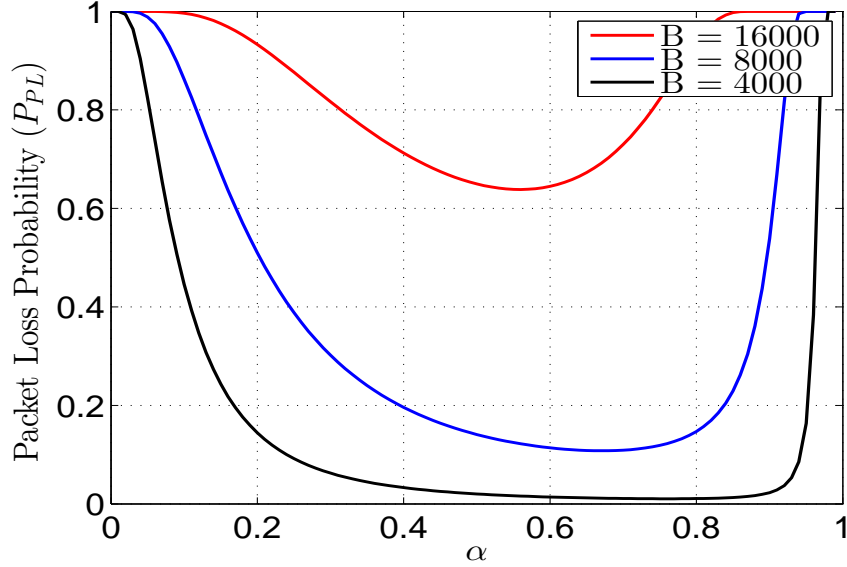


Figure 6.5: Packet loss probability for different values of  $B$  with  $d_2 = 15m$  and  $\gamma = 1.6$ .

$T_d$ . This is because increasing  $T_d$  allows more time to harvest light energy and to retransmit the data packet over the second-hop RF channel at lower data rate.

## 6.5 Summary

In this chapter, we introduced a dual-hop VLC/RF transmission system with an energy harvesting relay to extend the coverage of indoor VLC systems. The relay between the two hops harvests indoor light energy which is used to retransmit the data packet to the mobile terminal over the RF channel. We considered a main QoS constraint for the data services applications, which is transmitting a data packet to the mobile terminal within a strict end-to-end time delay. Considering this QoS constraint, we analyzed the probability of data packet loss. The parameter  $\alpha$  determines the time available for excess light energy harvesting and the time available for data packet retransmission. This parameter was found to affect the system performance. An optimal value of  $\alpha$  exists that minimizes packet loss probability. This optimal value was found to be independent of the mobile terminal distance and the path loss exponent. However, the optimal value of  $\alpha$  showed inverse dependence on the packet size. For a certain value of packet size  $B$ , the optimal value  $\alpha^*$  can be determined off-line using standard optimization techniques such as golden-section search method.

## Chapter 7

# Optimal Design of Dual-Hop VLC/RF Communication System with Energy Harvesting

In this chapter, we introduce a dual-hop VLC/RF system as a new approach in hybrid VLC/RF systems to extend the coverage of indoor wireless system based on VLC. In this proposed hybrid VLC/RF system, the optical source, specifically a LED source uses a SIM scheme to transmit the information over a VLC channel to a relay. The relay uses DD scheme to retrieve the information. The relay harvests energy from the LED light. Then, the second-hop RF transmission uses the harvested energy over the first-hop VLC transmission to retransmit these information to a mobile terminal.

The remainder of the chapter is organized as follows. In section 7.1, we introduce the dual-hop VLC/RF transmission system model. In section 7.2, we design the optimal VLC bias and analysis the performance of the proposed system in terms of its average end-to-end data rate. Finally, section 7.3 presents some numerical examples to investigate the performance of the proposed hybrid VLC/RF transmission system, followed by the chapter summary in section 7.4.

### 7.1 Dual-Hop VLC/RF Transmission System Modeling

The general block diagram of a dual-hop hybrid VLC/RF communication system with energy-harvesting relay is shown in Fig. 7.1. Assuming time division relaying scheme,

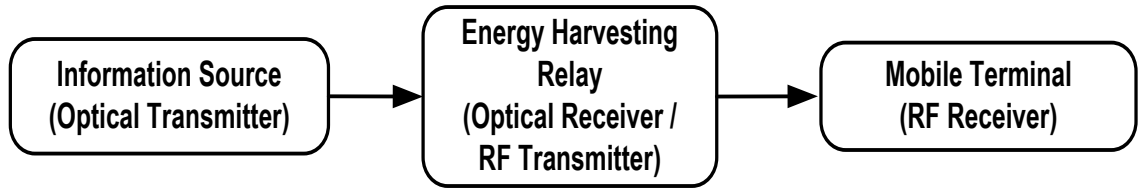


Figure 7.1: General block diagram of a dual-hop hybrid VLC/RF system

in the first time slot of duration  $T_1$ , the information source terminal sends its signal over the VLC channel to the relay terminal. In the second time slot of duration  $T_2$ , the relay retransmits the source information to the mobile terminal over the RF channel. The relay harvests the light energy from the LED source during  $T_1$  and  $T_2$ . Here, the relay is assumed to be located in a fixed position, where it has a clear LOS communication link to the LED source. On the other hand, the designated user can move freely within the room. A detailed block diagram of the proposed system is shown in Fig. 7.2, which will be discussed in the following subsections.

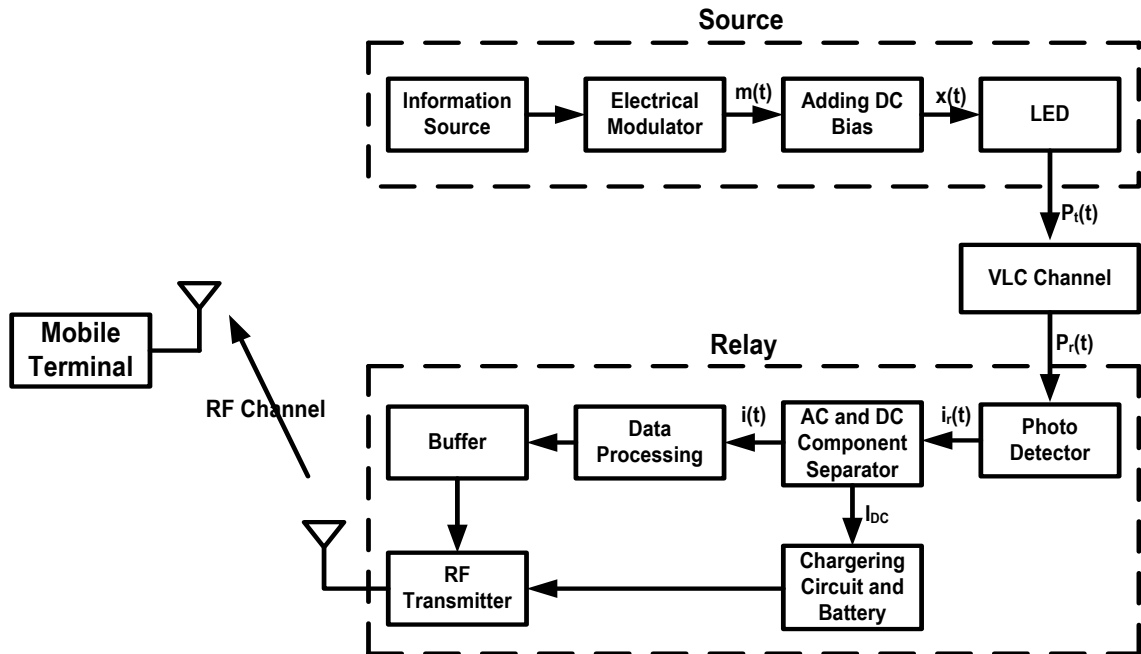


Figure 7.2: Detailed block diagram of a dual-hop hybrid VLC/RF system

### 7.1.1 Optical Signal Transmission and Detection

The bit stream from the information source is first used to modulate an RF subcarrier to produce signal  $m(t)$ . A DC bias  $B$  is added to the electrical modulated signal to insure that  $m(t)$  is non-negative, before being used to modulate the optical intensity of a LED array. At the same time, this DC bias places the LED in the proper operation mode. The transmitted optical signal can be written as:

$$P_t(t) = NP_{LED}[B + m(t)], \quad (7.1)$$

where  $N$  is the number of LEDs in the LED array, and  $P_{LED}$  is the single LED power with units of Watt/Ampere assuming identical LEDs. At the relay, the received optical power is converted into electrical current through direct detection at the photo-detector. The electrical current  $i_r(t)$  at the output of the photo-detector can be written as:

$$i_r(t) = \eta HP_t(t) + n(t) = I_{DC} + i(t) + n(t), \quad (7.2)$$

where  $\eta$  is the photo-detector responsivity in  $A/W$  and  $H$  is the VLC channel power gain.  $n(t)$  is an AWGN coming from ambient shot light noise and thermal noise, with zero mean and total variance  $\sigma_1^2 = \sigma_{shot}^2 + \sigma_{thermal}^2$ , where  $\sigma_{shot}^2$  is the shot noise variance and  $\sigma_{thermal}^2$  is the thermal noise variance [79]. Thus, the noise power is given by  $\sigma_1^2 = N_0W$ , where  $N_0$  is the noise power spectral density and  $W$  is the modulation bandwidth for the LED [45].

The VLC channel power gain  $H$  is given by [80]:

$$H = \frac{A_r(\xi + 1)}{2\pi d_1^2} \cos^\xi(\phi) \cos(\psi), \quad (7.3)$$

where  $A_r$  is the physical area of the photo-detector,  $\xi$  is the Lambert index that depends on the semi-angle at half luminance  $\phi_{1/2}$ , as  $\xi = -1/\log_2 \cos(\phi_{1/2})$ ,  $d_1$  is the transmission distance from the LED to the illuminated surface of the photo-detector,  $\phi$  is the irradiance angle, and  $\psi$  is the incidence angle.

### 7.1.2 Information Processing at the Relay

From (7.2), the AC component  $i(t) = \eta HNP_{LED}m(t)$  carries the information. To avoid clipping distortion by the nonlinearity of the LED, the input electrical signal to the LED must be within the linear region of LED operation. This can be done by adjusting the DC bias current  $B$  such that it is within the dynamic range of operation of the LED denoted by  $D\Delta I_H - I_L$ , where  $I_L$  denotes the minimum input bias current and  $I_H$  denotes the maximum input bias current. In this case, the input electrical signal  $m(t)$  varies around the DC bias  $B$  with peak amplitude given by:

$$A = \begin{cases} B - I_L, & \text{if } B < \frac{I_L + I_H}{2} \\ I_H - B, & \text{if } B \geq \frac{I_L + I_H}{2}. \end{cases} \quad (7.4)$$

Thus, the received electrical power  $P_r^e$  will be given by  $P_r^e = (\eta HNP_{LED}A)^2$ . The received electrical SNR at the relay, denoted by  $\gamma_1$ , can then be defined as:

$$\gamma_1 = \frac{(\eta HNP_{LED}A)^2}{\sigma_1^2}. \quad (7.5)$$

### 7.1.3 Energy Harvesting at the Relay

The maximum amount of energy that the relay can harvest is given by [50]:

$$E_h = 0.75I_{DC}V_{oc}(T_1 + T_2), \quad (7.6)$$

where  $I_{DC} = \eta HNP_{LED}B$  is the DC component of the output current  $i_r(t)$  from the photo-detector and  $V_{oc}$  is the open circuit voltage of the photo-detector.  $V_{oc}$  is related to  $I_{DC}$  as  $V_{oc} = V_t \ln\left(\frac{I_{DC}}{I_0} + 1\right)$  [50], where  $V_t$  is the thermal voltage ( $V_t \approx 25$  mVolt) and  $I_0$  is the dark saturation current of the photo-detector ( $I_0$  is in the order of  $10^{-9} \sim 10^{-12}$  Ampere [75]).  $E_h$  is upper bounded by  $E_h = 0.75T_1V_tI_{DC}^2/I_0$ .

The harvested energy is used for three purposes in our system: 1) to power data processing electronics, 2) to power charging circuit electronics, and 3) to charge the battery for the RF transmission. In general, the data processing and charging management circuit consumes much less energy compared to the RF transmission.

### 7.1.4 Information Transmission over RF Channel

The relay will use the harvested energy  $E_h$ , which is stored in the battery, to retransmit the data to the mobile terminal during  $T_2$ . At steady state condition, the RF retransmission power is equal to  $E_h/T_2$ . Accordingly, the instantaneous received SNR at the mobile terminal, denoted by  $\gamma_2$  can be defined as:

$$\gamma_2 = \frac{|h_2|^2 E_h / T_2}{G_2 \sigma_2}, \quad (7.7)$$

where  $|h_2|^2$  is the RF channel power gain with  $E[|h_2|^2]$  normalized to unity, where  $E[\cdot]$  is the expectation operator, and  $\sigma_2$  is the noise power assuming AWGN noise.  $G_2$  is the second-hop path loss defined as  $G_2 = (4\pi d_0 / \lambda)^2 (d_2 / d_0)^\gamma$ , with  $\lambda$  is the used RF carrier wavelength,  $d_0 = 1m$  is the reference distance,  $d_2$  is the distance from the relay to the destination terminal, and  $\gamma$  is the path loss exponent (typically,  $\gamma$  takes values 1.6 - 1.8 in indoor situations [74]). The RF fading gain  $h_2$  is modeled by Nakagami- $m$  distribution. The PDF of  $|h_2|^2$  is given by [59] as

$$f_{|h_2|^2}(|h_2|^2) = \frac{m^m (|h_2|^2)^{m-1}}{\Gamma(m)} \exp(-m|h_2|^2), |h_2|^2 \geq 0, \quad (7.8)$$

where  $m$  is the Nakagami- $m$  parameter indicating the fading severity over the second-hop RF channel. Accordingly, the received SNR  $\gamma_2$  will have the following PDF and CDF, respectively as [59]

$$f_{\gamma_2}(\gamma_2) = \frac{\left(\frac{m}{\bar{\gamma}_2}\right)^m \gamma_2^{m-1}}{\Gamma(m)} \exp\left(-\frac{m\gamma_2}{\bar{\gamma}_2}\right), \gamma_2 \geq 0, \quad (7.9)$$

$$F_{\gamma_2}(\gamma_2) = \frac{1}{\Gamma(m)} \gamma \left(m, \frac{m\gamma_2}{\bar{\gamma}_2}\right), \gamma_2 \geq 0, \quad (7.10)$$

where  $\bar{\gamma}_2$  is the average SNR of the second-hop RF channel given by  $\bar{\gamma}_2 = E_h / T_2 G_2 \sigma_2$  and  $\gamma(\cdot, \cdot)$  is the lower incomplete Gamma function defined in [53, Eq. (8.350.1)].

## 7.2 Average End-to-End Data Rate Analysis with Optimal VLC Bias Design

Suppose that the LED source transmits data to the relay with rate  $R_1$  bits/second/Hz and the relay retransmits the data to the mobile terminal with rate  $R_2$  bits/second/Hz. The data rate of the whole system will be limited by the smaller data rate between the two hops, given by  $R = \min(R_1, R_2)$ , where  $R_1$  is given by the lower bound on the capacity of the VLC channel [81] as  $R_1 = \log_2 \left(1 + \frac{c}{2\pi} \gamma_1\right)$ , and  $R_2$  is given by the well-known Shannon formula as  $R_2 = \log_2 (1 + \gamma_2)$ . We assume that the signals transmitted over two hops have the same bandwidth. It is clear that increasing the DC bias  $B$  will lead to an increase in the amount of harvested energy at the relay which leads to an increase in the data rate of the second-hop RF channel  $R_2$ . However, to transmit more information over the first-hop VLC channel, we need to reduce the DC bias  $B$  to increase the received electrical power  $P_r^e$  and thus increase  $R_1$ . Thus, the optimal DC bias needs to be designed. In what follows, we present two methods to design the optimal VLC DC bias.

### 7.2.1 Optimal VLC Bias Design Based on Average End-to-End Data Rate (ADR-Based method)

Since the first-hop VLC channel is static channel in its nature and the second-hop RF channel is dynamic channel, then the average end-to-end data rate, denoted by  $\bar{R}$ , can be obtained by using the law of total expectation as:

$$\begin{aligned}
 \bar{R} &= E[\min(R_1, R_2)] \\
 &= E[R_1 | R_1 \leq R_2] P_r[R_1 \leq R_2] + E[R_2 | R_1 > R_2] P_r[R_1 > R_2] \\
 &= R_1 [1 - F_{\gamma_2}(c)] + F_{\gamma_2}(c) \int_0^c \log_2(1 + \gamma_2) f_{\gamma_2}(\gamma_2) d\gamma_2,
 \end{aligned} \tag{7.11}$$

where  $c = 2^{R_1} - 1$ . To evaluate the integral part of (7.11), after the substitution with (7.9), we first express  $\log_2(1 + \gamma_2)$  as  $\ln(1 + \gamma_2) / \ln(2)$ . Then, by applying the integration by part rule, and using [53, Eqs. (2.33.10) and (8.352.7)], along with the

binomial expansion rule,  $\bar{R}$  can be expressed in this case in a closed form as:

$$\bar{R} = R_1[1 - F_{\gamma_2}(c)] - \frac{F_{\gamma_2}(c)}{\Gamma(m) \ln(2)} \left\{ \ln(1+c) \Gamma\left(m, \frac{mc}{\bar{\gamma}_2}\right) - (m-1)! \exp\left(\frac{m}{\bar{\gamma}_2}\right) \sum_{i=0}^{m-1} \sum_{k=0}^i \frac{(-m/\bar{\gamma}_2)^{i-k}}{k!(i-k)!} \left[ \Gamma\left(k, \frac{m}{\bar{\gamma}_2}\right) - \Gamma\left(k, \frac{m(1+c)}{\bar{\gamma}_2}\right) \right] \right\}, \quad (7.12)$$

where  $\Gamma(\cdot, \cdot)$  is the upper incomplete Gamma function defined in [53, Eq. (8.350.2)]. The optimal bias  $B_A^*$ , which maximizes the average end-to-end data rate  $\bar{R}$  can be obtained by solving  $\frac{\partial \bar{R}}{\partial B} = 0$  for  $B$ . However, it will be difficult to obtain the optimal  $B_A^*$  in closed form.

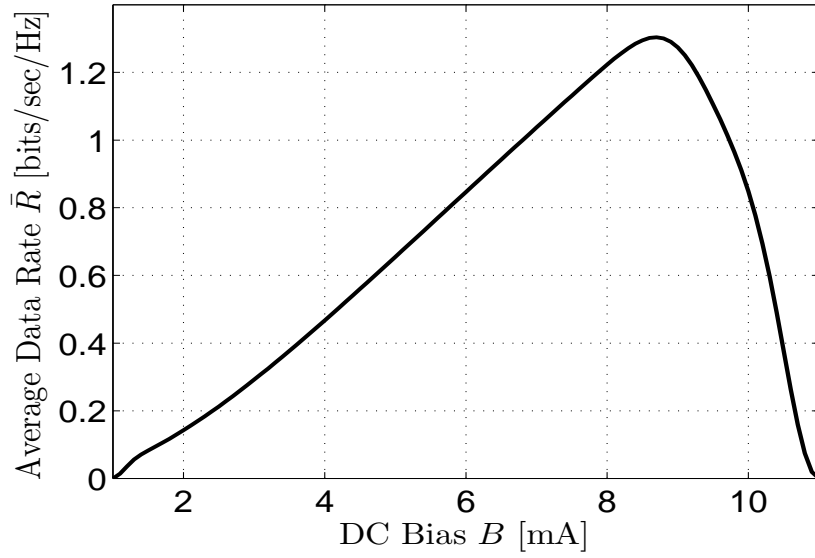


Figure 7.3: Average data rate for ADR-based method with  $d_2 = 10m$  and  $m = 1$ .

It is clear from Fig. 7.3 that  $\bar{R}$  is a unimodal function in  $B$ . Thus, we can treat the problem as one-dimensional optimization problem with uncertainty range of  $[I_L, I_H]$ , and use numerical methods, such as Golden-section search method [68], to search for the optimal  $B_A^*$ .

## 7.2.2 Optimal VLC Bias Design Based on Instantaneous End-to-End Data Rate (IDR-Based method)

To maximize the instantaneous end-to-end data rate  $R$ , we need to solve the following optimization problem:

$$\begin{aligned} & \underset{B}{\text{maximize}} && R(B) = \min(R_1, R_2) \\ & \text{subject to} && B \in [I_L, I_H]. \end{aligned}$$

Normally, such max-min problem has solution at  $R_1 = R_2$ , which when we consider the constraint  $B \in [I_L, I_H]$ , leads to the solution:

$$B_1 = \frac{c_1 I_H - \sqrt{c_1 c_2 I_H^2 |h_2|^2}}{c_1 - c_2 |h_2|^2}, \quad (7.13)$$

with  $c_1 = eG_2\sigma_2T_2I_0$  and  $c_2 = 1.5\pi\sigma_1^2(T_1+T_2)V_T$ , where we plot  $R_1$  and  $R_2$  as function of  $B$  in Fig. 7.4 using parameters given in section 7.3.

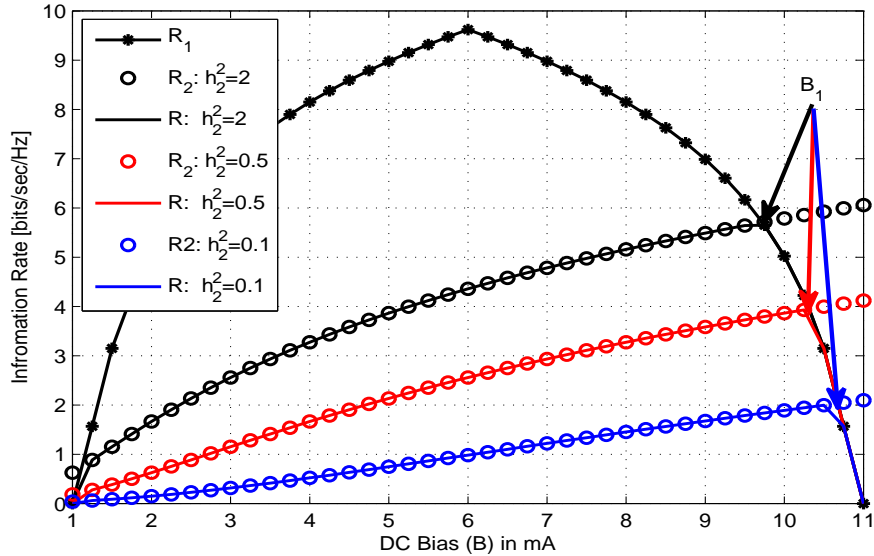


Figure 7.4: System data rates with  $d_2 = 10\text{m}$ .

When second-hop RF channel gain  $|h_2|^2$  increases (i.e., the quality of the second-hop RF channel improves), the intersection point of  $R_2$  with  $R_1$  (whose projection on the DC bias  $B$ -axis equals to  $B_1$ ) moves up towards the peak of  $R_1$  and thus the end-to-end data rate  $R$  of the whole system increases with a decrease in the required

DC bias  $B$ . However, the maximum end-to-end data rate is constrained by the peak value of  $R_1$ , which corresponds to the case when  $B_1 = (I_L + I_H)/2$  (equals to 6 mA in Fig. 7.4 that occurs when:

$$|h_2|^2 \equiv |h_2|_T^2 = \frac{\left(\sqrt{c_1 c_2 I_H^2} - \sqrt{c_1 c_2 I_H^2 - 4c_1 c_2 c_m (I_H - c_m)}\right)^2}{4c_2^2 c_m^2}, \quad (7.14)$$

where  $c_m = (I_L + I_H)/2$ . Thus, the optimal DC bias, denoted by  $B_I^*$ , in this case can be chosen according to the following criteria:

$$B_I^* = \begin{cases} B_1, & \text{if } |h_2|^2 \leq |h_2|_T^2 \\ \frac{I_L + I_H}{2}, & \text{if } |h_2|^2 > |h_2|_T^2, \end{cases} \quad (7.15)$$

with optimum data rate  $R(B_I^*) = R_1(B_I^*) = R_2(B_I^*)$ . Accordingly, the average end-to-end data rate, with optimal DC bias  $B_I^*$  chosen based on the instantaneous RF channel power gain  $|h_2|^2$ , is obtained by averaging the optimal data rate  $R(B_I^*)$  over the distribution of  $|h_2|^2$  as:

$$\bar{R} = \int_0^{|h_2|_T^2} R(B_I^*) f_{|h_2|^2}(|h_2|^2) d|h_2|^2 + \int_{|h_2|_T^2}^{\infty} R(B_I^*) f_{|h_2|^2}(|h_2|^2) d|h_2|^2. \quad (7.16)$$

The first integral part of (7.16) can be evaluated numerically as it is hard to be obtained in closed form. The second integral part of (7.16), can be given in a closed form as  $\frac{\Gamma(m, m|h_2|_T^2)}{\Gamma(m)} R_1|_{B_I^*=(I_L+I_H)/2}$  by using [53, Eq. (3.351.2)].

### 7.3 Numerical Results

In this section, we present numerical examples to illustrate our analysis by using the parameters given in Table 7.1 [45, 79]. We assume  $T_1 = T_2 = 1$  second.

In Fig. 7.5, we plot the average data rate of the whole system as a function of the distance  $d_2$  from the relay to the mobile terminal. For the ADR-based method, the RF channel path loss  $G_2$  varies with  $d_2$ . For each value of  $G_2$ , we use the Golden-section search method with an accuracy of  $10^{-6}$  to find the optimal DC bias  $B_A^*$  and the corresponding average end-to-end data rate to obtain the ADR-based curve. For the IDR-based method, we use (7.16) to obtain the IDR-based curve. It can be seen from

Table 7.1: Parameters of VLC and RF subsystems

Parameter	Symbol	Value
Single LED Power	$P_{LED}$	20 $mW/A$
Minimum Bias Current	$I_L$	1 $mA$
Maximum Bias Current	$I_H$	11 $mA$
Semi-angle at Half Luminance	$\phi_{1/2}$	15 $deg.$
Irradiance Angle	$\phi$	20 $deg.$
Incidence Angle	$\psi$	20 $deg.$
VLC Channel Range	$d_1$	1.5 $m$
Physical Area of Photo-detector	$A_r$	0.04 $m^2$
Photo-detector Responsivity	$\eta$	0.53 $A/W$
Number of LEDs in the Array	$N$	10
VLC Noise Power Spectral Density	$N_0$	$10^{-21}$ $A^2/Hz$
Modulation Bandwidth for LED	$W$	40 $MHz$
Dark Saturation Current of Photo-detector	$I_0$	$10^{-9}$ $A$
RF Noise Power	$\sigma_2$	$10^{-8}$ $W$
RF Path Loss Exponent	$\gamma$	1.6

Fig. 7.5 that, the average data rate decreases as  $d_2$  increases, using either ADR-based method or IDR-based method in choosing the optimal DC bias. However, the average end-to-end data rate had shown improvement when the optimal DC bias is chosen based on the instantaneous RF channel power gain  $|h_2|^2$  (IDR-based method) over the method when the optimal DC bias is chosen based on RF channel path loss  $G_2$  (ADR-based method), especially, at smaller distances between the mobile terminal and the relay. As the distance  $d_2$  increases, the performance of the two methods approach to each other. Note that, the performance advantage of the IDR-based method comes at the cost of requiring instantaneous channel knowledge of  $|h_2|^2$  at the LED source to calculate the optimal DC bias  $B_f^*$  according to the criteria given by (7.15).

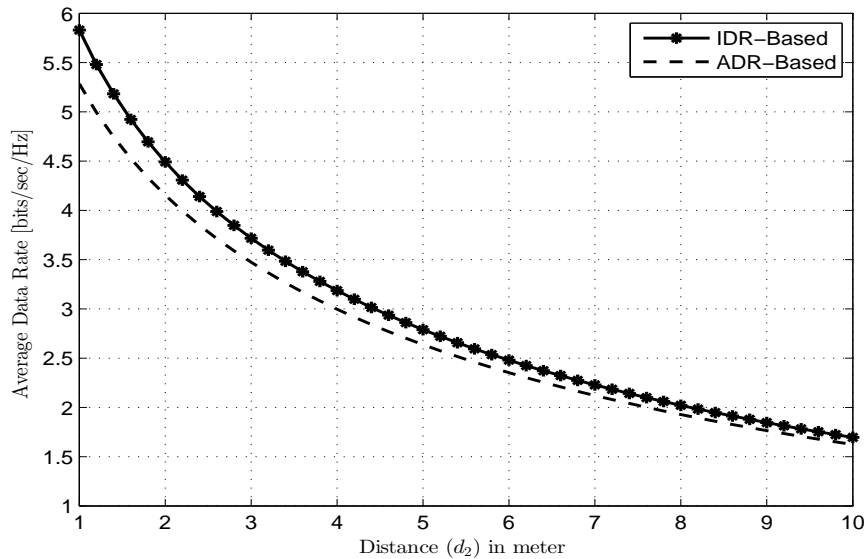


Figure 7.5: System average data rate with optimal DC bias.

## 7.4 Summary

In this chapter, we presented a dual-hop heterogeneous communication system that composed of two different types of communication links, specifically, VLC and RF links. A relay between the two hops is able to harvest energy from the VLC link and uses it to retransmit the data to a mobile terminal over the RF link. The DC bias imposed on the electrical signal at the LED source, before being transmitted over the first-hop VLC channel, affects both the power of the transmitted electrical signal over the first-hop VLC channel and the amount of energy harvested by the relay. Thus, it affects the data rates of both hops of the hybrid VLC/RF system. Two methods of designing the optimal DC bias were introduced and the corresponding end-to-end average data rate of the system in each case was analyzed. One method is based on the second-hop RF channel's instantaneous power gain (IDR-based method) and the other one is based on the second-hop RF channel's path loss (ADR-based method). The IDR-based method was shown to give better average data rate performance over the ADR-based method. However, the performance advantage of the IDR-based method comes at the cost of requiring instantaneous second-hop RF channel knowledge at the LED source.

## Chapter 8

# Conclusions and Future Work

In this chapter, we conclude the thesis by summarizing the accomplished work and suggesting some potential further research topics.

### 8.1 Conclusions

In this thesis, we first presented and analyzed a new transmission scheme for hybrid FSO/RF systems. This transmission scheme is based on adaptive combining. The exact CDF of the received SNR for the proposed hybrid FSO/RF system with adaptive combining is obtained, which is used to study the system outage performance. Hybrid FSO/RF system with adaptive scheme had shown improved outage performance compared to FSO-only and RF-only systems in all weather conditions and atmospheric turbulence regimes.

To effectively use the available resources of hybrid FSO/RF systems with adaptive combining scheme, we also presented two new joint adaptive schemes. One is joint adaptive modulation and adaptive combining scheme. We obtained a closed-form of the exact CDF of the received SNR for the proposed adaptive hybrid FSO/RF system. This proposed adaptive hybrid FSO/RF system had shown improved spectral efficiency and outage performance compared to that of switch-over hybrid FSO/RF and FSO-only systems, while maintaining good average BER. The other joint adaptive scheme is joint power adaptation and adaptive combining scheme. In this adaptive scheme, two new power adaptation policies that are based on a modified TCI were implemented on the RF link of the hybrid FSO/RF system. These two policies were defined as  $\gamma_{RF}$ -based TCI adaptation policy and  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation

policy. Closed form for the system outage probability for each policy was derived. Hybrid FSO/RF system with this joint adaptive scheme had shown improved outage performance compared to outage performance of the same system without power adaptation, while conserving RF power. Also, we have showed that  $\gamma_{RF}$ -based TCI adaptation policy achieves better outage performance than  $\gamma_{RF} + \gamma_{FSO}$ -based TCI adaptation policy.

Considering a multi-user scenario, we proposed and analyzed a new P2MP Hybrid FSO/RF Network. In this network, a common backup RF link is used by the central node for data transmission to any remote node in case of the failure of its corresponding FSO link. We developed a discrete-time Markov chain model for the transmit buffer of the link between the central node and a single remote node (tagged node). Studying the tagged node allowed us to investigate several performance criteria such as throughput from central node to the tagged node, the average transmit buffer size, the symbol queuing delay in the transmit buffer, the efficiency of the queuing system, the symbol loss probability, and the RF link utilization. Using a common backup RF link in the P2MP Hybrid FSO/RF network had achieved considerable performance improvement over the P2MP FSO-only network.

To extend the coverage of indoor VLC systems, we introduced a dual-hop VLC/RF transmission system with an energy harvesting relay. We proposed two approaches for energy harvesting at the relay between the two hops. In the first approach, the relay harvests indoor light energy. Considering QoS constraint of a strict end-to-end time delay, we analyzed the probability of data packet loss. The parameter  $\alpha$  that determines the time available for excess light energy harvesting and the time available for data packet retransmission was found to affect the system performance. An optimal value of  $\alpha$  that minimizes packet loss probability was found to be independent of the mobile terminal distance and the path loss exponent.

In the second approach, the relay harvests energy from the received optical signal. The amount of harvested energy is related to the DC bias that was imposed on the electrical signal at the LED source. Two methods of designing the optimal DC bias were introduced and the corresponding end-to-end average data rate of the system in each case was analyzed. One method is based on the second-hop RF channel's instantaneous power gain (IDR-based method) and the other one is based on the second-hop RF channel's path loss (ADR-based method). The IDR-based method was shown to give better average data rate performance over the ADR-based method at the cost of requiring instantaneous second-hop RF channel knowledge at the LED

source.

## 8.2 Future Work

The ideas proposed in this thesis can be expanded in the future in different directions:

1. We have focused in this thesis, mainly in chapters 2-5, for outdoor data transmission on the FSO systems which require line-of-sight. UV systems can achieve outdoor NLOS data transmission. However, there are a lot of challenges in using UV systems. Many open research topics in this field including channel modeling, performance limitation, trade-off studies such as data rate and communication range trade-offs, and UV transceiver design can be considered in future work.
2. We have assumed in chapter 5 that, when more than one FSO link fail, the central node will use the RF link to communicate with one of the corresponding remote nodes on an equal priority basis. Using other protocols such as unequal priority protocol, round robin protocol, random delay protocol, and delay aware scheduling protocol will affect the Markov chain model and thus the system performance. These arbitration/scheduling protocols can be considered in future work.
3. We have introduced a dual-hop VLC/RF system in chapters 6 and 7. In this system, we assumed that LED source already have the data to be transmitted. However, the LED source should access the backbone information network to acquire the data. Power Line Communication (PLC) systems utilize the ubiquitous power line network to power the LED sources while serving as the backbone network for the VLC systems. Hybrid PLC/VLC/RF systems can be considered in future work.

# Appendix A

## Proof of Proposition 1

We had adopted the distribution fitting approach to validate proposition 1. First we generate one million log-normally distributed random numbers  $x$  that represent the samples of  $I_{sc}$  with mean  $= \mu_x$  and variance  $= \sigma_x^2$ . The histogram of  $I_{sc}$  and its log-normal distribution fitting is shown in Fig. A.1a. By using these samples, we generate another set of samples  $y$  for the output power  $P_h$  by using the relationship  $y = 0.75V_t x \ln\left(\frac{x}{I_0} + 1\right)$ . By drawing the histogram of  $P_h$ , it can be observed that it fits a log-normal distribution as shown in Fig. A.1b. The red curve in Fig. A.1b is the log-normal distribution fitting to the histogram for two different values of  $I_0$ . This red curve is plotted by using the MATLAB function `histfit`. Other distributions were attempted but it was found that the log-normal distribution provides the best fit. Thus, we conclude that  $P_h$  follows a a log-normal distribution  $P_h \sim \text{LN}(\mu_y, \sigma_y)$ , where  $\mu_y$  and  $\sigma_y$  are the mean and the standard deviation of  $P_h$ .

Also, since  $I_{sc}$  is in the order of  $10^{-3} \sim 10^{-6}$  Ampere [77], which is very large compared to  $I_0$ , then the term  $\ln\left(\frac{I_{sc}}{I_0} + 1\right)$  in (6.10) tends to be constant and  $P_h$  in (6.10) will be a monotonically increasing function in  $I_{sc}$ . Thus, it is logic to find that the output power  $P_h$  has the same statistical distribution as  $I_{sc}$ , i.e., log-normal distribution.

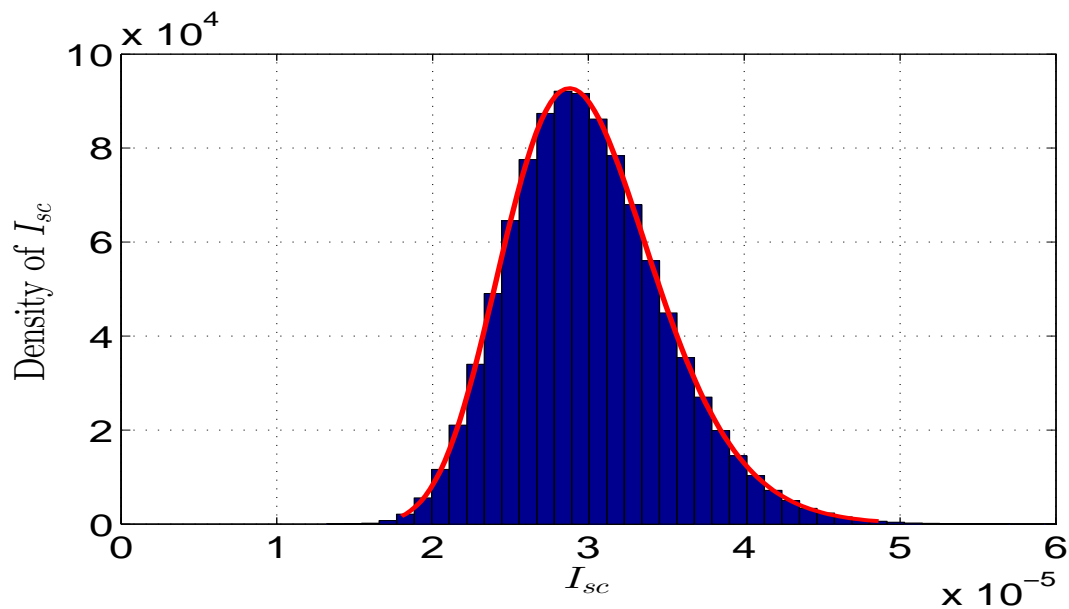
Defining the function  $f(x) = P_h = 0.75V_t x \ln\left[\frac{x}{I_0} + 1\right]$ , then  $\mu_y$  is calculated as [78]:

$$\mu_y = \int_0^{\infty} f(x) f_{I_{sc}}(x) dx, \quad (\text{A.1})$$

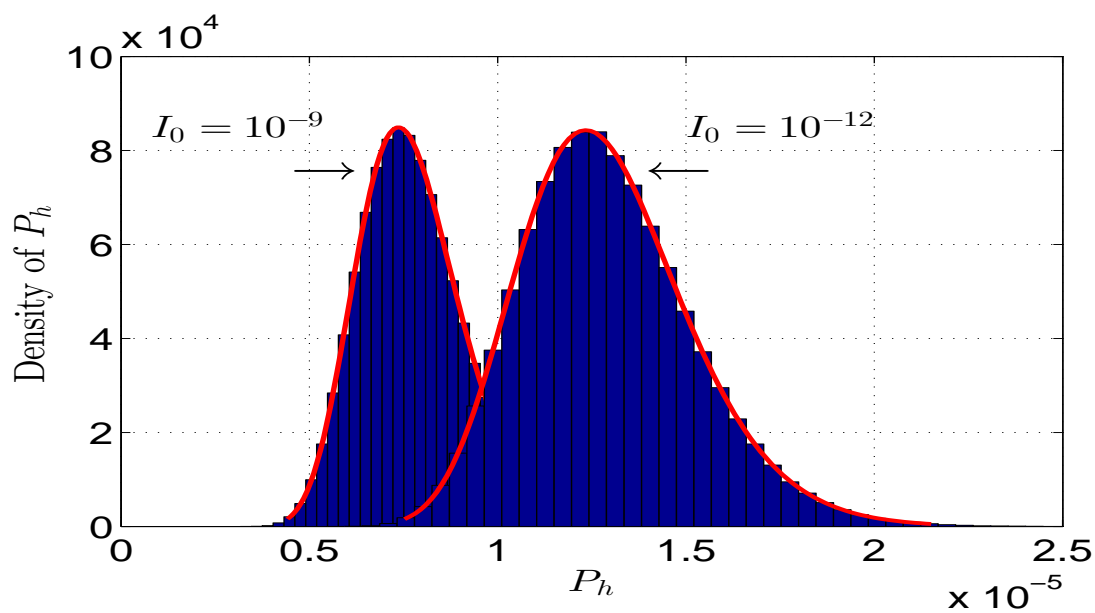
where  $f_{I_{sc}}(x)$  is the PDF of  $I_{sc}$  given by (6.11), and  $\sigma_y$  is calculated approximately

as [78]:

$$\begin{aligned}\sigma_y &\approx \sigma_x \left. \frac{df(x)}{dx} \right|_{x=\mu_x} \\ &= 0.75 \sigma_x V_t \left[ \frac{x}{x+I_0} + \ln \left( \frac{x}{I_0} + 1 \right) \right]_{x=\mu_x} \\ &= 0.75 \sigma_x V_t \left[ \frac{\mu_x}{\mu_x+I_0} + \ln \left( \frac{\mu_x}{I_0} + 1 \right) \right].\end{aligned}\tag{A.2}$$



(a) Histogram of  $I_{sc}$  assuming  $\mu_x = 3 \times 10^{-5}$  Ampere,  $\sigma_x = 0.5 \times 10^{-5}$  Ampere.



(b) Histogram of corresponding  $P_h$  for  $I_0 = 10^{-9}$  and  $10^{-12}$  Amperes.

Figure A.1: Histograms of  $I_{sc}$  and  $P_h$  and their log-normal distribution curve fitting.

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